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**TIDAL PARAMETERS
DERIVED FROM THE PERTURBATIONS
IN THE ORBITAL INCLINATIONS OF THE
BE-C, GEOS-I, AND GEOS-II SATELLITES**

DAVID PARRY RUBINCAM

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FROM THE PERTURBATIONS IN THE ORBITAL
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THE ORBITAL INCLINATIONS OF THE BE-C, GEOS-I,
AND GEOS-II SATELLITES

David Parry Rubincam

Geodynamics Branch

April 1976

GODDARD SPACE FLIGHT CENTER
Greenbelt, Maryland

ABSTRACT

The tidal perturbations in the orbital inclinations of the BE-C, GEOS-I, and GEOS-II satellites are analyzed. Effective tidal Love numbers and phase angles for the O_1 , K_1 , M_2 , K_2 , P_1 , and S_2 tides are recovered. The effective tidal phase angles tend to be on the order of a few degrees. The effective tidal Love numbers are generally less than the solid earth Love number k_2 of about 0.30. This supports the contention of Lambeck, et al. (1974) that the ocean tides give an apparent depression of the solid earth Love number. Ocean tide amplitudes and phases are calculated for the above tides assuming $k_2 = 0.30$ and the solid earth lag angle $\phi_2 = 0$. The results show good agreement with Felsentreger, et al. (1976) on GEOS-I but not on GEOS-II. The M_2 effective Love number and phase angle are poorly determined, but give a lunar acceleration of -29 ± 15 arc sec/(100 yr)², an energy dissipation of $-3.6 \pm 1.8 \times 10^{19}$ erg/sec, and a tidal function time scale of 1.4×10^9 yr when averaged over all three satellites. This is in fair agreement with current estimates.

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TIDAL PARAMETERS DERIVED FROM THE PERTURBATIONS IN
THE ORBITAL INCLINATIONS OF THE BE-C, GEOS-I,
AND GEOS-II SATELLITES

INTRODUCTION

The sun and moon raise tides on the earth; the displaced mass perturbs the orbits of earth satellites. These perturbations may be analyzed in order to learn about the earth's tides.

Early analyses of the tidal perturbations performed by Kozai (1965, 1968), Newton (1965, 1968), Anderle (1971), Smith, et al. (1973), and Douglas, et al. (1974) were aimed at recovering the Love number k_2 and lag angle ϕ_2 of the solid earth tide. The resulting Love numbers were found to be generally smaller than the well-known value for k_2 of about 0.29 to 0.31 obtained from seismic studies (e.g., Longman, 1966). The discrepancy has been ascribed by Lambeck (1974) and Lambeck et al. (1974) to the corruption of the solid earth tidal signal by the ocean tides (and to a lesser extent the atmospheric tides), which Kaula (1962) showed might be significant. The ocean tides give the appearance of Love numbers and lag angles which vary from constituent to constituent. Accordingly, some satellite data have been re-analyzed (Lambeck, et al. 1974; Felsentreger, et al. 1976) in an effort to learn about the solid earth, ocean, and atmospheric tides.

We continue with such a re-analysis here by examining the tidal perturbations in the orbital inclination of three different earth satellites: BE-C (Beacon Explorer C), GEOS-I, and GEOS-II. Table 1 gives pertinent information about the satellites. Inclination perturbations are analyzed because they give a relatively clean separation of tidal effects from other disturbing forces.

THE DATA

The BE-C data consists of 36 laser observations, spanning a 501 day period beginning in July 1970. The amplitude of the variation in inclination is about 1.0 arc seconds (40 meters). For further details, see Smith, et al. (1973). The GEOS-I consists of 142 TRANET Doppler observations spaced over 626 days, beginning in February 1966. The amplitude of the tidal signal is about 1.2 arc second (36 meters). The GEOS-II data is composed of 113 precision reduced camera and TRANET Doppler observations taken over a 651 day period beginning in March 1968. For further details, see Felsentreger, et al. (1976).

In each case the well-known disturbing forces were modelled and removed, so that the remaining perturbations are presumably due almost entirely to the tides.

ANALYTICAL EXPRESSION FOR THE INCLINATION VARIATION

We now derive an analytical expression for the total tidal perturbation in the inclination of the orbit of an earth satellite by modifying the equation for the solid earth tidal potential.

The solid earth tidal potential expressed in orbital elements is given by
 (Kaula, 1964)

$$U_{\ell mpq} = k_{\ell} R_E^{2\ell+1} B_{\ell m}^* C_{\ell mpq} \sum_{h,j} C_{\ell mhj} \cdot \cos \left\{ v_{\ell mpq}^* - v_{\ell mhj} - m\theta^* + m\theta + \epsilon_{\ell mpq} \right\} \quad (1)$$

where $B_{\ell m}^* = Gm^* \frac{(\ell - m)!}{(\ell + m)!}$, $C_{\ell mpq}^* = \frac{F_{\ell mp}(I^*) G_{\ell pq}(e^*)}{a^{*\ell+1}}$

and $v_{\ell mpq}^* = (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^*$

The starred (*) quantities refer to the disturbing body (sun or moon) and the unstarred refer to the satellite. The sign in front of the tidal phase angle $\epsilon_{\ell mpq}$ had been minus in Kaula's original formulation; Lambeck, et al. (1974) changed the sign to plus, which makes the important phase angles positive quantities in the case of a frictionally-delayed solid earth tidal bulge. We follow the convention of Lambeck, et al. here.

We wish to find the total tidal potential $T_{\ell mpq}$ caused by the solid earth, oceans, and atmosphere, since this is the potential felt by a satellite. We limit the discussion to $\ell = 2$, since the second degree terms dominate the motion of

the satellite and the evolution of the earth-moon system. (For a discussion of fourth degree terms, see below and Appendix 2.)

In finding the total tidal potential of degree 2 we make the following assumption: the amplitude of the potential and the phase angle become frequency-dependent. This means that the solid earth Love number k_2 in eq. (1) is replaced by the effective Love number d_{2mpq} and the solid earth phase angle ϵ_{2mpq} is replaced by the effective phase angle δ_{2mpq} . The adjective "effective" is necessary since we now refer to the tidal response of the entire earth, and not just the solid earth. This procedure takes care of any possible frequency dependence of the solid earth Love number, the response of the oceans, and the atmosphere tides. The letters "d" and "δ" are chosen to avoid possible confusion with the solid earth tides.

The total tidal potential is now to be substituted in Lagrange's planetary equations to find the perturbation in the inclination of the orbit of an earth satellite. Before doing this, however, let us make several simplifications: (a) omit the zero sum $-m\theta^* + m\theta$, (b) consider only terms for which $j = 0$ and $\ell = 2h$, to be rid of dependence on the satellite eccentricity and mean anomaly, and (c) consider only terms for which $q = 0$ to be rid of small terms which depend on the eccentricity of the disturbing body. The total tidal potential now becomes

$$T_{2mp0} = d_{2mp0} \frac{Gm^*}{R_E} \frac{(2-m)!}{(2+m)!} (2 - \delta_{0m}) \left(\frac{R_E}{a^*} \right)^3 \left(\frac{R_E}{a} \right)^3 \cdot F_{2mp}(I^*) F_{2m1}(I) \cos \left\{ (2-2p)(M^* + \omega^*) + m\Omega^* - m\Omega + \delta_{2mp0} \right\}.$$

Substitution of this potential into the Lagrange equation

$$[\dot{I}]_{\text{Lmpq}} = - \frac{1}{\sqrt{GM_E a} (1 - e^2)^{1/2} \sin I} \frac{\partial T_{\text{Lmpq}}}{\partial \Omega}$$

and integration with respect to time yields

$$\begin{aligned} \Delta I_{2mp0} &= \frac{d_{2mp0}}{\sqrt{GM_E a} (1 - e^2)^{1/2} \sin I} \left[(2 - \delta_{0m}) \frac{(2 - m)!}{(2 + m)!} m \right] \left(\frac{R_E}{a^*} \right)^3 \left(\frac{R_E}{a} \right)^3 \\ &\cdot F_{2mp}(I^*) F_{2m1}(I) \frac{\cos \left\{ (2 - 2p)(\omega^* + M^*) + m\Omega^* - m\Omega + \delta_{2mp0} \right\}}{\left[(2 - 2p)(\omega^* + M^*) + m\dot{\Omega}^* - m\dot{\Omega} \right]} \end{aligned} \quad (2)$$

We have assumed in the integration that the satellite elements, a , e , and I , as well as the nodal rate $\dot{\Omega}$ are constants. We have also assumed that $\omega^* + M^*$, $\dot{\Omega}^*$, and I^* remain constant. This last set of assumptions must be removed in the case of the moon when considering periods of time longer than a few years, due principally to the motion of the lunar node on the ecliptic.

The tidal inclination perturbation is thus given by

$$\Delta I = \sum_{\substack{m,p \\ \text{Moon}}} \Delta I_{2mp0} + \sum_{\substack{m,p \\ \text{Sun}}} \Delta I_{2mp0} + \Delta I_0$$

where ΔI_0 is a constant of integration.

We note in passing several features of eq. (1). First, tides for which $m = 0$ do not perturb the orbital inclination; thus we obtain no information on these tides. Second, the periods of the tides felt by the satellite are greatly lengthened

over their periods on the earth's surface, due to the replacement of $\dot{\theta}$ in the frequency by $\dot{\Omega}$. Third, there is no way to separate the K_1^M tide from the K_1^S tide ($\ell_{mpq} = 2110$), or the K^M tide from the K_2^S tide ($\ell_{mpq} = 2210$), since in either case the periods are the same. A hypothesis is needed to do this.

ANALYSIS OF THE DATA

Eq. (2) may be conveniently written

$$\Delta I_{2mp0} = c_{2mp0} [\cos \left\{ (2 - 2p)(\omega^* + M^*) + m\Omega^* - m\Omega \right\} - s_{2mp0} [\sin \left\{ (2 - 2p)(\omega^* + M^*) + m\Omega^* - m\Omega \right\}]]$$

for the analysis of the data. Here $c_{2mp0} = d_{2mp0} \cos \delta_{2mp0}$, $s_{2mp0} = d_{2mp0} \sin \delta_{2mp0}$, and the empty brackets denote a factor common to both terms. The coefficients c_{2mp0} and s_{2mp0} are found from multiple linear regression, from which the effective Love numbers and phase angles may be easily computed.

The regression analyses for the three satellites were carried out with the computer program described in Appendix 3. In each case the tides with the largest expected amplitudes in eq. (2) were retained in the analysis and the smaller ones ignored. The theoretical amplitudes in the solid earth signal were conveniently used to pick out the major contributors.

Table 2 gives the regression solutions. The effective Love numbers and phase angles for the K_1^M , and K_1^S tides are assumed to be the same; likewise for the K_2^M and K_2^S tides. The resulting inclination curves and residuals are shown in Figures 1 - 6.

Another computer run was made in which the effective phase angles of all but the K_1 tide in the BE-C data and the K_1 and S_2 tides in the GEOS-I and GEOS-II data (the major contributors in each signal) were set to zero. No major changes in the effective Love numbers (or in those effective phase angles solved for) took place. A similar computer run was made with only the first 28 points in the BE-C data and the first 72 points of the GEOS-I data retained. Also, 20 neighboring points in the GEOS-II data taken from the middle of July to the end of September in 1968 were removed and a run made. Again no major changes in the effective Love numbers and phase angles took place, indicating the stability of the solutions. However, the deleted points in the GEOS-II data were chosen not to disturb the basic signal, due to the spacing of the data.

Examination of Table 2 reveals good agreement between the BE-C and GEOS-I results, but poor agreement between GEOS-II and the other two satellites. Also, there is good agreement between our determination of ocean tide parameters and that of Felsentreger, et al. (1976) for GEOS-I, but no agreement on the ocean tide parameters for GEOS-II (see below). The cause of this discrepancy is unknown; hence the GEOS-II results must be treated with caution.

Most of the effective Love numbers given in Table 2 are smaller than the solid earth Love number k_2 of 0.29 to 0.31. This is in general accord with the ocean tide models and charts given in Table 2 of Lambeck, et al. (1974). The only entry in that table which predicts an effective Love number greater than k_2 is the O_1 tide chart of Dietrich. (The S_2 tide model of Bogdanov and Magarik

predicts an apparent increase in the effective Love number for GEOS-II due to a fourth degree term.) The phase angles are on the order of a few degrees, as expected, although some are negative and the BE-C K_2 and the GEOS-II P_1 effective phase angles are embarrassingly large. Also, the BE-C K_2 and GEOS-II S_2 effective Love numbers are rather large and the GEOS-II P_1 effective Love number is rather small. These presumably reflect the inadequacies of the data. However, it will be noted that all three satellites indicate a remarkably small effective Love number for the P_1 tide, apparently indicating a large ocean tide effect. If this effect is real it is highly interesting, since the O_1 tide (the lunar counterpart of the P_1 tide) shows no similar behavior. In fact, the O_1 effective Love number should be larger than k_2 according to Dietrich's chart, as mentioned above. Unfortunately, we have only one poorly determined effective Love number for the O_1 tide, and no mathematical models for either the O_1 or P_1 tide appear to exist.

SEPARATION OF OCEAN AND EARTH TIDES

We now solve for the ocean tide parameters from the satellite data in the manner of Felsentreger, et al. (1976). To do so, we assume that the tidal signal consists solely of the solid earth and ocean tides; this lumps the small atmospheric tides (principally an S_2 tide) with the ocean tides.

Separation of the ocean from the solid earth tides requires knowledge of the solid earth tidal response. If we assume the solid earth Love number to be

frequency-independent, then from Appendix 2 we have

$$c_{2mp0} = d_{2mp0} \cos \delta_{2mp0} = k_2 \cos \epsilon_{2mp0} + Z_{mp}(1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \end{bmatrix}_{m \text{ even}} \begin{bmatrix} -C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \\ -C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \end{bmatrix}_{m \text{ odd}} \quad (3)$$

$$s_{2mp0} = d_{2mp0} \sin \delta_{2mp0} = k_2 \sin \epsilon_{2mp0} + Z_{mp}(1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \\ -C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \end{bmatrix}_{m \text{ even}} \begin{bmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \end{bmatrix}_{m \text{ odd}} \quad (4)$$

where $\epsilon_{2mp0} \approx m\phi_2$ (Lambeck, et al. 1974), ϕ_2 being the solid earth lag angle and k'_2 the second degree load deformation coefficient.

The question arises as to what values to choose for k_2 , k'_2 , and ϕ_2 . Let us pick $k_2 = 0.30$ and $k'_2 = -0.30$, in accord with Longman (1966), and $\phi_2 = 0$, in accord with a high Q (~ 230) for the earth's mantle (see, e.g. Stacey, 1969).

The two rightmost columns of Table 2 give the resulting ocean tide amplitudes and phases. These are to be compared with Table 2 of Lambeck, et al. (1974) and Table 1 of Felsentreger, et al. (1976).

The ocean tide amplitudes in our Table 2 have absorbed the fourth (and higher) degree terms in the ocean tidal potential, which Lambeck, et al. (1974) showed

to be important for some tides. The fourth degree terms could be solved for from observations of two or more satellites, since these terms cause an apparent variation in the second degree effective Love number from satellite to satellite (see Appendix 2). We have chosen not to solve for them here, since the differences between the effective Love numbers tend to be several times larger than those predicted by the ocean tide models and charts; and there are no clear trends.

We may also make a rough estimate of k_2 from the ocean tides charts and models, in the manner of Lambeck, et al. (1974). For this we set

$$d_2 \approx k_2 + Z_{mp} (1 + k'_2) \begin{bmatrix} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ \end{bmatrix} \begin{matrix} m \text{ even} \\ m \text{ odd} \end{matrix}$$

and substitute the ocean tide amplitudes and phases in Table 2 of Lambeck, et al. (1974) into the right side of this equation and our values into the left. A simple average of all charts, models and satellites yields $k_2 \approx 0.27$. Performing the same calculation without the GEOS-II results gives $k_2 \approx 0.26$.

The effective Love numbers and phase angles of the well-determined tides permit an estimate of ϕ_2 as well as k_2 . Using the K_1 tide from BE-C and the K_1 and S_2 tides from GEOS-I and GEOS-II, in connection with the K_1 and S_2

tides from Table 2 of Lambeck, et al. (1974), we find from eqs. (3) and (4) that $K_2 \approx 0.29$ and $\phi_2 \approx 1.5^\circ$. Once again an arithmetic average has been taken.

From ϕ_2 we determine a rough estimate of Q for the mantle, since (see, e.g., Stacey, 1969)

$$Q \approx \frac{1}{\tan \epsilon_{2200}} \approx \frac{1}{\tan 2\phi_2}$$

yielding a value of 19. Omitting the GEOS-II results yields $k_2 \approx 0.28$, $\phi_2 \approx 4.2^\circ$, and $Q \approx 7$.

Only a simple arithmetic average is taken in the computations above because we have treated the ocean tide models and charts as "observations" without knowing how to weight them. Further, the quality of the satellite data prevents us from reading too much significance into the numbers (such as the extremely low Q values). Hence the values computed above indicate only the plausibility of the hypothesis that the ocean tides are responsible for the variations in the effective Love numbers and phase angles.

TIDAL FRICTION

The evolution of the earth-moon system is dominated by the second degree terms in the total tidal potential. In fact the secular rates of change of n_M , a_M , e_M , J , I_s , $\dot{\theta}$, and E may all be written

$$\dot{X} \approx \sum_{mpq} [\dot{X}]_{2mpq}$$

where X is one of the above-mentioned quantities and the right side of the equation has the form (Appendix 1)

$$[\dot{X}]_{2mpq} = P_{2mpq} s_{2mpq}$$

The values of P_{2mp0} are given in Table 5. Note that the s_{2mpq} are determined directly from the data by the regression analysis, apart from possible corruption by the fourth degree ocean tide terms.

The $[\dot{X}]_{2mpq}$ may be conveniently arranged in a table, with the entries to be filled in as reliable data become available. Our own tentative values are found in Table 3. These were computed from the weighted average over all three satellites of each s_{2mp0} . Table 4 is similar to Table 3, except that the GEOS-II data have been omitted.

Our value of $\dot{n}_M \approx -29 \pm 15$ arc sec/(100 yr)², taken from Table 3, compares favorably with Lambeck's (1975) -34 ± 5 arc sec/(100 yr)², computed from ocean tide models and charts. It also agrees well with the astronomically determined values, which range from -37.5 ± 5 to -52 ± 4 arc sec/(100 yr)² (Lambeck, 1975). The value of $\dot{n}_M \approx -17 \pm 20$ arc sec/(100 yr)² from Table 4 is barely half the current estimates.

Our value of $\dot{E} \approx -3.6 \pm 1.8 \times 10^{19}$ erg/sec from Table 3 is also in good agreement with current estimates. It is bracketed by Miller's (1966) value of -1.7×10^{19} ergs/sec, determined from energy dissipation in shallow seas, and Lambeck's

(1975) value of -5.7×10^{19} ergs/sec, determined from ocean tide charts and models. The number quoted in Table 4 is close to Miller's value, which probably represents a lower limit on the energy dissipation.

On the whole, it would appear that Table 3 agrees better with modern estimates than Table 4. However, Table 3 indicates that the effective phase angle of the S_2 tide is negative, which would speed up the earth's rotation. This is reminiscent of Holmberg's (1952) hypothesis that the atmospheric tidal torque, which tends to speed up the earth, balances the frictional torque, which tends to slow the earth down, thus keeping the earth at a steady rotation rate. The data given in Table 3 of Lambeck (1975) does not indicate a negative effective phase angle for the S_2 tide, however.

Our data on the M_2 tide may be used to estimate the time scale of the tidal evolution of the earth-moon system. Taking (see Appendix 1)

$$\dot{a}_M \approx \dot{a}_{2200} \cong \frac{\sqrt{G(M_E + m_M)}}{3M_E a_M^{11/2}} m_M R_E^5 [F_{220}(l_M)]^2 d_{2200} \sin \delta_{2200}.$$

multiplying each side by $a^{11/2}$ and integrating with respect to time yields

$$a^{13/2} - a_0^{13/2} = 13/6 \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} R_E^5 [F_{220}(l_M)]^2 d_{2200} \sin \delta_{2200} (t - t_0)$$

assuming the inclination, Love number, and phase angle remain constant. At the early time t_0 when the moon was close to the earth $a_0 \approx 0$. Hence the tidal friction age of the earth-moon system is approximately

$$T \approx 6/13 \frac{M_E a_M^{13/2}}{\sqrt{G(M_E + m_M)} m_M [F_{2200}(l_M)]^2 d_{2200} \sin \delta_{2200}}$$

$$\approx \frac{0.0469}{d_{2200} \sin \delta_{2200}} \times 10^9 \text{ yr.}$$

The above equation gives $T = 1.4 \times 10^9$ yr using the weighted average s_{2200} value for all the satellites, and $T = 2.4 \times 10^9$ yr using the BE-C and GEOS-I data only. These times are obviously much shorter than the age of 4.6×10^9 yr for the earth and moon determined by radioactive dating. A way out of this time scale difficulty has been pointed out by Lambeck (1975). He notes that the tidal torques may have been much smaller in the distant past when the oceans did not flood the continental shelves, and that the ocean basin configuration was much different than it is now, due to continental drift.

DISCUSSION

One might wonder whether the variation in the effective Love numbers is in fact due to the ocean tides and not due to frequency-dependence of the solid earth Love number. Alterman, et al. (1959) show that k_2 does vary with frequency. However, the predicted change in Love number over the tidal frequencies is much smaller than that observed here.

Another possibility is core-mantle resonance. The theories of Jeffreys and Vincente (1957) and Molodensky (1961) both predict a variation in Love number

near the diurnal frequency on the same order of magnitude as that observed here. These theories would not explain the observed differences at frequencies away from the diurnal frequency; but core-mantle resonance cannot be ruled out as a possible contributor to the Love number variation.

Our results lend support to the ocean tide hypothesis of Lambeck, et al. (1974), and indicate what can be done when more data become available. They also indicate directions for further study. Regularly spaced and densely packed laser observations, for instance, would give good information on the short-period M_2 tide. Observations of a low-inclination satellite would also increase the amplitude of the M_2 signal, thus determining it more reliably. If the effective Love number of the P_1 tide is really as small as our data suggests, then a mathematical model of the P_1 ocean tide would be of great interest.

NOTATION

$a^*I^*e^*M^*\Omega^*\omega^*$ orbital elements of disturbing body (sun or moon)

$aIeM\Omega\omega$ orbital elements of satellite

C moment of inertia of the earth

C_{nst}^\pm ocean amplitude

$d_{\ell_{mpq}}$ effective tidal Love number

G universal constant of gravitation

k_2 solid earth Love number, degree 2

k'_s load deformation coefficient, degree s

m^* mass of disturbing body (sun or moon)

M_E mass of the earth

$2\pi n f T$ tidal argument

R_E radius of the earth

$\delta_{\ell_{mpq}}$ effective tidal phase angle

$\epsilon_{\ell_{mpq}}$ solid earth tidal phase angle

ϵ_{st}^{\pm} ocean tide phase angle

$\dot{\theta}$

rotational speed of the earth

 $\bar{\rho}_E$

average density of the earth

 ρ_w

density of sea water

 ϕ_2

solid earth tidal lag angle

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APPENDIX 1

We discuss here the rates of change of the lunar orbital elements and the orientation and spin of the earth under the influence of tidal friction, and the dissipation of tidal energy.

We treat the earth-moon-sun system as two separate systems, namely earth-moon and earth-sun. Strictly speaking, this is impermissible, since we are dealing with a three body problem. However, the errors made in doing this are small compared to the uncertainties in determining the effective tidal Love numbers and phase angles.

In the following equations we follow the formalism of Kaula (1964), using the sign convention of Lambeck, et al. (1974) and the corrections for the two body problem of Rubincam (1975, Appendix 1).

The secular rate of change in time of the lunar semimajor axis is given by (Kaula, 1964)

$$\dot{a} = \sum_{\ell,m,p,q} [\dot{a}]_{\ell mpq}$$

where

$$[\dot{a}]_{\ell mpq} = 2\sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+3/2}} \frac{(\ell - m)!}{(\ell + m)!} (2 - \delta_{0m})(\ell - 2p + q)$$

$$\cdot [G_{\ell pq}(e_M) F_{\ell mp}(i_M)]^2 d_{\ell mpq} \sin \delta_{\ell mpq}.$$

The moon's mean motion n_M is related to a_M by

$$n_M = \frac{\sqrt{G(M_E + m_M)}}{a_M^{3/2}}$$

so that

$$\frac{dn_M}{dt} = -3/2 \sqrt{G(M_E + m_M)} a_M^{-5/2} \frac{da_M}{dt}$$

Thus $[n_M]_{\ell_{mpq}} = -3 \frac{G(M_E + m_M)}{a_M^3} \frac{m_M}{M_E} \left(\frac{R_E}{a_M} \right)^{2\ell+1} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$

$$\cdot (\ell - 2p + q) [G_{\ell_{pq}}(e_M) F_{\ell_{mp}}(l_M)]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}.$$

The components of the rate of change of the lunar orbital eccentricity are given by (Kaula, 1964)

$$[\dot{e}_M]_{\ell_{mpq}} = \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+3/2}} \frac{(1-e_M^2)^{1/2}}{e_M} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot [(1-e_M^2)^{1/2} (\ell - 2p + q) - (\ell - 2p)] [G_{\ell_{pq}}(e_M) F_{\ell_{mp}}(l_M)]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}.$$

Let us call the angle between the plane of the lunar orbit and the ecliptic J . Then we have approximately (Rubincam, 1975, Appendix 1)

$$[\dot{J}]_{\ell_{mpq}} = \sqrt{G(M_E + m_M)} \frac{m_M}{M_E} \frac{R_E^{2\ell+1}}{a_M^{2\ell+5/2}} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m}) \cdot \frac{(\ell-2p) \cos I_M - m}{(1 - e_M^2)^{1/2} \sin I_M} [G_{\ell_{pq}}(e_M) F_{\ell_{mp}}(I_M)]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}.$$

We now turn our attention to the earth. Note that both lunar and solar tidal friction disturb the earth. This is in contrast to the treatment above, where only lunar tidal friction disturbs the moon's orbit. The tidal bulge raised by the moon is geared to the lunar motion, but the solar tidal bulge is not.

From considerations of the conservation of angular momentum the rate of change of the earth's equatorial tilt to the ecliptic is given by (Rubincam, 1975, Appendix 1)

$$[\dot{I}_S]_{\ell_{mpq}} = \frac{Gm^{*2}}{R_E C \dot{\theta}} \left(\frac{R_E}{a^*} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m}) \left[\frac{(\ell-2p) - m \cos I^*}{\sin I^*} \right] \cdot [G_{\ell_{pq}}(e^*) F_{\ell_{mp}}(I^*)]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}$$

and the slowdown in the earth's rotation by

$$[\dot{\theta}]_{\ell_{mpq}} = - \frac{Gm^{*2}}{R_E C} \left(\frac{R_E}{a^{*}} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m}) m \\ \cdot [G_{\ell_{pq}}(e^{*}) F_{\ell_{mp}}(I^{*})]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}.$$

Let us now derive the rate of dissipation of tidal energy in the earth.

The orbital energy in the center of mass frame is

$$E_0 = - \frac{GM_E m^{*}}{2a^{*}}$$

and the rotational energy of the earth is

$$E_r = \frac{1}{2} C \dot{\theta}^2$$

Therefore the total mechanical energy is simply

$$E = E_0 + E_r = - \frac{GM_E m^{*}}{2a^{*}} + \frac{1}{2} C \dot{\theta}^2.$$

Thus the rate of dissipation of energy is

$$\dot{E} = \frac{GM_E m^{*}}{2a^{*}} \frac{da^{*}}{dt} + C \dot{\theta} \frac{d\dot{\theta}}{dt}.$$

From the previous equations we derive the relatively compact expression

$$[\dot{E}]_{\ell_{mpq}} = \frac{Gm^{*2}}{R_E} \left(\frac{R_E}{a^*} \right)^{2\ell+2} \frac{(\ell-m)!}{(\ell+m)!} (2 - \delta_{0m})$$

$$\cdot [(\ell - 2p + q)n^* - m\dot{\theta}] [G_{\ell_{pq}}(e^*) F_{\ell_{mp}}(I^*)]^2 d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}$$

It will be noted that the above equations all have the form

$$[\dot{X}]_{\ell_{mpq}} = P_{\ell_{mpq}} s_{\ell_{mpq}}$$

where X is the quantity of interest, $s_{\ell_{mpq}} = d_{\ell_{mpq}} \sin \delta_{\ell_{mpq}}$, and $P_{\ell_{mpq}}$ is a multiplicative factor whose value is easily computed. Table 5 gives the $P_{\ell_{mpq}}$ for $\ell = 2$ (the degree which dominates the evolution of the earth-moon system) and $q = 0$. In the computations for P_{2mp0} the lunar inclination functions $F_{\ell_{mp}}(I_M)$, which change with time due to the motion of the lunar node, are assumed to take on their average values. Also, $G_{2p0}(e^*)$ is taken to be 1.

Table 5 gives us some insight in determining which tides are important in changing what quantities. It is clear that the M_2 tide governs the rates of change of n_M , a_M , $\dot{\theta}$, and E . The O_p , K_1^M , and M_2 tides appear to be about equally important in changing J and I_s . The table gives the appearance of the M_2 tide governing the change in e_M ; but it is probably the N_2 ($\ell_{mpq} = 2201$) and L_2 ($\ell_{mpq} =$

220(-1) tides which dominate the change in the lunar orbital eccentricity. These tides are not given in the table.

APPENDIX 2

We wish to show here how the ocean tides combine with the solid earth tides to give the total tidal potential, as explained by Lambeck, et al. (1974).

The potential of a particular ocean tide constituent n is given by (Lambeck, et al., 1974)

$$U_n = \frac{4\pi G R_E^2}{a} \rho_w \sum_{s,t,u,v} \sum_{\pm} \frac{1+k_s^t}{1+2s} \left(\frac{R_E}{a}\right)^s C_{nst}^{\pm} F_{stu}(l) G_{suv}(e) \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ (s-2u)\omega + (s-2u+v)M + t(\Omega - \theta) \pm 2\pi n f T + e_{st}^{\pm} \right\} \begin{array}{l} s-t \text{ even} \\ s-t \text{ odd} \end{array} .$$

Note that a spherical harmonic in the tide-raising potential excites many spherical harmonics in the ocean tide response; hence the summations in the equation above.

We may simplify the expression above by getting rid of small terms which depend upon the satellite's mean anomaly M and eccentricity e by setting $v = 0$, $G_{su0}(e) \approx 1$, and $s - 2u + v = 0$ (which implies s is even and $u = s/2$). The equation then becomes

$$U_n = \frac{4\pi G R_E^2}{a} \rho_w \sum_{\substack{\text{even } s \\ t}} \sum_{\pm} \frac{1+k_s^t}{1+2s} \left(\frac{R_E}{a}\right)^s C_{nst}^{\pm} F_{st(s/2)}(l) \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ t(\Omega - \theta) \pm 2\pi n f T + e_{st}^{\pm} \right\} \begin{array}{l} s-t \text{ even} \\ s-t \text{ odd} \end{array}$$

Let us now convert the tidal frequency into orbital elements with the correspondence

$$-2\pi n f T \doteq (\ell - 2p) \omega^* + (\ell - 2p + q) M^* + m(\Omega^* - \theta) - m\pi.$$

The correspondence is not exact (Lambeck, et al., 1973) and more detailed considerations must be given if the period of time under consideration is more than a few years. We now have

$$U_{\ell mpq} = \frac{4\pi G R_E^2}{a} \rho_w \sum_{\substack{\text{even } s \\ t}} \sum_{+} \frac{1 + k'_s}{1 + 2s} \left(\frac{R_E}{a}\right)^s C_{(\ell mpq)st}^{\pm} F_{st(s/2)}(I) \\ \cdot \begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ t(\Omega - \theta) \mp [(\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m(\Omega^* - \theta) - m\pi] + \epsilon_{st}^{\pm} \right\} \begin{cases} s - t \text{ even} \\ s - t \text{ odd} \end{cases}$$

where the subscript n has been replaced by (ℓmpq) .

Let us now get rid of terms which depend upon the earth's rotation θ . The only way to do this is to pick the plus (+) in \sum_{+} and set $t = m$. Then

$$\begin{bmatrix} \sin \\ -\cos \end{bmatrix} \left\{ -[(\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^*] - m\Omega + m\pi + \epsilon_{sm}^+ \right\} \begin{cases} s - m \text{ even} \\ s - m \text{ odd} \end{cases} \\ = \begin{bmatrix} -\sin \\ \cos \end{bmatrix} \left\{ (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^* - m\Omega - \epsilon_{sm}^+ \right\} \begin{cases} m \text{ even} \\ m \text{ odd} \end{cases}$$

Also $(4\pi/3) \bar{\rho}_E R_E^3 = M_E$, so that we may write

$$U_{\ell mpq} = \frac{3GM_E}{R_E^2} \left(\frac{\rho_w}{\bar{\rho}_E} \right) \sum_{\substack{s=2,4,\dots \\ m}} \frac{1+k'_s}{1+2s} \left(\frac{R_E}{a} \right)^{s+1} C_{(\ell mpq) sm}^+ F_{sm(s/2)}(I)$$

$$+ \begin{bmatrix} -\sin \\ \cos \end{bmatrix} \left\{ (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^* - m\Omega - \epsilon_{sm}^+ \right\} \begin{array}{l} m \text{ even} \\ m \text{ odd} \end{array}$$

$$= \frac{3GM_E}{R_E^2} \left(\frac{\rho_w}{\bar{\rho}_E} \right) \sum_{\substack{s=2,4,\dots \\ m}} \left(\frac{1+k'_s}{1+2s} \right) \left(\frac{R_E}{a} \right)^{s+1} C_{(\ell mpq) sm}^+ F_{sm(s/2)}(I)$$

$$\begin{bmatrix} C_{(\ell mpq) sm}^+ \sin \epsilon_{sm}^+ \cos \left\{ \right\} \\ C_{(\ell mpq) sm}^+ \cos \epsilon_{sm}^+ \cos \left\{ \right\} \end{bmatrix} - \begin{bmatrix} C_{(\ell mpq) sm}^+ \cos \epsilon_{sm}^+ \sin \left\{ \right\} \\ C_{(\ell mpq) sm}^+ \sin \epsilon_{sm}^+ \sin \left\{ \right\} \end{bmatrix} \begin{array}{l} m \text{ even} \\ m \text{ odd} \end{array}$$

where the empty curly brackets mean

$$\left\{ \right\} = (\ell - 2p)\omega^* + (\ell - 2p + q)M^* + m\Omega^* - m\Omega.$$

Compare this to the solid earth tidal potential, which for $\ell = 2$; $m > 0$; $q = 0$ and small eccentricities is

$$U_{2mp0}^{\text{solid}} = \frac{2Gm^*}{R_E} \frac{(2-m)!}{(2+m)!} F_{2mp}(I^*) \left(\frac{R_E}{a^*} \right)^3 \left(\frac{R_E}{a} \right)^3 F_{2m1}(I)$$

$$+ [k_2 \cos \epsilon_{2mp0} \cos \left\{ \right\} - k_2 \sin \epsilon_{2mp0} \sin \left\{ \right\}]$$

Assuming that the total tidal potential is composed of the solid earth and ocean tides only, one may show from the expressions for the ocean and solid earth tidal potentials that

$$d_{2mp0} \cos \delta_{2mp0} = k_2 \cos \epsilon_{2mp0} + Z_{mp} (1 + k'_2)$$

$$\begin{cases} C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ & m \text{ even} \\ C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ & m \text{ odd} \end{cases}$$

$$\left[+ Z_{mp} \cdot 5/9 (1 + k'_4) \left(\frac{R_E}{a} \right)^2 \frac{F_{4m2}(I)}{F_{2m1}(I)} \begin{cases} C_{(2mp0)4m}^+ \sin \epsilon_{4m}^+ & m \text{ even} \\ C_{(2mp0)4m}^+ \cos \epsilon_{4m}^+ & m \text{ odd} \end{cases} \right]$$

and

$$d_{2mp0} \sin \delta_{2mp0} = k_2 \sin \epsilon_{2mp0} + Z_{mp} (1 + k'_2)$$

$$\begin{cases} C_{(2mp0)2m}^+ \cos \epsilon_{2m}^+ & m \text{ even} \\ -C_{(2mp0)2m}^+ \sin \epsilon_{2m}^+ & m \text{ odd} \end{cases}$$

$$\left[+ Z_{mp} \cdot 5/9 (1 + k'_4) \left(\frac{R_E}{a} \right)^2 \frac{F_{4m2}(I)}{F_{2m1}(I)} \begin{cases} C_{(2mp0)4m}^+ \cos \epsilon_{4m}^+ & m \text{ even} \\ -C_{(2mp0)4m}^+ \sin \epsilon_{4m}^+ & m \text{ odd} \end{cases} \right]$$

where

$$Z_{mp} = 3/10 \frac{(2+m)!}{(2-m)!} \left(\frac{M_E}{m^*} \right) \left(\frac{\rho_w}{\bar{\rho}_E} \right) \left(\frac{a^*}{R_E} \right)^3 \frac{1}{F_{2mp}(I^*) R_E}$$

The term in brackets at the end of each of the above equations for $d_{2mp0} \cos \delta_{2mp0}$ and $d_{2mp0} \sin \delta_{2mp0}$ represents the amount by which the second degree effective

Love numbers and phase angles will be corrupted by the fourth degree ocean tides, if the fourth degree terms are not solved for.

Care must be taken when solving for the effective Love numbers and phase angles of the K_1^M and K_1^S tides. The reason is that the C^+ and ϵ^+ are given for the $K_1 = K_1^M + K_1^S$ tide, and not for the K_1^M and K_1^S tides individually. Some hypothesis is needed to decompose the K_1 into the K_1^M and K_1^S tides. Similar statements hold for the K_2^M and K_2^S tides.

APPENDIX 3

A. PURPOSE

The computer program solves for the effective frequency-dependent tidal Love numbers and phase angles for the whole earth (solid earth + oceans + atmosphere). It does it by performing a multiple regression analysis on the observed tidal perturbation in the inclination of the orbit of an earth satellite. It also solves for ocean tide amplitudes and phases from the Love numbers and lag angles found from the regression analysis, given an assumed tidal response for the solid earth.

All tides are considered to be of second degree only, and only tides which depend on the first power of the orbital eccentricity of the disturbing body are retained; hence the subscripts on the inclination and eccentricity functions run as follows: $\ell = 2$; $m = 1, 2$; $p = 0, 1, 2$; and $q = -1, 0, 1$. Within these limits, any combination of tidal constituents may be chosen to fit the data, giving their effective Love numbers and effective phase angles. Also, the phase angle of any constituent solved for can be set to zero, resulting in a solution for the Love number only for that constituent. There is no restriction on the number of different regression analyses that can be carried out on the data during a run of the program. For example, the sample data cards given in the listing of the main program give two regression analyses.

In practice only the few constituents which give the largest signal in the inclination are fit. If these are not known, then a call to subroutine THEORY gives the theoretical amplitudes and periods of all the constituents in the solid earth signal, given an assumed Love number for the solid earth, such as 0.30. These can be used as a guide for picking out the important constituents. The subroutine also gives a sample plot of inclination vs. time, if this is desired.

The precession of the lunar orbit around the ecliptic requires a certain amount of averaging to be done on the input data for the moon; this is explained in section D. Suffice it to say here that the motion of the lunar node and the moon in its orbit with respect to the earth's equator are average rates over the data span; the inclination of the lunar orbit to the earth's equator is assumed to be constant and equal to its average over the data span. If the data span is longer than four or five years, then a different program taking the precession of the orbit into account more exactly will be needed.

B. THE EXPRESSION FOR THE TIDAL INCLINATION PERTURBATION

The expression for the tidal inclination perturbation is

$$\Delta I = \sum_{m,p,q} \Delta I_{2mpq} + \Delta I_0$$

where

$$\Delta I_{2mpq} = d_{2mpq} \left[2 \frac{(2-m)!}{(2+m)!} \right] m \left[\frac{Gm^*}{\sqrt{GM_E}} \frac{R_E^5}{a^{*3} a^{7/2}} \right] [F_{2mp}(I^*) F_{2ml}(l)] [G_{2pq}(e^*)]$$

$$\cdot \left[\frac{1}{\sin I_0} \right] \cos \frac{\left[(2 - 2p)(\omega^* + M^*) + qM^* + m\Omega^* - m\Omega + \delta_{2mpq} \right]}{\left[(2 - 2p)(\omega^* + M^*) + qM^* + m\Omega^* - m\Omega \right]}$$

The program names of the variables in the above equation and in which subroutine they are computed are given below.

<u>Variable</u>	<u>Program Name</u>	<u>Subroutine</u>
d_{2mpq}	YKM(LM,LP,LQ),YKS(LM,LP,LQ)	REGRES,LOVNUM
δ_{2mpq}	EPSLNM(LM,LP,LQ),EPSLNS(LM,LP,LQ)	REGRES,LOVNUM
$\frac{2}{(2-m)!} \frac{(2-m)!}{(2+m)!}$	B1(LM)	BLM
m	YLM	LOVNUM
$\frac{Gm^*}{\sqrt{GM_E}} \frac{R_E^5}{a^{*3}a^{7/2}}$	CFNTM,CFNTS	COEFF
I^*	XIMOON,XISUN	READMS
$F_{2mp}(I^*)$	A1(LM,LP),B(LM,LP)	INCL
I	XI	RDSAT
$F_{2mp}(I)$	C(LM,LP)	INCL
e^*	EMOON,ESUN	ECCFUN
$G_{2pq}(e^*)$	GLPQM(LP,LQ),GLPQS(LP,LQ)	ECCFUN
$\sin I_0$	SS	MAIN
$\dot{\omega}^* + \dot{M}^*$	XNDM,XNDS	READMS,MAIN
\dot{M}^*	XMDOTM,XMDOTS	READMS,MAIN

Variable	Program Name	Subroutine
$\dot{\Omega}^*$	OMGDOT	READMS
$\dot{\Omega}$	Q	RDSAT
$(2 - 2p) (\dot{\omega}^* + \dot{M}^*)$ + $q\dot{M}^* + m\dot{\Omega}^* - m\dot{\Omega}$	ARGDTM(LM,LP,LQ),ARGDTS(LM,LP,LQ)	ARGDOT
$\omega^* + M^*$	XNDM*(TT-TMS)+DELMN, XNDS*(TT-TMS)+DELSUN	READMS,ARG
M^*	XMDOTM*(TT-TMS)+XMEANM, XMDOTS*(TT-TMS)+XMEANS	READMS,ARG
Ω^*	OMGDOT*(TT-TMS)+OMEGAM, OMEGAS	READMS,ARG
Ω	Q*(TT-TZERO)+XNODE	RDSAT,ARG
$\cos \left\{ \right. \right\}$	ARGUM(LM,LP,LQ).ARGUS(LM,LP,LQ)	ARG
ΔI_0	ANS(1),XJ0	REGRES,LOVNUM

The regression coefficients are found by writing

$$\Delta I_{2mpq} = d_{2mpq} \cos \delta_{2mpq} [\quad] \cos \left\{ (2 - 2p) (\omega^* + M^*) + qM^* + m\Omega^* - m\Omega \right\}$$

$$- d_{2mpq} \sin \delta_{2mpq} [\quad] \sin \left\{ (2 - 2p) (\omega^* + M^*) + qM^* + m\Omega^* - m\Omega \right\}$$

so that the data are of the form

$$y_i = \sum_j a_j x_{ij} + b$$

where the regression coefficients a_j are $d_{2mpq} \cos \delta_{2mpq}$ and $-d_{2mpq} \sin \delta_{2mpq}$, and b is ΔI_0 , d_{2mpq} and δ_{2mpq} can obviously be solved for from the regression coefficients.

C. BRIEF SUMMARY OF OPERATION

The program begins by reading in the satellite data; the sun and moon data; TSTART, TEND and DT; the assumed solid earth Love number and load deformation coefficient; and the solid earth tidal lag angle. Next, parts of the tidal inclination perturbation are computed. Subroutines TIME1 and CORRES are called, which are used in the plotting and printing of the inclination perturbation and residuals against time.

The program then reads in JTHORY and JPLOT; if JTHORY = 0, then the regression analysis is done without calling subroutine THEORY. If JTHORY = 1, then subroutine THEORY is called but no regression analysis is done. JTHORY = 2 does both. If subroutine THEORY is called and a sample plot of the solid earth signal is desired, then JPLOT should be 1. If no plot of the solid earth signal is desired, then set JPLOT = 0.

The regression analysis begins by calling subroutine LASDTA, which reads in the observed inclination. Subroutine REGRES is then called, which reads data cards to determine what constituents are to be solved for. The comments given in REGRES tell how to pick the constituents. Subroutine REGRES computes the regression coefficients and their errors, prints them and calls subroutine LOVNUM.

Subroutine LOVNUM computes the effective frequency-dependent Love numbers and phase angles and their errors from the regression coefficients and their errors. Then it computes the ocean tide amplitudes and phases from these

by subtracting out the solid earth tide. All of these results are then printed and the inclination and residuals vs. time are printed and plotted.

D. SAMPLE INPUT

The sample input is listed in the main program. Each data card (number) and each number on the data card (letter) are discussed below.

1. The satellite name and when the data were taken are given.
2. a. The semimajor axis of the orbit is 8.07291×10^8 cm.
- b. The eccentricity of the orbit is 0.0726.
- c. The rate at which the node progresses along the earth's equator is -2.246536 degrees/day. This figure is obtained by noting that on Feb. 7, 1966 near the beginning of the data span the node position was -109.08202 degrees, and on Oct. 26, 1967 near the end of the data span the node position was -75.41322 degrees. (All times are 0 hours UT.) Hence the rate is

$$\frac{-1440 + 109.08202 - 75.41322}{626} = -2.246536 \text{ degrees/day}$$

where the $-1440 = -4(360)$ indicates four complete revolutions of the node.

- d. The inclination of the orbit is 59.38053 degrees with respect to the earth's equator.

- e. TZERO is Feb. 7, 1966 12 hrs UT, so TZERO = 38.5.
- f. The node position of the satellite at time TZERO was -109.08202 degrees.

The American Ephemeris and Nautical Almanac (Nautical Almanac for short) and Figure 7 are used for obtaining the numbers on the next two data cards.

3. a. The positions of the moon and sun are given for Feb. 4, 1966 in the Nautical Almanac, near the beginning of the data span; hence TMS is taken as TMS = 35.0. On this day the position of the lunar node on the ecliptic was $\Omega = 60.8500$ degrees, according to the Almanac. The position of the lunar node on the earth's equator is found from the formula

$$\tan \Omega^* = \frac{\sin J \sin \Omega}{\sin I \cos J + \cos I \sin J \cos \Omega}$$

where $J = 5.1453964$ degrees = inclination of the lunar orbit to the ecliptic, and $I = 23.44319$ degrees = inclination of the ecliptic to the earth's equator. Solving the equation gives $\Omega^* = 10.1770$ degrees.

b. DELTA1 is $\omega^* + M^*$ (measured from the earth's equator); so

$$\text{DELTA1} = \omega^* + M^* = ((- \Omega + c$$

where $(($ and Ω are given by the Almanac and c is the arc shown in Figure 7. c can be found from the formula

$$\cos c = \frac{\cos I - \cos I^* \cos J}{\sin I^* \sin J}$$

where I^* , the inclination of the lunar orbit to the earth's equator is given by

$$\cos I^* = \cos I \cos J - \sin I \sin J \cos \Omega$$

We find that on Feb. 4, 1966 $I^* = 26.3140$ degrees, $c = 51.6092$ degrees, $(\Omega = 115.2340$ degrees, and $\Omega = 60.8500$ degrees. Hence $\Delta\Omega = 105.9932$ degrees.

- c. The nodal position of the sun is always 0.0 degrees.
- d. $\Delta\Omega = \omega^* + M^*$ for the sun is 313.7163 degrees, according to the Almanac.
- e. The speed at which the moon moves around in its orbit averaged over the data span is $XNDM1 = \omega^* + M^* = 13.183848$ degrees/day. This is found by computing the lunar position on Oct. 27, 1967 at the end of the data span. We find that $\Omega^* = 5.0417$ degrees, $I^* = 28.1025$ degrees, $c = 22.9427$ degrees, and $\omega^* + M^* = 131.8174$ degrees. Subtracting this last figure from $\omega^* + M^*$ for Feb. 4, 1966 and making allowance for 23 revolutions of the moon gives

$$XNDM1 = \frac{23(360) + 131.8174 - 105.9932}{630} = 13.183848 \text{ degrees/day.}$$

- f. The average speed of the moon's node on the equator is

$$OMGDT1 = \frac{5.0417 - 10.1770}{630} = -0.00815 \text{ degrees/day.}$$

4. a. The inclination of the moon's orbit to the earth's equator averaged over the data span is

$$XID1 = \frac{26.3140 + 28.1025}{2} = 27.2082 \text{ degrees}$$

b. The inclination of the solar orbit to the earth's equator is 23.44319 degrees.

c. TMS is 35.0 days (Feb. 4, 1966).

d. The position of the lunar mean anomaly on Feb. 4, 1966 is $(\text{L} - \Gamma) = 331.5588$ degrees, according to the Almanac.

e. The solar mean anomaly on Feb. 4, 1966 is 31.3590 degrees, according to the Almanac.

5. a. TSTART is 37.0 days (Feb. 6, 1966).

b. TEND is 666.0 days (Oct. 28, 1967).

c. DT is 2.0 days.

6. a. The solid earth Love number is taken to be 0.30.

b. The load deformation coefficient of the solid earth is taken to be -0.30.

7. The solid earth tidal lag angle is taken to be 0.0.

8. a. Both the theoretical amplitudes and regression analysis are wanted, so $JTHORY = 2$.

b. A plot of the theoretical tidal signal is wanted, so $JPLOT = 1$.

9. a. There are 142 data points.

b. TDAY is 38.5, since this is the date of the first data point and the time on the following cards is measured from the first data point.

10. a. The tidal inclination perturbation of the first data point is -1.1594475 arc seconds.

b. The time of the first data point is 0.0 days.

11. a. The tidal inclination perturbation of the second data point is -0.89708115 arc seconds.

b. The time of the second data point is 13.0 days after the first.

12-151. The rest of the data cards.

152.a. The name of the satellite is GEOS I.

b. There are 142 data points.

c. There are 68 independent variables + 1 dependent variable = 69 variables.

d. Two subset selection cards follow.

153.a. Eight variables are chosen for this regression analysis.

b-i. Fit the K_1 tide (9 and 10), the K_2 tide (27 and 28), the P_1 tide (39 and 40), and the S_2 tide (55 and 56) for effective Love numbers and phase angles.

154.a. Seven variables are chosen for this regression analysis.

b-c. Fit the K_1 and S_2' tides for effective Love numbers and phase angles (9 and 10, 55 and 56).

d-g. Fit the M_2 , K_2 , and P_1 tides for effective Love numbers but no phase angles (which are forced to be zero).

COMPUTER PROGRAM LISTING

MAIN PROGRAM

THIS PROGRAM SOLVES FOR THE EFFECTIVE FREQUENCY-DEPENDENT TIDAL LOVE NUMBERS AND LAG ANGLES FOR THE WHOLE EARTH BY CARRYING OUT A MULTIPLE REGRESSION ANALYSIS ON THE TIDAL PERTURBATION IN THE INCLINATION OF THE ORBIT OF AN EARTH SATELLITE. IT ALSO SOLVES FOR OCEAN TIDE AMPLITUDES AND PHASES FROM THE LOVE NUMBERS AND LAG ANGLES FOUND, GIVEN THE TIDAL RESPONSE OF THE SOLID EARTH.

ONLY 2ND DEGREE TIDES ARE CONSIDERED, AS WELL AS ONLY TERMS WHICH DEPEND ON THE FIRST POWER OF ORBITAL ECCENTRICITY. HENCE THE SUBSCRIPTS ON THE INCLINATION AND ECCENTRICITY FUNCTIONS RUN AS FOLLOWS: $L=2$, $M=1,2$, $P=0,1,2$, AND $Q=-1,0,1$. (SINCE THE COMPUTER CANNOT HANDLE ZERO SUBSCRIPTS, IN THIS PROGRAM THEY RUN AS FOLLOWS: $LM=M$, $LP=P+1$, AND $QC=Q+2$.) WITHIN THESE LIMITS, ANY COMBINATION OF TIDAL CONSTITUENTS MAY BE CHECKED FOR FITTING TO THE DATA. IN PRACTICE, ONLY THE FEW CONSTITUENTS WHICH GIVE THE LARGEST SIGNAL IN THE INCLINATION ARE FIT. (THE IMPORTANT SIGNALS MAY BE FOUND BY CALLING SUBROUTINE THEORY.)

IMPORTANT NOTE IN THIS PROGRAM TIDAL INCLINATION PERTURBATION IS
ABBRIVIATED TIP.

BRIEF DESCRIPTION OF EACH SUBROUTINE

ARG - COMPUTES THE COSINE TERM IN THE EXPRESSION FOR THE TIP
 ARGDOT - COMPUTES THE DERIVATIVE OF THE ARGUMENT OF THE COSINE TERM IN
 THE TIP
 ARGSLST - COMPUTES SINES AND COSINES TO BE USED IN SUBROUTINE DATA
 BLM - COMPUTES THE FACTORIAL TERM IN THE TIP
 COEFF - COMPUTES THE COEFFICIENT IN THE TIP OF THE FCRM
 CONSTANT/(A+7/2)
 CUPRES - USED ONLY BY SUBROUTINE PLOTIP TO DETERMINE WHETHER AN
 EXPERIMENTAL DATA POINT SHOULD BE PLOTTED AT A PARTICULAR TIME
 DATA - COMPUTES VALUES TO BE USED IN REGRESSION ANALYSIS
 ECPFUN - COMPUTES ECCENTRICITY FUNCTIONS
 INCL - COMPUTES INCLINATION FUNCTIONS
 LAGI - READS IN SOLID EARTH LAG ANGLE
 LAGE - SETS THE FREQUENCY DEPENDENT LAG ANGLES INITIALLY EQUAL TO ZERO
 LASOTA - READS IN THE OBSERVED TIP
 LOVE - READS IN THE SOLID EARTH LOVE NUMBER AND LOAD DEFORMATION
 COEFFICIENT
 LOVNUM - TAKES THE OUTPUT OF REGRES AND COMPUTES FREQUENCY-DEPENDENT LOVE
 NUMBER 3, LAG ANGLES, AND OCEAN TIDE PARAMETERS
 PLUTER - PLITS OUT THE TIP, EXPERIMENTAL DATA POINTS, AND THE RESIDUALS
 ON THE COMPUTER PAPER
 RUSAT - READS IN SATELLITE ELEMENTS
 READMO - READS IN SUN AND MOON POSITIONS, RATES
 REGRES - PERFORMS REGRESSION ANALYSIS
 THEORY - COMPUTES AMPLITUDE, PERIODS OF THE SOLID EARTH TIDAL SIGNAL
 TIME1 - COMPUTES TIME VALUES FOR ARRAY T(1)

NOTATION

SATELLITE

A	- SEMIMAJOR AXIS IN 10*18 CM
C(LM,LP)	- INCLINATION FUNCTIONS
E	- ORBITAL ECCENTRICITY
O	- RATE OF CHANGE OF NODE POSITION
SAT(J)	- ALPHANUMERIC INFORMATION, SUCH AS NAME OF SATELLITE
SS	- SINE OF SATELLITE INCLINATION
TZERO	- TIME (MEASURED FROM BEGINNING OF THE YEAR) WHEN THE NODE HAD VALUE XNODE
XI	- SATELLITE INCLINATION
XNODE	- POSITION OF NODE AT TIME TZERO

MUON AND SUN

ORIGINAL PAGE IS
OF POOR QUALITY

```

C   ARGUM(LM,LP,LQ) - COSINE TERM IN THE TIP
C   ARGUS(LM,LP,LQ)
C
C   ARGUTM(LM,LP,LQ) - RATE OF CHANGE OF ARGUMENT OF COSINE IN THE TIP
C   ARGUTS(LM,LP,LQ)
C
C   A1(LM,LP)      - INCLINATION FUNCTIONS OF MOON
C   B1(LM,LP)
C
C   CFNTM          - TERM IN TIP OF FORM CONSTANT/(#**7/2)
C   CFNTS
C
C   DELMN          - (ARGUMENT OF PERIGEE + MEAN ANOMALY) OF MOON AT TIME
C   TMS, MEASURED WITH RESPECT TO EARTH'S EQUATOR
C
C   DELSUN          - ECCENTRICITY OF LUNAR ORBIT
C
C   EMOON          - ECCENTRICITY OF LUNAR ORBIT
C   ESUN
C
C   EPSLNM(LM,LP,LQ) - EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE FOR LUNAR TIDES
C   EPSLNS(LM,LP,LQ)
C
C   GLPOM(LP,LQ)   - ECCENTRICITY FUNCTION FOR MOON
C   GLPOS(LP,LQ)
C
C   OMEGAM          - POSITION OF LUNAR NODE ON EARTH'S EQUATOR
C   OMEGAS
C
C   XIMMOON        - INCLINATION OF LUNAR ORBIT TO EARTH'S EQUATOR
C   XISUN
C
C   XMDOOTM         - RATE OF CHANGE OF LUNAR MEAN ANOMALY
C   XMDOOTS
C
C   XMOON(LM,LP,LQ) - LUNAR PART OF TIP
C   XSUN(LM,LP,LQ)
C
C   XNDM          - RATE OF CHANGE OF (ARGUMENT OF PERIGEE + MEAN ANOMALY)
C   OF MOON, WITH RESPECT TO THE EARTH'S EQUATOR
C
C   XNDS
C
C   YKM(LM,LP,LQ)   - EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER FOR LUNAR
C   TIDES
C   YKS(LM,LP,LQ)
C
C   TMS           - TIME OF MOON AND SUN POSITIONS
C
C   DATA
C
C   MEXP          - NUMBER OF DATA POINTS
C   TODAY          - CORRECTION TO TEXP(J) TO GIVE IT IN DAYS FROM THE
C   BEGINNING OF THE YEAR
C   TEXP(J)        - TIME OF OBSERVATION XIEXP(J)
C   XIEXP(J)       - OBSERVED TIP AT TIME TEXP(J)
C
C   MISCELLANEOUS
C
C   DT             - INTERVAL BETWEEN SUCCESSIVE VALUES OF T(L)
C   MT             - TOTAL NUMBER OF VALUES IN ARRAY T(L)
C   T(L)           - TIME VALUES BETWEEN AND INCLUDING TSTART AND TEND
C   TEND           - ENDING TIME OF DATA SPAN
C   TSTART          - STARTING TIME OF DATA SPAN
C   F               - CONVERSION FACTOR FROM DEGREES TO RADIANS
C   B1(LM)         - FACTORIAL PART OF THE TIP
C   XK             - SOLID EARTH LOVE NUMBER (SECOND DEGREE)
C   XKP            - LOAD DEFORMATION COEFFICIENT (SECOND DEGREE)
C   X10            - ADDITIVE CONSTANT IN TIP
C   XLAG           - LAG ANGLE OF SOLID EARTH TIDE
C   XINC(L)        - THE COMPUTED TIP AT TIME T(L)
C   INDEX          - INDEX WHICH KEEPS TRACK OF TIME IN SUBROUTINE DATA
C   NTFACK(L)      - DETERMINES WHETHER A DATA POINT SHOULD BE PLOTTED AT
C   TIME T(L)
C   TIDE(LM,LP,LQ) - CONTAINS ALPHANUMERIC NAMES OF TIDES (K1,M2, ETC.)
C   FACTOR         - USED IN SUBROUTINE LOVMUN AS A CORRECTION TO THE
C   LUNAR TIDES TO GET THE PREDICTED AMPLITUDE OF THE
C   LUNISOLAR TIDES
C
C
C

```

```

C SAMPLE INPUT (COLUMN 1 OF THE INPUT STARTS IN COLUMN 3 HERE)
C
C (SAT(J), J=1,14) (FORMAT 13AE,A2)
C GEOS - 1 , 1966-1967 DATA
C
C A E Q1 X11 TZERO XNODE1 (FORMAT 8F10.5)
C 4.07291 0.0726 -2.246535 59.38053 38.5 -109.0820
C CMEGA1 DELTA1 OMEGA2 DELTA2 XNDM1 CMGCT1 (FORMAT 8F10.5)
C 10.1770 105.9932 0.0 313.7163 13.19385 -0.00815
C XID1 XIC2 TMS XMEAN1 XMEAN2 (FORMAT 8F10.5)
C 27.2082 23.44316 35.0 331.5588 31.3590
C
C TSTART TEND DT (FORMAT 8F10.5)
C 37.0 666.0 2.0
C XK XKP (FORMAT 8F10.5)
C 0.30 -0.30
C XLAG (FORMAT 8F10.5)
C 0.0
C JTHORY JPLOT (FORMAT 2I5)
C 2 1
C MEXP TODAY (FORMAT 15,F10.5)
C 1+2 38.5
C
C XIEP(J) TEXP(J) (FORMAT 2D14.8)
C -1159447ED 010.0
C -89708115D 000.13 D 02
C ETC.
C
C PR,PRI N M NS (FORMAT 36I2)
C GEOS 1 14267 2
C K (ISAVE(J), J=1,K)
C 8 910272839405556
C 7 9102127395556
C
C
C ISN 0002 IMPLICIT REAL*8 (A-H,O-Z)
C ISN 0003 DIMENSION EPSLNMT(2,3,3),EPSLNS(2,1,3),ARGUM(2,3,3),ARGUE(2,3,3),
C 1 ARGCTM(2,3,3),ARGOTS(2,3,3)
C ISN 0004 DIMENSION E1(2),XMC0N(2,3,3),XESN(2,3,3),YKM(2,3,3),YKS(2,3,3)
C ISN 0005 DIMENSION TEXP(200),XIEP(200),T(700),XINCL(700),NTRACK(700)
C ISN 0006 DIMENSION C(2,3),A(2,3,3),B(2,3),GLPQM(3,3),GLPQS(3,3)
C ISN 0007 COMMON/BLK1/EP3LN,EP3LNS,ARGUM,ARGUE,ARGDTM,ARGOTS
C ISN 0008 COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XH0DN,XGJN,YKM,YKS,XKP
C ISN 0009 COMMON/BLKD/XLAGD,CMEGAM,DELMN,CMEGAS,DELSN,SS,XID,A,E,X1,XNDE,
C ISN 0010 1 TZERU,XIMDN,XISUN,TMS,XNDM,XNDSt,XMEANM,XMEANS,XNDTM,XMDOTs,
C 2 CMGDOT,MEXP
C COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
C ISN 0011 F=3.141592654D/180.0D0
C ISN 0012 XNDE=(0.945647D0)=F
C ISN 0013 XMUDOTs=(1.1064952D0)=F
C ISN 0014 XMUDOTs=(0.5856D0)=F
C ISN 0015
C READ IN THE DATA, COMPUTE PARTS OF THE TIP
C ISN 0016 CALL FDSAT
C ISN 0017 CALL READMS
C ISN 0018 READ (5,1) TSTART,TEND,DT
C ISN 0019 1 FORMAT (8F10.5)
C ISN 0020 WRITE (6,7) TSTART,TEND,DT
C ISN 0021 7 FORMAT (////////////,2X,*TSTART=*,F10.4,5X,*TEND=*,F10.4,5X,*DT=*,F10.4,5X,*"DAYS")
C ISN 0022 CALL LD0E
C ISN 0023 CALL LAG1
C ISN 0024 CALL LAG2
C ISN 0025 SS=DSIN(X1)
C ISN 0026 CALL FCCFUN
C ISN 0027 CALL INCL(X1,C)
C ISN 0028 CALL INCL(XIMDN,A1)
C ISN 0029 CALL INCL(XISUN,B)
C ISN 0030 CALL BLM
C ISN 0031 CALL ARGDOT
C ISN 0032 CALL COEFF

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ISN 0033      CALL TIME1(TSTART,TEND,DT,MT)
ISN 0034      INDEX=0
ISN 0035      MEXP=0
ISN 0036      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0037      READ (5,2) JTHORY,JPLOT
ISN 0038      2  FORMAT (2I6)
ISN 0039      C IF JTHORY=2, CALL THEORY, READ IN DATA POINTS, DO REGRESSION ANALYSIS
ISN 0040      C IF JTHORY=1, CALL THEORY ONLY
ISN 0041      C IF JTHORY=0, READ IN DATA AND DO REGRESSION ANALYSIS WITHOUT CALLING THEORY
ISN 0042      C IF JPLOT=1, THEN A SAMPLE CURVE OF THE TIP WITH SOLID EARTH LOVE NUMBER=XX AND
ISN 0043      C ZERO LAG ANGLE IS PLOTTED BY THEORY
ISN 0044      IF (JTHORY .EQ. 2) GO TO 6
ISN 0045      IF (JTHORY .EQ. 1) GO TO 3
ISN 0046      GO TO 4
ISN 0047      0  CALL THEORY(JPLOT,MT)
ISN 0048      CALL LASOTA
ISN 0049      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0050      CALL REGRES(MT)
ISN 0051      GO TO 5
ISN 0052      3  CALL THEORY(JPLOT,MT)
ISN 0053      GO TO 5
ISN 0054      4  CONTINUE
ISN 0055      CALL LASOTA
ISN 0056      CALL CORRES(TSTART,TEND,DT,MEXP)
ISN 0057      CALL REGRES(MT)
ISN 0058      0  CONTINUE
ISN 0059      STOP
ISN 0060      END

```

```

ISN 0002      SUBROUTINE ARG(TT)
C
C      THIS SUBROUTINE COMPUTES THE COSINE OF THE ARGUMENT OF THE TIP (I.E. IT
C      COMPUTES THE COSINE OF (L - 2*P)*(ARGUMENT OF PERIGEE+MEAN ANOMALY) + C* (MEAN
C      ANOMALY) + M*(NODE OF DISTURBING BODY) - M*(NODE OF SATELLITE) + TIDAL LAG
C      ANGLE).
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
ISN 0005      1 ARGDTM(2,3,3),ARGDTS(2,3,3)
ISN 0006      COMMON/BLKA/ELSLNM,EPSLNS,ARGUM,ARGUS,ARGDTM,ARGCTS
ISN 0007      COMMON/BLKD/XLAG,Q,OMEGAM,DELMN,EMEGAS,DELSUN,SS,XI0,A,E,XI,XNODE,
ISN 0008      1 TZERO,XIMONN,XISUN,TMS,XNDM,XNDS,F,X4EANM,XMEANS,XNDCTM,XMDCTS,
ISN 0009      2 OMGDOT,MEXP
ISN 0010      DO 10 LM=1,2
ISN 0011      YL=LM
ISN 0012      DO 10 LP=1,3
ISN 0013      YLP=LP-1
ISN 0014      DO 10 LQ=1,3
ISN 0015      YLQ=LQ-2
ISN 0016      A2=(2.0D0 - 2.0D0*YLP)*(XNDM*(TT-TMS)+DELMN) + YLQ*(XMDCTS*(TT-
ISN 0017      1 TMS)+XMEANS)+YLW*(OMGDOT*(TT-TMS)+OMEGAM) - YLM*(Q*(TT-TZERO)-
ISN 0018      2 XNODE) + EPSLNM(LM,LP,LQ)=DCOS(A2)
ISN 0019      A3=(2.0D0 - 2.0D0*YLP)*(XNDS*(TT-TMS)+DELFUN) + YLQ*(XMDCTS*(TT-
ISN 0020      1 TMS)+XMEANS)+YLM*OMEGAS - YLM*(Q*(TT-TZERO) + XNODE) +
ISN 0021      2 EPSLNS(LM,LP,LQ)
ISN 0022      ARGUS(LM,LP,LQ)=DCOS(A3)
ISN 0023      10 CONTINUE
ISN 0024      RETURN
ISN 0025      END

```

```

ISN 0002      SUBROUTINE ARGDT
C
C      THIS SUBROUTINE COMPUTES THE ANGULAR SPEED OF EACH CONSTITUENT (I.E. IS
C      THE TIME DERIVATIVE OF THE ARGUMENT COMPUTED IN SUBROUTINE ARG).
C
ISN 0003      IMPLICIT REAL*8(A-H,C-Z)
ISN 0004      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
ISN 0005      1 ARGDTM(2,3,3),ARGDTS(2,3,3)
ISN 0006      COMMON/BLKA/ELSLNM,EPSLNS,ARGUM,ARGUS,ARGDTM,ARGCTS
ISN 0007      COMMON/BLKD/XLAG,Q,OMEGAM,DELMN,EMEGAS,DELSUN,SS,XI0,A,E,XI,XNODE,
ISN 0008      1 TZERO,XIMONN,XISUN,TMS,XNDM,XNDS,F,XMEANS,XMEANS,XNDCTM,XMDCTS,
ISN 0009      2 OMGDOT,MEXP
ISN 0010      DO 10 LM=1,2
ISN 0011      YL=LM
ISN 0012      DO 10 LP=1,3
ISN 0013      YLP=LP-1
ISN 0014      DO 10 LQ=1,3
ISN 0015      YLQ=LQ-2
ISN 0016      1 ARGDTM(LM,LP,LQ)=(2.0D0 - 2.0D0*YLP)*XNDM + YLQ*XMDCTS - YLM*Q
ISN 0017      10 ARGDTS(LM,LP,LQ)=(2.0D0 - 2.0D0*YLP)*XNDS + YLQ*XMDCTS - YLM*Q
ISN 0018      CONTINUE
ISN 0019      RETURN
ISN 0020      END

```

```

ISN 0002          SUBROUTINE ARGSLST(TT)
C
C   THIS SUBROUTINE FINDS THE SINE AND COSINE OF (L - 2*P)*(ARGUMENT OF
C   PERIGEE+MEAN ANOMALY) + Q*(MEAN ANOMALY) + M*(NODE OF DISTURBING BODY) -
C   M*(NODE OF SATELLITE) FOR USE IN SUBROUTINE DATA.
C
C
ISN 0003          IMPLICIT REAL*16(A-H,C-Z)
ISN 0004          DIMENSION CSM(2,3,3),SNS(2,3,3),CSS(2,3,3)
ISN 0005          COMMON/BULK/ XLAG,Q,OMEGAM,DELMN,CMEGAS,DELCSUN,SS,XIO,A,E,XI,XNDE,
ISN 0006          1,TZERO,XIMOGN,XISUN,TM3,XNDS,XNDS,F,XMEANM,XMEANS,XMDCTM,XMDCTS,
ISN 0007          2,XMDCTI,XEXP
ISN 0008          COMMON/BULKF/CEM,FNM,CS,SS,SNS
ISN 0009          DO 10 LM=1,2
ISN 0010          VL=4*LM
ISN 0011          DO 10 LP=1,3
ISN 0012          VLP=LP-1
ISN 0013          DO 10 LD=1,3
ISN 0014          VLD=LD-2
ISN 0015          A2=(2.000 - 2.000*VLP)*(XNDM(TT-TM5)+DELMN) + VLQ*(XMDCTM*(TT-
ISN 0016          1,TM5)+XMEANM)+VLM*(CMGDT*(TT-TM5)+OMEGAM) - VLM*(0-(TT-TZERO)*
ISN 0017          2,XNDE)
ISN 0018          CSM(LM,LP,LD)=DCOS(A2)
ISN 0019          SNS(LM,LP,LD)=DSIN(A2)
ISN 0020          A3=(2.000 - 2.000*VLP)*(XNDS*(TT-TM5)+DELCSUN) + VLQ*(XMDCTS*(TT-
ISN 0021          1,TM5)+XMEANS)+VLM*(CMEGAS - VLM*(Q*(TT-TZERO) + XNDE))
ISN 0022          CSS(LM,LP,LD)=DCOS(A3)
ISN 0023          SNS(LM,LP,LD)=DSIN(A3)
ISN 0024          10 CONTINUE
ISN 0025          RETURN
ISN 0026          END

```

ISN 0002 SUBROUTINE BLM
C THIS SUBROUTINE COMPUTES THE FACTORIAL PART OF THE TIP.
C
C IMPLICIT REAL*8 (A-H,O-Z)
C DIMENSION E1(2),XMON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
C COMMON/BLKB/ B1,XX,CFTM,CFTS,SUM,XMON,XSUN,YKM,YKS,XXP
C B1(1)=1.0D/3.0D0
C B1(2)=1.0D/12.0D0
C D1(2)=1.0D/12.0D0
C RETURN
C END

```

1FN 0002          SUBROUTINE CFFFF
C
C THIS SUBROUTINE COMPUTES THE PART OF THE TIP WHICH HAS THE FORM
C C1NISTANT/(A**7/2).
C
C
1SN 0003          IMPLICIT REAL*8 (A,B,C,D)
1SN 0004          DIMENSION B1(2),XMD0N(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
1SN 0005          COMMON/WLKB/B1,XK,CFNTM,CFNTS,SUM,XMD0N,XSUN,YKM,YKS,XKP
1SN 0006          COMMON/BLKD/XLAG,Q,CEGAM,DELMN,CEGAM,DELSUN,SS,X1D,A,E,XI,XNCD,
1TZERO,XIMCON,XISUN,TMS,XNDM,XND5,F,XMEANM,XMEANS,XMDCTM,XMDCTS,
2OMGDT,MEXP
1SN 0007          A2=DSQHT(A)
1SN 0008          CFNTM=813.223200/((A**3)*A2)
1SN 0009          CFNTS=372.971500/((A**3)*A2)
1SN 0010          RETURN
1SN 0011          END

```

```

1SN 0002      SUBROUTINE CORRES(TSTART,TEND,DT,MEXP)
C
C      THIS SUBROUTINE IS USED ONLY BY SUBROUTINE PLOTER. IT PUTS IN THE VALUES
C      OF ARRAY NTRACK( ), WHICH DETERMINES WHETHER OR NOT AN EXPERIMENTAL DATA POINT
C      SHOULD BE PRINTED AT TIME T(I). (NTRACK(N)=THE NUMBER OF THE EXPERIMENTAL
C      DATA POINT IF YES, ZERO IF NO.)
C
C
1SN 0003      IMPLICIT REAL*8(A-H,C-Z)
1SN 0004      DIMENSION TEXP(200),XIEXP(200),T(700),XTINCL(700),NTRACK(700)
1SN 0005      COMMON/BLKC/TEXP,XIEXP,T,XTINCL,NTRACK
1SN 0006      MT=(TEND-TSTART)/DT + 1.1DD0
1SN 0007      DO 10 I=1,MT
1SN 0008      10  NTRACK(I)=0
1SN 0009      IF (MEXP .EQ. 0) GO TO 12
1SN 0010      DO 11 I=1,MEXP
1SN 0011      N=(TEXP(I)-TSTART)/DT + 1.5DD0
1SN 0012      IF (N .LT. 1) N=1
1SN 0013      IF (N .GT. MT) N=MT
1SN 0014      IF (N .GT. MT) N=MT
1SN 0015      NTRACK(N)=1
1SN 0016      11  CONTINUE
1SN 0017      12  CONTINUE
1SN 0018      RETURN
1SN 0019      END

```

```

TSN 0002      SUBROUTINE DATA(MM,D)
C
C      THIS SUBROUTINE IS USED TO FEED IN DATA FOR USE IN THE MULTIPLE
C      REGRESSION ANALYSIS CARRIED OUT BY SUBROUTINE REGRES.
C
C
ISN 0003      IMPLICIT REAL*8(A-H,O-Z)
ISN 0004      REAL*8 H(MM)
ISN 0005      DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
ISN 0006      1,ARGDTM(2,3,3),ARGOTS(2,3,3)
ISN 0007      DIMENSION E(2,2),XMCN(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
ISN 0008      DIMENSION C(2,3),A1(2,2),E(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0009      DIMENSION CS(2,3,3),SNM(2,3,3),CSS(2,3,3),SNS(2,3,3)
ISN 0010      COMMON/BLKA/EPNLNM,EPNLNS,ARGUM,ARGUS,ARGDTM,ARGOTS
ISN 0011      COMMON/BLKB/B1,X,CENTM,CENTS,SUM,XMOON,XSUN,YKM,YKS,XKP
ISN 0012      COMMON/BLKD/XLAG,Q,CMEGAM,DELMN,CMEGAS,DELSUN,SE,XIO,A,E,XI,XNCD,E,
ISN 0013      COMMON/BLKD/XLAG,Q,CMEGAM,DELMN,CMEGAS,DELSUN,SE,XIO,A,E,XI,XNCD,E,
ISN 0014      1,TZERD,XIMON,XIEUN,TMS,XNDM,XNDC,F,XMEANM,XMEANS,XNDCTM,XNDCTS,
ISN 0015      2,CMGDOT,MEXP
ISN 0016      COMMON/BLKF/CEM,SNM,CSS,SNS
ISN 0017      COMMON/BLKG/C,A1,R,GLPQM,GLPQS,INDEX
ISN 0018      C INDEX IS USED TO KEEP TRACK OF TIME
ISN 0019      INDEX=INDEX + 1
ISN 0020      TT=TEXP(INDEX)
ISN 0021      CALL ARGLS(TT)
ISN 0022      C DO THE LUNAR TIDES. WE LUMP THE LUNISOLAR TIDES WITH THE LUNAR TIDES.
ISN 0023      I=0
ISN 0024      DO 70 LM=1,2
ISN 0025      YLM=LM
ISN 0026      DO 70 LP=1,3
ISN 0027      DO 70 LQ=1,3
ISN 0028      I=I + 1
ISN 0029      D(I)=CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPQM(LP,LQ)*YLM*CSN(LM,LP,LQ)
ISN 0030      1/(ARGDTM(LM,LP,LQ)*ES)
ISN 0031      70  CONTINUE
ISN 0032      C DO THE SOLAR TIDES
ISN 0033      DO 71 LM=1,2
ISN 0034      YLM=LM
ISN 0035      DO 71 LP=1,3
ISN 0036      DO 71 LQ=1,3
ISN 0037      IF (LP .EQ. 2 .AND. LQ .EQ. 2) GO TO 71
ISN 0038      I=I + 1
ISN 0039      D(I)=CFNTS*B1(LM)*C(LM,2)*B(LM,LP)*GLPQS(LP,LQ)*YLM*CSN(LM,LP,LQ)
ISN 0040      1/(ARGDTS(LM,LP,LQ)*ES)
ISN 0041      71  CONTINUE
ISN 0042      C PUT IN OBSERVED INCLINATION
ISN 0043      I=I + 1
ISN 0044      D(I)=XIEXP(INDEX)
ISN 0045      RETURN
ISN 0046      END

ISN 0002      SUBROUTINE ECCFUN
C
C      THIS SUBROUTINE COMPUTES THE ECCENTRICITY FUNCTIONS FOR THE MOON AND SUN.
C
C
ISN 0003      IMPLICIT REAL*8(A-H,O-Z)
ISN 0004      DIMENSION C(2,3),A1(2,2),E(2,3),GLPQM(3,3),GLPQS(3,3)
ISN 0005      COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
ISN 0006      EMON=0.054900
ISN 0007      GLPQM(1,1)=(-C*5D0)*EMON
ISN 0008      GLPQM(1,2)=1.0D0
ISN 0009      GLPQM(1,3)=(-3.5D0)*EMON
ISN 0010      GLPQM(2,1)=(3.5D0)*EMON
ISN 0011      GLPQM(2,2)=1.0D0
ISN 0012      GLPQM(2,3)=(-1.5D0)*EMON
ISN 0013      GLPQM(3,1)=(-3.5D0)*EMON
ISN 0014      GLPQM(3,2)=1.0D0
ISN 0015      GLPQM(3,3)=(-2.5D0)*EMON
ISN 0016      ESUN=(-C*167D0)
ISN 0017      GLPQS(1,1)=(-0.5D0)*ESUN
ISN 0018      GLPQS(1,2)=1.0D0
ISN 0019      GLPQS(1,3)=(-3.5D0)*ESUN
ISN 0020      GLPQS(2,1)=(1.5D0)*ESUN
ISN 0021      GLPQS(2,2)=1.0D0
ISN 0022      GLPQS(2,3)=(-1.5D0)*ESUN
ISN 0023      GLPQS(3,1)=(-3.5D0)*ESUN
ISN 0024      GLPQS(3,2)=1.0D0
ISN 0025      GLPQS(3,3)=(-0.5D0)*ESUN
ISN 0026      RETURN
ISN 0027      END

```

1SN 0002 SUBROUTINE INCL(XI,F)
C C THIS SUBROUTINE COMPUTES THE SECOND DEGREE INCLINATION FUNCTIONS.

```

      IMPLICIT REAL*8(A-H,C-Z)
      DIMENSION F(2,3)
      S=D*SIN(X1)
      C=DC*COS(X1)
      S2=C**2
      C2=C**2
      F(1,1)=(3.0D0/4.0D0)*S*(1.0D0 + C)
      F(1,2)=(-3.0D0/2.0D0)*S*C
      F(1,3)=(-3.0D0/4.0D0)*S*(1.0D0 - C)
      F(2,1)=(3.0D0/4.0D0)*((1.0D0 + C)**2)
      F(2,2)=(3.0D0/2.0D0)*S2
      F(2,3)=(3.0D0/4.0D0)*((1.0D0 - C)**2)
      RETURN
      END

```

15N 0002 SUBROUTINE LAG1
C
C THIS SUBROUTINE READS IN THE SOLID EARTH LAG ANGLE XLAG AND CONVERTS IT
C FROM DEGREES TO RADIANS.

```

C      IMPLICIT REAL*8(A-H,C-Z)
IEN 0003  COMMON//BLKD/XLAG,Q,UMEGAM,DELMN,CMEGAS,DELSUN,SS,XIO,A,E,XI,XNCD,
IEN 0004  1 TZERO,XIMON,XISUN,TMS,XNDM,XNDS,F,XMEAN,XMEANS,XMDCTM,XMDCTS,
          2 UMGDOT,MEXP
IEN 0005  READ (5,1) XLAG
ISN 0006  1 FORMAT (BF10.5)
ISN 0007  2 WRITE (5,2) XLAG
ISN 0008  2 FORMAT (////////////,23X,*SOLID EARTH LAG ANGLE=*,FB.3,1X,*DEGREES*)
ISN 0009  XLAG=XLAG*F
IEN 0010  RETURN
IEN 0011  END

```

15N 0002 SUBROUTINE LAG2
C
C THIS SUBROUTINE SETS THE FREQUENCY DEPENDENT TIDAL LAG ANGLES INITIALLY
C EQUAL TO ZERO.

```

C
10003 IMPLICIT REAL*8(A-H,C-Z)
10004 DIMENSION EPSLN(2,3,3),EPSLN(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
1 ARGDTM(2,3,2),ARGDT(2,3,2)
10005 COMMON/BLKA/EPSLN,EPSLN,ARGUM,ARGUS,ARCDTM,ARGDT,
1 COMMON/BLKD/XLAG,Q,OMEGAM,DELMN,CMEGAS,DEL SUN,SS,XI),E,XI,XNODE,
1 TZERO,XIMON,XISUN,TMS,XNOM,XNDE,E,F,XMEANM,XMEANS,XRECTM,XMDOTS,
2 DMGDT,MEXP
10007 DU 10 LM=1,2
10008 DU 10 LP=1,3
10009 DU 10 LG=1,3
10010 EPSLN(1,1,LP,1,0)=0.000
10011 EPSLN(1,LM,LP,LG)=0.050
10012 10 CONTINU
10013 RETURN
10014 END

```

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ISN 0062

SUBROUTINE LASOTA

C
C THIS SUBROUTINE READS IN, THEN PRINTS OUT, THE OBSERVED TIP. XIEXP(J) IS
C THE OBSERVED TIP (IN ARCSSECONDS) AT TIME TEXP(J) (IN DAYS).
C TODAY IS A CORRECTION FACTOR, WHICH MAKES TEXP(J) START AT THE BEGINNING OF
C THE YEAR (JAN 1 AT 0 HRS UT = 1). TODAY IS NECESSARY SINCE OFTENTIMES THE
C TIME OF EACH DATA POINT IS GIVEN IN DAYS AFTER THE FIRST OBSERVATION (I.E.
C TEXP(1)=0.0).

ISN 0003
ISN 0004
ISN 0005
ISN 0006
ISN 0007
ISN 0008
ISN 0009
ISN 0010
ISN 0011
ISN 0012
ISN 0013
ISN 0014
ISN 0015
ISN 0016
ISN 0017
ISN 0018
ISN 0019
ISN 0020
ISN 0021
ISN 0022
ISN 0023
ISN 0024
ISN 0025
ISN 0026
ISN 0027
ISN 0028
ISN 0029
ISN 0030

IMPLICIT REAL*8(A-H,C-Z)
DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
COMMON/BLKD/XLAG,Q,UMEGAM,DELMN,CMEGAS,DELSUN,SS,XIC,A,E,XI,XNCD,E,
1 TZERL,XIMON,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMCOTM,XMDOTS,
2 XMDOT,MEXP
READ (5,33) MEXP,TDAY
FORMAT (15,F10.5)
DO 32 J=1,MEXP
READ (5,34) XIEXP(J),TEXP(J)
TEXP(J)=TEXP(J) + TDAY
CONTINUE
FORMAT (2D14.6)
WRITE (6,2)
FORMAT (1H1)
WRITE (6,3)
FORMAT (//////,50X,*SATELLITE TRACKING DATA*,/////)
WRITE (6,15) MEXP,TDAY
FORMAT (41X,*'15*' DATA POINTS, TDAY='',F8.4,* DAYS)*,/////)
WRITE (6,4)
FORMAT (48X,*TIME*,13X,*INCLINATION*,/)
WRITE (6,5)
FORMAT (7X,*(DAYS)*,14X,*'(APCSEC)*)
WRITE (6,6)
FORMAT (38X,*'(JAN 1, 0 HRS UT = 1)*,///)
DO 10 J=1,MEXP
10 WRITE (6,14) J,TEXP(J),XIEXP(J)
FORMAT (35X,1E+5X,F10.4,10X,F10.4)
RETURN
END

ISN 0032

SUBROUTINE LOVE

C
C THIS SUBROUTINE READS IN THE SECND DEGREE LOVE NUMBER AND LOAD
C DEFORMATION COEFFICIENT OF THE SOLID EARTH.

ISN 0003
ISN 0004
ISN 0005
ISN 0006
ISN 0007
ISN 0008
ISN 0009
ISN 0010
ISN 0011

IMPLICIT REAL*8(A-H,C-Z)
DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
COMMON/BLKA/B1,XK,CFNTM,CFN*5,SUM,XMOON,XSUN,YKM,YKS,XKP
READ (5,1) XK,XKP
FORMAT (3F10.5)
WRITE (6,2) XK,XKP
FORMAT (//////,23X,*SOLID EARTH LOVE NUMBER=*,F8.4,10X,*LOAD DEF
1FORMATION COEFFICIENT=*,F8.4)
RETURN
END

```

1SN 0002      SUBROUTINE LOVMUM(MT)
C
C  THIS SUBROUTINE TAKES THE COEFFICIENTS AND THEIR ERRORS FOUND IN
C  SUBROUTINE REGRES AND SOLVES FOR THE FREQUENCY DEPENDENT LOVE NUMBERS, TICAL
C  LAG ANGLES, AND THEIR ERRORS. IT ALSO FINDS THE OCEAN TIDE PARAMETERS.
C  ASSUMING THE SOLID EARTH LOVE NUMBER AND LAG ANGLE ARE KNOWN,
C  ****ALL TIDES ARE ASSUMED TO BE 2ND DEGREE ONLY. HENCE ALL OTHER TIDES ARE
C  ABSORBED INTO THE 2ND DEGREE TIDES.
C
C  IMPLICIT REAL*8(A-H,O-Z)
1SN 0003  REAL*4 VV(70),VE(70),ANS(10)
1SN 0004  DIMENSION EPSLNM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
1SN 0005  ARGDTM(2,3,3),ARGDTS(2,3,3)
1SN 0006  DIMENSION B(12),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKS(2,3,3)
1SN 0007  DIMENSION TXP(200),XEXP(200),TC(700),XINCL(700),NTRACK(700),
1SN 0008  DIMENSION C(2,3),A1(2,3),B(2,3),GLPQ(3,3),GLPQS(3,3)
1SN 0009  DIMENSION NN(7),ISAVE(70)
1SN 0010  DIMENSION TIDE(2,3,3)
1SN 0011  DIMENSION SAT(14)
1SN 0012  COMMON/BLKA/EPISLN,EPISLN,ARGUM,ARGUS,ARGDTM,ARGDTS
1SN 0013  COMMON/BLKB/B1,XK,CFNTM,CFNTS,SUM,XMOON,XSUN,YKM,YKS,XKP
1SN 0014  COMMON/BLKC/TXP,XEXP,T,XINCL,NTRACK
1SN 0015  COMMON/BLKD/XLAG,U,CMEGAM,DELMN,CMEGAS,DELSUN,SS,XIO,A,E,XI,XNODE,
1    TZERD,XMOON,XISUN,TMS,XNDM,XNDE,F,XMEAN,XMEAN,XNCTM,XMDOTS,
2    DMGDT,MEXP
1SN 0016  COMMON/BLKG/C,A1,B,GLPQ,GLPQS,INDEX
1SN 0017  COMMON/BLKH/VV,VE,ANS,ISAVE,M,K
1SN 0018  COMMON/BLKI/SAT
1SN 0019  DATA BLANK/4H   /
1SN 0020  DATA TM112,TM122,TM212,TM222/4H01 ,4HK1 ,4HK2 ,4HK3 /
1SN 0021  DATA TS112,TS122,TS212,TS222/4H01 ,4HK1S ,4HK2S ,4HK3S /
1SN 0022  PI=3.1415926535900
1SN 0023  YLAG=XLAG/F
C  SET THE ADDITIVE CONSTANT IN THE TIP EQUAL TO XIO
1SN 0024  XIO=ANS(1)
1SN 0025  WRITE (6,19)
1SN 0026  19  FORMAT (1H1)
C  PRINT OUT THE HEADINGS
1SN 0027  WRITE (6,31)
1SN 0028  31  FORMAT (23X,****FREQUENCY DEPENDENT LOVE NUMBERS****,10X,
1    ****OCEAN TIDE PARAMETERS****)
1SN 0029  WRITE (6,32)
1SN 0030  32  FORMAT (30X,*(ASSUMING 2ND DEGREE TIDES ONLY)*17X,*(ASSUMING 2ND
1    DEGREE TIDES*))
1SN 0031  WRITE (6,33)
1SN 0032  33  FORMAT (79X,*ONLY AND SOLID EARTH LOVE*)
1SN 0033  WRITE (6,34) XK
1SN 0034  34  FORMAT (79X,*NUMBER K2=*,F5.3,1X,*AND SOLID*)
1SN 0035  WRITE (6,35) YLAG
1SN 0036  35  FORMAT (79X,*EARTH TIDAL LAG=*,F6.3,1X,*DEG)*,/
1SN 0037  WRITE (6,40)
1SN 0038  40  FORMAT (1X,L4PQ TIDE DIS,BODY LOVE NUMBER STD. ERROR LAG
1    ANGLE STD. ERROR   C   STD. ERROR PHASE STD. ERROR
2    *)
1SN 0039  WRITE (6,39)
1SN 0040  39  FORMAT (51X,*(DEGREES)*,3X,*(DEGREES)*,7X,*(CM)*,3X,*(CM)*,3X,
1    1 *(DEGREES)*,4X,*(DEGREES)*,/)
C  SET NN(J)=0 FOR TIDES NOT SOLVED FOR BY THE MULTIPLE REGRESSION IN
C  SUBROUTINE REGRES, AND NN(J)=1 FOR THOSE WHICH ARE SOLVED FOR
1SN 0041  MV=M-1
1SN 0042  DO 20 J=1,MV
1SN 0043  20  NN(J)=0
1SN 0044  DO 21 J=1,K
1SN 0045  21  ISSE=ISAVE(J)
1SN 0046  NN(ISS)=1
C
C  ****LUNAR AND LUNISOLAR TIDES****
C
C  PUT NAME OF TIDAL CONSTITUENT IN ARRAY TIDE
1SN 0047  DO 89 LM=1,2
1SN 0048  DO 89 LP=1,3
1SN 0049  DO 89 LO=1,3
1SN 0050  89  TIDE(LM,LP,LO)=BLANK
1SN 0051  TIDE(1,1,2)=TM112
1SN 0052  TIDE(1,2,2)=TM122
1SN 0053  TIDE(2,1,2)=TM212

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ISN 0054 TIDE(2,2,2)=TM322
ISN 0055 LLL=2
ISN 0056 I=9
ISN 0057 DD 60 LM=4,2
ISN 0058 YLM=LM
ISN 0059 DD 60 LP=1,3
ISN 0060 YLP=LP - 1
ISN 0061 LP=LP - 1
ISN 0062 DD 60 LQ=1,3
ISN 0063 LQG=LQ - 2
ISN 0064 I=I + 1
ISN 0065 U1=VV(I)
ISN 0066 E1=VE(I)
ISN 0067 I=I
ISN 0068 I= I + 1
ISN 0069 U2=VV(I)
ISN 0070 E2=VE(I)
ISN 0071 C IF ONLY THE EFFECTIVE LOVE NUMBER IS SOLVED FOR, PUT THE EFFECTIVE LAG ANGLE
ISN 0072 C AND ITS ERROR EQUAL TO ZERO
ISN 0073 C IF (NN(1) .EQ. 0) U2=0.000
ISN 0074 C IF (NN(1) .EQ. 0) E2=0.000
ISN 0075 C IF THIS TIDE WAS NOT SOLVED FOR, GO TO 62
ISN 0076 C IF (NN(I3) .EQ. 0 .AND. NN(I) .EQ. 0) GO TO 62
ISN 0077 C U3=U1*2 + U2*F2
ISN 0078 C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER
ISN 0079 C YKM(LM,LP,LQ)=DSORT(U3)
ISN 0080 C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE, MAKING SURE WE KNOW WHICH
ISN 0081 C QUADRANT IT IS IN
ISN 0082 C EPSLNM(L4,LP,LQ)=DATAN(U4)
ISN 0083 C IF (U4) 22,25,23
ISN 0084 C 23 CONTINUE
ISN 0085 C IF (U1) 29,47,27
ISN 0086 C 24 EPSLNM(LM,LP,LQ)=PI
ISN 0087 C GO TO 27
ISN 0088 C 22 CONTINUE
ISN 0089 C IF (U2) 25,24,24
ISN 0090 C 25 EPSLNM(LM,LP,LQ)=EPSLNM(LM,LP,LQ) + PI
ISN 0091 C 26 CONTINUE
ISN 0092 C 27 IF (U2) 25,47,27
ISN 0093 C 28 EPSLNM(LM,LP,LQ)=EPSLNM(LM,LP,LQ) + PI
ISN 0094 C 29 CONTINUE
ISN 0095 C EP IS THE EFFECTIVE TIDAL LAG ANGLE IN DEGREES
ISN 0096 C EPS=EPSLNM(LM,LP,LQ)/F
ISN 0097 C SIGSOR=((E1*#2)*(U1*#2) + (E2*#2)*(U2*#2))/U3
ISN 0098 C SIGLOV IS THE STD. ERROR OF YKM(LM,LP,LQ)
ISN 0099 C SIGLOV=DSORT(SIGSOR)
ISN 0100 C SIGSOR=((E2*#2)*(U1*#2) + (E1*#2)*(U2*#2))/U3*#2
ISN 0101 C SIGLAG IS THE STD. ERROR OF EPSLNM(LM,LP,LQ) IN DEGREES
ISN 0102 C SIGLAG=DSORT(SIGSOR)/F
ISN 0103 C
ISN 0104 C FACTOR=1.000 + (CFNTS*B(LM,2))/(CFNTM*A1(LM,LP))
ISN 0105 C
ISN 0106 C DC THE OCEAN TIDES
ISN 0107 C
ISN 0108 C YM*XLAG IS THE LAG ANGLE OF THE SOLID EARTH CONVERTED TO FREQUENCY-DEPENDENT
ISN 0109 C FORM
ISN 0110 C YM=LM
ISN 0111 C CXLAG=DCOS(YM*XLAG)
ISN 0112 C SXLAG=DSIN(YM*XLAG)
ISN 0113 C SUBTRACT OUT THE SOLID EARTH TIDE
ISN 0114 C SEA1=U1 - XK*CXLAG
ISN 0115 C IF (LP .EQ. 2 .AND. LQ .EQ. 2) SEA1=U1 - FACTOR*XK*CXLAG
ISN 0116 C SEA2=U2 - XK*SXLAG
ISN 0117 C IF (LP .EQ. 2 .AND. LQ .EQ. 2) SEA2=U2 - FACTOR*XK*SXLAG
ISN 0118 C SEA3=SEA1*#2 + SEA2*#2
ISN 0119 C SEA3=DSORT(SEA1)
ISN 0120 C FIND COCEAN, THE OCEAN AMPLITUDE
ISN 0121 C COCEAN=(320.0375500)*SEA5*B1(LM)*A1(LM,LP)/(1.000 + XKP)
ISN 0122 C SIGSOR=((E1*#2)*(SEA1*#2) + (E2*#2)*(SEA2*#2))/SEA3
ISN 0123 C SIG=DSORT(SIGSOR)
ISN 0124 C SIGC IS THE STD. ERROR OF COCEAN

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ISN 0115      SIGC=(320.0379500)*SIG*B1(LM)*DABS(A1(LM,LP))/(1.000 + XKP)
ISN 0116      SIGSOP=((E2*2)+(SEA1*2)+(E1*2)+(SEA2*2))/(SEA3*2)
ISN 0117      SIGPHS=DSQRT(SIGSOP)/F
ISN 0118      U44=SEA2/SEA1
ISN 0119      C FIND THE PHASE ANGLE OF THE OCEAN TIDE, MAKING SURE WE KNOW WHICH QUADRANT
ISN 0120      C IT IS IN
ISN 0121      43  PHASE=DATAN(U44)
ISN 0122      .F (U44) 42.48.43
ISN 0123      48  CONTINUE
ISN 0124      IF (SEA1) 49.47.47
ISN 0125      49  PHASE=PI
ISN 0126      GO TO 47
ISN 0127      42  CONTINUE
ISN 0128      IF (SEA2) 45.44.44
ISN 0129      44  PHASE=PHASE + PI
ISN 0130      45  CONTINUE
ISN 0131      GO TO 47
ISN 0132      IF (SEA2) 45.47.47
ISN 0133      46  PHASE=PHASE + PI
ISN 0134      47  CONTINUE
ISN 0135      PHASE=-PHASE + (YM - 1.000)*(PI/2.000)
ISN 0136      C INSURE THAT COPLAN IS A POSITIVE AMPLITUDE
ISN 0137      IF (COPLAN) 51.50.50
ISN 0138      51  COCEAN=COPLAN
ISN 0139      52  PHASE=PHASE - PI
ISN 0140      53  CONTINUE
ISN 0141      C CONVERT PHASE FROM RADIANS TO DEGREES
ISN 0142      PHASE=PHASE*F
ISN 0143      IF (PHASE) 90.91.91
ISN 0144      90  PHASE=PHASE+360.0
ISN 0145      91  CONTINUE
ISN 0146      IF (PHASE) 92.93.93
ISN 0147      92  PHASE=PHASE+360.0
ISN 0148      93  CONTINUE
ISN 0149      IF (LP .EQ. 2 .AND. LO .EQ. 2) GO TO 67
ISN 0150      C PRINT OUT L,M,P,O, CONSTITUENT, DISTURBING BODY, FREQUENCY DEPENDENT LOVE
ISN 0151      C NUMBER AND ITS ERROR, LAG ANGLE AND ITS ERROR, OCEAN AMPLITUDE AND ITS
ISN 0152      C ERROR, PHASE ANGLE AND ITS ERROR
ISN 0153      WRITE (5,53) LLL,LLV,LPP,LQO,TIDE(LM,LP,LO),YKM(LM,LP,LC),SIGLOV,EP
ISN 0154      54  1,SIGLAG,COCEAN,SIGC,PHASE,SIGPHS
ISN 0155      55  FORMAT (+1E.2,A4.4X,*MOON*,5X,F10.5,2X,F10.5,2X,F9.5,3X,F9.5,
ISN 0156      56  1+4X,F10.5,2X,F10.5,2X,F9.4,2X,F9.4)
ISN 0157      57  GO TO 69
ISN 0158      XLVNUM=YKM(LM,LP,LO)/FACTOR
ISN 0159      SIGLOV=SIGLOV/FACTOR
ISN 0160      WRITE (5,55) LLL,LM,LPP,LQO,TIDE(LM,LP,LO),XLVNUM,SIGLCV,EP,SIGLAG
ISN 0161      58  1,COCEAN,SIGC,PHASE,SIGPHS
ISN 0162      59  FORMAT (+12.2X,A4.2X,*MCM+SUN*,3X,F10.5,2X,F10.5,2X,F9.5,3X,F9.5,
ISN 0163      60  1+4X,F10.5,2X,F10.5,2X,F9.4,2X,F9.4)
ISN 0164      61  CONTINUE
ISN 0165      GO TO 60
ISN 0166      62  CONTINUE
ISN 0167      63  CONTINUE
ISN 0168      64  CONTINUE
ISN 0169      WRITE (6,13)
ISN 0170      13  FORMAT (10X,///)
ISN 0171      C ****SOLAR TIDES****
ISN 0172      C
ISN 0173      C PUT NAME OF TIDAL CONSTITUENT IN APPAY TIDE
ISN 0174      83  DO 88 LM=1,2
ISN 0175      84  DO 88 LP=1,3
ISN 0176      85  DO 88 LO=1,3
ISN 0177      86  TIDE(LM,LP,LC)=BLANK
ISN 0178      TIDE(1,1,2)=TE112
ISN 0179      TIDE(1,2,2)=TE122
ISN 0180      TIDE(1,1,3)=TE212

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157 ISN 0178      TIDE(2,2,2)=TS222
158 ISN 0179      DO 65 LM=1,2
159 ISN 0180      YLM=LM
160 ISN 0181      DO 65 LP=1,3
161 ISN 0182      YLP=LP - 1
162 ISN 0183      LPY=LP - 1
163 ISN 0184      DO 65 LQ=1,3
164 ISN 0185      LQY=LQ - 2
165 ISN 0186      IF (LP .EQ. 2 .AND. LQ .EQ. 2) GO TO 66
166 ISN 0187      I=I + 1
167 ISN 0188      U1=VV(I)
168 ISN 0189      E1=VE(I)
169 ISN 0190      I3=I
170 ISN 0191      I=I + 1
171 ISN 0192      U2=-VV(I)
172 ISN 0193      E2=VE(I)
173 ISN 0194      C IF ONLY THE EFFECTIVE LOVE NUMBER IS SOLVED FOR, PUT THE EFFECTIVE LAG ANGLE
174      C AND ITS ERROR EQUAL TO ZERO
175 ISN 0195      IF (NN(I) .EQ. 0) U2=0.000
176 ISN 0196      IF (NN(I) .EQ. 0) E2=0.000
177 ISN 0197      C IF THIS TIDE WAS NOT SOLVED FOR, GO TO 66
178 ISN 0198      IF (NN(I3) .EQ. 0 .AND. NN(I) .EQ. 0) GO TO 66
179 ISN 0199      U3=U1**2 + U2**2
180 ISN 0200      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LOVE NUMBER
181      YKS(LM,LP,LQ)=DSQRT(U3)
182 ISN 0203      U=U2/U1
183 ISN 0204      C FIND THE EFFECTIVE FREQUENCY-DEPENDENT LAG ANGLE, MAKING SURE WE KNOW WHICH
184      C QUADRANT IT IS IN
185      EPSLNS(LM,LP,LQ)=DATAN(U4)
186 ISN 0205      IF (U4) 32,36,33
187 ISN 0206      33  CONTINUE
188 ISN 0207      IF (U1) 41,37,37
189 ISN 0208      41  EPSLNS(LM,LP,LQ)=PI
190 ISN 0209      GO TO 37
191 ISN 0210      32  CONTINUE
192 ISN 0211      IF (U2) 35,34,34
193 ISN 0212      34  EPSLNS(LM,LP,LQ)=EPSLNS(LM,LP,LQ) + PI
194 ISN 0213      35  CONTINUE
195 ISN 0214      GO TO 37
196 ISN 0215      33  CONTINUE
197 ISN 0216      IF (U2) 36,37,37
198 ISN 0217      36  EPSLNS(LM,LP,LQ)=EPSLNS(LM,LP,LQ) + PI
199 ISN 0218      37  CONTINUE
200 ISN 0219      C EP IS THE EFFECTIVE TIDAL LAG ANGLE IN DEGREES
201      EP=EPSLNS(LM,LP,LQ)/F
202 ISN 0220      SIGLOF=((E1**2)*(U1**2) + (E2**2)*(U2**2))/U3
203 ISN 0221      C SIGLOF IS THE STD. ERROR OF YKS(LM,LP,LQ)
204      SIGLOF=DSQRT(SIGSQR)
205 ISN 0222      SIGSQR=((E1**2)*(U1**2) + (E2**2)*(U2**2))/(U3**2)
206 ISN 0223      C SIGLAG IS THE STD. ERROR OF EPSLNS(LM,LP,LQ) IN DEGREES
207      SIGLAG=DSQRT(SIGSQR)/F
208 ISN 0224      C DO THE OCEAN TIDES
209 ISN 0225      YM=LM
210 ISN 0226      C YM+XLAG IS THE LAG ANGLE OF THE SOLID EARTH CONVERTED TO FREQUENCY-DEPENDENT
211      C FORM
212      CXLAG=DCOS(YM+XLAG)
213      SXLAG=DSIN(YM+XLAG)
214 ISN 0227      C SUBTRACT OUT THE SOLID EARTH TIDE
215      SEA1=U1 - XK*CXLAG
216 ISN 0228      SEA2=U2 - XK*SXLAG
217 ISN 0229      SEA3=SEA1**2 + SEA2**2
218 ISN 0230      SEA3=DSQRT(SEA3)
219 ISN 0231      C FIND COCEAN, THE OCEAN AMPLITUDE
220      COCEAN=(145.775500)*SEA5*J1(LM)*P(LM,LP)/(1.000 + XKP)
221 ISN 0232      SIGSQR=((E1**2)*(SEA1**2) + (E2**2)*(SEA2**2))/SEA3
222 ISN 0233      SIGSQR=DSQRT(SIGSQR)
223 ISN 0234      C SIGC IS THE STD. ERROR OF COCEAN
224      SIGC=(145.775500)*SIG*BITLM*DABS(P(LM,LP))/(1.000 + XKP)
225 ISN 0235      SIGC=DSQRT(SIGC)
226 ISN 0236      C SIGPHS IS THE STD. ERROR OF THE PHASE ANGLE IN DEGREES
227      SIGPHS=DSQRT(SIGSQR)/F
228 ISN 0237      I44=SEA2/SEA1
229 ISN 0238      C FIND THE PHASE ANGLE OF THE OCEAN TIDE, MAKING SURE WE KNOW WHICH QUADRANT
230      C IT IS IN
231      PHASE=DATAN(I44)
232 ISN 0239      IF (I44) 52,55,53
233 ISN 0240      53  CONTINUE
234 ISN 0241      IF (SEA1) 54,57,57

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1SN 0242      59  PHASE=PI
1SN 0243      60  GO TO 57
1SN 0244      62  CONTINUE
1SN 0245      63  IF (SEA2) 55,54,54
1SN 0246      64  PHASE=PHASE + PI
1SN 0247      65  CONTINUE
1SN 0248      66  GO TO 57
1SN 0249      67  CONTINUE
1SN 0250      68  IF (SEA2) 56,57,57
1SN 0251      69  PHASE=PHASE + PI
1SN 0252      70  CONTINUE
1SN 0253      71  PHASE=PHASE + (YM - 1.000)*(PI/2.0D0)
1SN 0254      72  C INSURE THAT COCEAN IS A POSITIVE AMPLITUDE
1SN 0255      73  IF (COCEAN) 73,74,74
1SN 0256      74  COCEAN=COCEAN
1SN 0257      75  PHASE=PHASE - PI
1SN 0258      76  CONTINUE
1SN 0259      77  C CONVERT PHASE FROM RADIANS TO DEGREES
1SN 0260      78  PHASE=PHASE*F
1SN 0261      79  IF (PHASE) 75,76,76
1SN 0262      80  PHASE=PHASE+360.0
1SN 0263      81  CONTINUE
1SN 0264      82  IF (PHASE) 77,78,78
1SN 0265      83  PHASE=PHASE+360.0
1SN 0266      84  CONTINUE
1SN 0267      85  IF (PHASE) 77,78,78
1SN 0268      86  PHASE=PHASE+360.0
1SN 0269      87  CONTINUE
1SN 0270      88  C PRINT OUT L,M,P,Q, CONSTITUENT, DISTURBING BODY, FREQUENCY DEPENDENT LOVE
1SN 0271      89  NUMBER AND ITS ERROR, LAG ANGLE AND ITS ERROR, OCEAN AMPLITUDE AND ITS
1SN 0272      90  ERROR, PHASE ANGLE AND ITS ERROR
1SN 0273      91  WRITE (6,71) LLL,LM,LPP,LQ,Q,TIDE(LM,LP,LQ),YKS(LM,LP,LQ),SIGLOV,EP
1SN 0274      92  71  FORMAT (4I2,2X,A4,5X,*8N*,5X,F10.5,2X,F10.5,2X,F9.5,3X,F9.5,
1SN 0275      93  72  14X,F10.5,2X,F10.5,2X,F9.4,2X,F9.4)
1SN 0276      94  GO TO 65
1SN 0277      95  CONTINUE
1SN 0278      96  C SET THE LOVE NUMBER AND LAG ANGLE TO ZERO FOR TIDES NOT SOLVED FOR
1SN 0279      97  YKS(LM,LP,LQ)=0.000
1SN 0280      98  EPSLNS(LM,LP,LQ)=0.000
1SN 0281      99  WRITE (6,91) LLL,LM,LPP,LQ,Q,TIDE(LM,LP,LQ)
1SN 0282      100  FORMAT (4I2,2X,A4,5X,*8N*,12X,*8N*,8X,*8N*,8X,*8N*)
1SN 0283      101  14I2,*8N*,8X,*8N*,8X,*8N*,8X,*8N*)
1SN 0284      102  CONTINUE
1SN 0285      103  WRITE (6,94) (EAT(J), J=1,14)
1SN 0286      104  FORMAT (13A5,A2)
1SN 0287      105  C PRINT OUT L, T(L), AND XINCL(L)
1SN 0288      106  DO 10 L=1,MT
1SN 0289      107  TT=T(L)
1SN 0290      108  CALL APLS(TT)
1SN 0291      109  SUM=0.000
1SN 0292      110  DU 70 L=1,2
1SN 0293      111  YLM=LM
1SN 0294      112  DO 70 LP=1,3
1SN 0295      113  YLP=LP - 1
1SN 0296      114  DO 70 LQ=1,3
1SN 0297      115  XINCL(L,LP,LQ)=YKS(LM,LP,LQ)*CFNTM+B1(LM)*C(LM,2)*A1(LM,LP)*GLPOM
1SN 0298      116  1(LP,LQ)*YLM*ARGUM(LM,LP,LQ)/(ARGCTM(LM,LP,LQ)*SS)
1SN 0299      117  XSUM(LM,LP,LQ)=YKS(LM,LP,LQ)*CFNTM+B1(LM)*C(LM,2)*E(LM,LP)*GLPQS(L
1SN 0300      118  1P,LP)*YLM*ARGUE(LM,LP,LQ)/(APGDTM(LM,LP,LQ)*SS)
1SN 0301      119  SJ=SUM + XMOON(LM,LP,LQ) + XUN(LM,LP,LQ)
1SN 0302      120  SUM=SUM + SJ
1SN 0303      121  XINCL(L)=SUM + X10
1SN 0304      122  CONTINUE
1SN 0305      123  WRITE (6,15)
1SN 0306      124  WRITE (6,100)
1SN 0307      125  100  FORMAT (40X,*TIDAL INCLINATION*,//)
1SN 0308      126  WRITE (6,101)
1SN 0309      127  101  FORMAT (15X,*TIME*,18X,*INCLINATION*)
1SN 0310      128  WRITE (6,122)
1SN 0311      129  102  FORMAT (30X,*JAN 1, 0 HRS UT = 1*.*12X,*APCSEC*.,//)
1SN 0312      130  DO 12 L=1,MT
1SN 0313      131  WRITE (6,12) L,T(L),XINCL(L)
1SN 0314      132  CONTINUE
1SN 0315      133  FORMAT (20X,15,5X,D15.5,10X,D15.5)
1SN 0316      134  C PRINT RESIDUALS
1SN 0317      135  WRITE (6,19)
1SN 0318      136  WRITE (6,103)
1SN 0319      137  103  FORMAT (45X,*RESIDUALS*,//)
1SN 0320      138  WRITE (6,104)
1SN 0321      139  104  FORMAT (35X,*TIME*,18X,*RESIDUAL*)
1SN 0322      140  WRITE (6,102)
1SN 0323      141  SUMSIG=0.0

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1SN 0305      DO 4 J=1,MEXP
1SN 0310      TT=TEXP(J)
1SN 0311      CALL ARG(TT)
1SN 0312      SUM=0.0
1SN 0313      DO 3 L=1,L
1SN 0314      YLM=LM
1SN 0315      DO 3 LP=1,3
1SN 0316      YLP=LP - 1
1SN 0317      DO 3 LQ=1,3
1SN 0318      XMDON(LM,LP,LQ)=YKM(LM,LP,LQ)*CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*GLPOM
1SN 0319      *(LP,LQ)-YLM*ARGUM(LM,LP,LQ)/(ARGOM(LM,LP,LQ)*SS)
1SN 0320      XSMN(LM,LP,LQ)=YKS(LM,LP,LQ)*CFNTS*B1(LM)*C(LM,2)*P(LM,LP)*GLPQS(L
1SN 0321      LP,LQ)-YLM*ARGUS(LM,LP,LQ)/(ARGOTS(LM,LP,LQ)*SS)
1SN 0322      SUM=SUM + XMDON(LM,LP,LQ) + XSMN(LM,LP,LQ)
1SN 0323      CONTINUE
1SN 0324      SUM=SUM + XI0
1SN 0325      RES1=IXEXP(J) - SUM
1SN 0326      SUMSIG=RES1**2 + SUMSIG
1SN 0327      WRITE (6,13) J,TEXP(J),RES1
1SN 0328      CONTINUE
1SN 0329      XN=MEXP - 1
1SN 0330      SIGMA=DSQRT(SUMSIG/XN)
1SN 0331      105 FORMAT (/////,10X, "SIGMA = SQRT((SUM OF SQUARES)/(MEXP-1)) = ", *
1SN 0332      & F10.5)
1SN 0333      C PLUT CUT XINCL(L) VS. T(L), RESIDUALS ON COMPUTER PAPER
1SN 0334      CALL PLETER(MT,MEXP)
1SN 0335      RETURN
1SN 0336      END

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ISN 0002

SUBROUTINE PLOTER(MT,MEXP)

C THIS SUBROUTINE PLOTS A CONTINUOUS CURVE PLUS EXPERIMENTAL DATA POINTS
C VS. TIME T(L). IT ALSO PLOTS THE RESIDUALS VS. TIME T(L).
C TIME INCREASES DOWN THE PAGE AND THE WIDTH OF THE PLOT IS 101 SPACES ACROSS.
C THERE ARE MT POINTS IN THE CURVE, WHICH IS STORED IN ARRAY XINCL(L), AND
C MEXP EXPERIMENTAL DATA POINTS, STORED IN ARRAY XIEXP(J). THE POINTS OF THE
C CURVE ARE PRINTED AS D'S AND THE DATA POINTS AS X'S.
C

ISN 0003 IMPLICIT REAL*8(A-H,D-Z)
ISN 0004 DIMENSION RESID(200)
ISN 0005 DIMENSION BINE(101)
ISN 0006 DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0007 COMMON/HLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0008 DATA DEE,EKS,HLANK/1H0,1H0,1H/
C DETERMINE THE WIDTH OF THE PLOT, BY FINDING THE MAXIMUM AND MINIMUM POINTS OF
C THE CURVE AND THE DATA POINTS
ISN 0009 XMAX1=XINCL(1)
ISN 0010 XMIN1=XINCL(1)
ISN 0011 DO 30 I=2,MT
ISN 0012 P=XINCL(I)
ISN 0013 IF (XMAX1 - P) 22,21,21
ISN 0014 22 XMAX1=P
ISN 0015 GO TO 30
ISN 0016 21 CONTINUE
ISN 0017 IF (P - XMIN1) 24,30,30
ISN 0018 24 XMIN1=P
ISN 0019 30 CONTINUE
ISN 0020 IF (MEXP .EQ. 0) GO TO 4
ISN 0021 GO TO 5
ISN 0022 4 XMAX=XMAX1
ISN 0023 XMIN=XMIN1
ISN 0024 GO TO 50
ISN 0025 5 CONTINUE
ISN 0026 XMAX2=XIEXP(1)
ISN 0027 XMIN2=XIEXP(1)
ISN 0028 DU 40 J=2,MEXP
ISN 0029 P=XIEXP(J)
ISN 0030 IF (XMAX2 - P) 42,41,41
ISN 0031 42 XMAX2=P
ISN 0032 GO TO 40
ISN 0033 41 CONTINUE
ISN 0034 IF (P - XMIN2) 43,40,40
ISN 0035 43 XMIN2=P
ISN 0036 40 CONTINUE
ISN 0037 45 IF (XMAX2 - XMAX1) 45,46,46
ISN 0038 XMAX=XMAX2
ISN 0039 GO TO 47
ISN 0040 47 XMAX=XMAX1
ISN 0041 CONTINUE
ISN 0042 IF (XMIN2 - XMIN1) 48,49,49
ISN 0043 48 XMIN=XMIN2
ISN 0044 GO TO 50
ISN 0045 49 XMIN=XMIN1
ISN 0046 50 CONTINUE
C COMPUTE FAC, SO THAT ALL OF THE POINTS FIT ON THE PAPER
ISN 0047 FAC=100.000/(XMAX-XMIN)
ISN 0048 WRITE (5,3)
ISN 0049 3 FORMAT (1H1)
ISN 0050 SCALE=XMAX - XMIN
ISN 0051 C WRITE THE LOWEST POINT, HIGHEST POINT, AND DISTANCE BETWEEN THEM
ISN 0052 WRITE (5,131) XMIN,XMAX,SCALE
ISN 0053 C SET ARRAY BINE(J) INITIALLY EQUAL TO BLANK
ISN 0054 20 BINE(J)=BLANK
ISN 0055 DU 29 L=1,MT
ISN 0056 J6=1
C PUT CURVE POINT IN BINE(JJ)
ISN 0057 JJ=(XINCL(L) - XMIN)*FAC + 1.51
ISN 0058 BINE(JJ)=DEE
C SEE IF AN EXPERIMENTAL DATA POINT SHOULD BE PLOTTED, BY CHECKING THE VALUE OF
C NTRACK(L)
ISN 0059 IF (NTRACK(L) .EQ. 0) GO TO 50
ISN 0060 NN=NTRACK(L)
C PUT EXPERIMENTAL DATA POINT IN BINE(J4)
ISN 0061 J4=(XIEXP(NN) - XMIN)*FAC + 1.51
ISN 0062

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ISN 0063      BINE(J4)=EKS
ISN 0064      60  CONTINUE
ISN 0065      C PRINT THE NUMBER OF THE CURVE POINT, BINE, AND THE NUMBER OF THE CURVE POINT
ISN 0066      WRITE (6,25) L,(BINE(J1), J1=1,101),L
ISN 0067      25  FORMAT (3X,15,2X,101A1,1X,15)
ISN 0068      C PUT ARRAY BINE(J) BACK TO BLANK
ISN 0069      BINE(JJ)=BLANK
ISN 0070      29  CONTINUE
ISN 0071      IF (MEXP .EQ. 0) GO TO 130
ISN 0072      C PLOT RESIDUALS VS. TIME
ISN 0073      DO 132 J=1,MEXP
ISN 0074      132  CONTINUE
ISN 0075      DO 101 L=1,MT
ISN 0076      IF (INTRACK(L) .EQ. 0) GO TO 101
ISN 0077      NN=NTRACK(L)
ISN 0078      RESID(NN)=X1EXP(NN) - XINCL(L)
ISN 0079      101  CONTINUE
ISN 0080      XMAX2=RESID(1)
ISN 0081      XMIN2=RESID(1)
ISN 0082      DO 140 J=2,MEXP
ISN 0083      140  CONTINUE
ISN 0084      P=RESID(J)
ISN 0085      IF (XMAX2 - P) 142,141,141
ISN 0086      XMAX2=P
ISN 0087      GO TO 140
ISN 0088      141  CONTINUE
ISN 0089      IF (P - XMIN2) 144,140,140
ISN 0090      144  XMIN2=P
ISN 0091      140  CONTINUE
ISN 0092      SCALE=XMAX2 - XMIN2
ISN 0093      WRITE (6,3)
ISN 0094      WRITE (6,13) XMIN2,XMAX2,SCALE
ISN 0095      131  FORMAT (10X,*MINIMUM=*,F10.5,10X,*MAXIMUM=*,F10.5,10X,
1  *SCALE=*,F10.5,*//)
ISN 0096      FAC=100.000/(XMAX2 - XMIN2)
ISN 0097      DO 126 J=1,1C1
ISN 0098      126  BINE(J)=BLANK
ISN 0099      DO 129 L=1,MT
ISN 0100      J4=1
ISN 0101      JJ=(-XMIN2)*FAC + 1.51
ISN 0102      BINE(JJ)=EKS
ISN 0103      IF (INTRACK(L) .EQ. 0) GO TO 160
ISN 0104      NN=NTRACK(L)
ISN 0105      J4=(RESID(NN) - XMIN2)*FAC + 1.51
ISN 0106      BINE(J4)=EKS
ISN 0107      160  CONTINUE
ISN 0108      WRITE (6,25) L,(BINE(J1), J1=1,1C1),L
ISN 0109      BINE(JJ)=BLANK
ISN 0110      BINE(J4)=BLANK
ISN 0111      129  CONTINUE
ISN 0112      130  CONTINUE
ISN 0113      RETURN
ISN 0114      END

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ISN 0002      SUBROUTINE RESAT
C
C THIS SUBROUTINE READS IN AND PRINTS OUT THE SATELLITE ELEMENTS AND NODE
C RATE. ALL INPUT IN DEGREES (OR DEGREES PER DAY) IS IMMEDIATELY CONVERTED TO
C RADIANS (OR RADIANS PER DAY) FOR USE IN THE PROGRAM.
C
C
ISN 0003      IMPLICIT REAL*8(A-H,O-Z)
ISN 0004      DIMENSION SAT(14)
ISN 0005      COMMON/RLK0/ XLAG,Q,CMEGAM,DELMN,CMEGAS,DELSUN,SS,X10,A,E,XI,XNODE1,
1  TZERO,Y1MOND,Y1SUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDOTM,XMDOTS,
2  OMDDOT,MEXP
ISN 0006      COMMON/BLK1/SAT
ISN 0007      READ (5,7) (SAT(J), J=1,14)
ISN 0008      7   FORMAT (13A6,A2)
ISN 0009      WRITE (5,2)
ISN 0010      2   FORMAT (1H1)
ISN 0011      WRITE (6,8) (SAT(J), J=1,14)
ISN 0012      8   FORMAT (10X,*14X,*ATELLITE*,1X,13A6,A2)
ISN 0013      READ (5,1) A,E,Q1,XI1,TZERO,XNODE1
ISN 0014      1   FORMAT (3F10.5)
ISN 0015      XI=XI1*F
ISN 0016      Q=Q1*F
ISN 0017      XNODE=XNODE1*F
ISN 0018      WRITE (5,3)
ISN 0019      3   FORMAT (10X,*50X,*SATELLITE DATA*,10X)
ISN 0020      4   FORMAT (24X,*A*,14X,*E*,10X,*INCLINATION*,AX,*NODE RATE*,RX,*TZERO
1  *11X,*NODE*,1X)
ISN 0021      WRITE (5,5)
ISN 0022      5   FORMAT (14X,*10**5 CM*,21X,*DEGREES*,5X,*DEG/DAY*,8X,*DAYS)
ISN 0023      6   FORMAT (23X,*DEGREES*,1X)
ISN 0024      WRITE (6,9) A,E,XI1,Q1,TZERO,XNODE1
ISN 0025      9   FORMAT (20X,6(F10.4,5X))
ISN 0026      RETURN
ISN 0027      END

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15N 0002          SUBROUTINE READMS
C
C   THIS SUBROUTINE READS IN AND PRINTS OUT THE POSITION AND ANGULAR SPEEDS OF
C   THE MOON AND SUN. INPUT IN DEGREES (OR DEGREES PER DAY) IS IMMEDIATELY
C   CONVERTED TO RADIANS (OR RADIANS PER DAY) FOR USE IN THE PROGRAM.
C
C
15N 0003          IMPLICIT REAL*8(A-H,C-Z)
15N 0004          COMMON/BULKD/XLAG,Q,CMEGAM,DELMN,CMEGAS,DELSUN,SS,XID,A,F,XI,XNODE,
15N 0005          &TZERI,XIMCUN,XISUN,TMS,XNDM,XNDS,F,XMEANM,XMEANS,XMDUTM,XMDOTS,
15N 0006          &OMGDOT,MEXP
15N 0007          READ (5,1) 1OMEGA1,DELT1,OMEGA2,DELT2,XNDM1,CMGDT1
15N 0008          READ (5,1) XID1,XID2,TMS,XMEAN1,XMEAN2
15N 0009          FORMAT (3F10.5)
15N 0010          XIMCUN=XID1*F
15N 0011          XISUN=XID2*F
15N 0012          DELMN=DELT1*F
15N 0013          DELSUN=DELT2*F
15N 0014          CMEGAM=CMEGAM*F
15N 0015          CMEGAS=CMEGA2*F
15N 0016          XMEANS=XMEAN1*F
15N 0017          XMEANM=XMEAN2*F
15N 0018          XNDM=XNDM1*F
15N 0019          XNDS1=2.93E47
15N 0020          WRITE (6,3)
15N 0021          FORMAT (10X,//////,5X,'MOON AND SUN DATA',////)
15N 0022          WRITE (6,3)
15N 0023          FORMAT (12X,'(CMEGA)',10X,'DELT1',7X,'INCLINATION',7X,'TMS ',8X,
15N 0024          1,'MEAN ANOMALY',2X,'MEAN MOTION',5X,'NODE RATE',/1)
15N 0025          WRITE (6,4)
15N 0026          FORMAT (21X,'(L.GREEK)',6X,'(DEGREES)',6X,'(DEGREES)',7X,'(CAYS)',4X,
15N 0027          ' (DEGREE/S)',4X,'(DEG/DAY)',6X,'(DEG/DAY)',/1)
15N 0028          WRITE (6,5) CMEGAM,DELT1,XID1,TMS,XMEAN1,XNDM1,CMGDT1
15N 0029          FORMAT (6X,'MOON',10X,7(F10.4,5X),/1)
15N 0030          WRITE (6,6) CMEGAS,DELT2,XID2,TMS,XMEAN2,XNDS1
15N 0031          FORMAT (6X,'SUN',11X,6(F10.4,5X))
15N 0032          RETURN
15N 0033          END

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ORIGINAL PAGE IS
OF POOR QUALITY

C
 C THIS SUBROUTINE CARRIES OUT THE MULTIPLE REGRESSION ANALYSIS.
 C THIS SUBROUTINE IS A MODIFICATION OF THE PROGRAM EXPLAINED AND LISTED ON
 C PAGES 303 - 407 OF THE IBM SYSTEM/360 SCIENTIFIC SUBROUTINE PACKAGE,
 C VERSION III, PROGRAMMERS MANUAL, PROGRAM NUMBER 20CA-CW-03X, FIFTH EDITION
 C (AUGUST 1970).

C THE PURPOSE HERE IS TO (1) READ THE PROBLEM PARAMETER CARD FOR A MULTIPLE
 C REGRESSION, (2) READ SUBSET SELECTION CARDS, (3) CALL THE SUBROUTINES TO
 C CALCULATE MEANS, STANDARD DEVIATIONS, SIMPLE AND MULTIPLE CORRELATION
 C COEFFICIENTS, T-VALUES, AND ANALYSIS OF VARIANCE FOR MULTIPLE REGRESSION,
 C (4) PRINT THE RESULTS, AND (5) SAVE THE REGRESSION COEFFICIENTS AND THEIR
 C ERRORS FOR SUBROUTINE LCNVN.

C THE NUMBER OF OBSERVATIONS, NEXP, IS CALLED N IN THIS SUBROUTINE. N MUST
 C BE GREATER THAN M+1, WHERE M IS THE NUMBER OF VARIABLES.

C IF SUBSET SELECTION CARDS ARE NOT PRESENT, THE PROGRAM CANNOT PERFORM
 C MULTIPLE REGRESSION.

C AFTER RETURNING FROM SUBROUTINE MINV, THE VALUE OF DETERMINANT (DET) IS
 C TESTED TO CHECK WHETHER THE CORRELATION MATRIX IS SINGULAR. IF DET IS
 C COMPARED AGAINST A SMALL CONSTANT, THIS TEST MAY ALSO BE USED TO CHECK NEAR-
 C SINGULARITY.

C THIS SUBROUTINE CALLS SUBROUTINES CORRE (WHICH, IN TURN, CALLS SUBROUTINE
 C DATA), ORDER, MINV, MULTR. ONLY DATA IS FOUND LISTED HERE, SINCE THE OTHERS
 C ARE STANDARD SUBROUTINES CONTAINED IN THE MACHINE.

C
 C THE SUBSET SELECTION CARD(S) GIVES K, THE NUMBER OF COEFFICIENTS SOLVED
 C FOR, AND (ISAVE(J), J=1..K), WHICH CONTAINS THE TIDAL CONSTITUENTS SOLVED FOR.
 C THE TABLE BELOW GIVES THE TIDAL CONSTITUENTS AND THEIR ISAVE(J) VALUES.

L	M	P	Q	TIDE	DIS.BODY	ISAVE(J)	VALUES
2	1	0	-1		MOON	1	AND 2
2	1	0	0	01	MOON	3	AND 4
2	1	0	1		MOON	5	AND 6
2	1	1	-1		MOON	7	AND 8
2	1	1	0	K1	MOON+SUN	9	AND 10
2	1	1	1		MOON	11	AND 12
2	1	2	-1		MOON	13	AND 14
2	1	2	0		MOON	15	AND 16
2	1	2	1		MOON	17	AND 18
2	2	0	-1		MOON	19	AND 20
2	2	0	0	M2	MOON	21	AND 22
2	2	0	1		MOON	23	AND 24
2	2	1	-1		MOON	25	AND 26
2	2	1	0	K2	MOON+SUN	27	AND 28
2	2	1	1		MOON	29	AND 30
2	2	2	-1		MOON	31	AND 32
2	2	2	0		MOON	33	AND 34
2	2	2	1		MOON	35	AND 36
2	1	0	-1		SUN	37	AND 38
2	1	0	0	P1	SUN	39	AND 40
2	1	0	1		SUN	41	AND 42
2	1	1	-1		SUN	43	AND 44
2	1	1	0	K1S	SUN	-	
2	1	1	1		SUN	45	AND 46
2	1	2	-1		SUN	47	AND 48
2	1	2	0		SUN	49	AND 50
2	1	2	1		SUN	51	AND 52
2	2	0	-1		SUN	53	AND 54
2	2	0	0	S2	SUN	55	AND 56
2	2	0	1		SUN	57	AND 58
2	2	1	-1		SUN	59	AND 60
2	2	1	0	K2S	SUN	-	
2	2	1	1		SUN	61	AND 62
2	2	2	-1		SUN	63	AND 64
2	2	2	0		SUN	65	AND 66
2	2	2	1		SUN	67	AND 68

C
 C EACH CONSTITUENT HAS TWO ISAVE(J) VALUES, SINCE WE SOLVE FOR TWO
 C PARAMETERS - A LOVE NUMBER AND A LAG ANGLE. IF WE WISH TO SOLVE FOR ONLY A
 C LOVE NUMBER (FORCING THE LAG ANGLE TO BE ZERO), THEN ONLY THE FIRST ISAVE(J)
 C VALUE OF THAT CONSTITUENT SHOULD APPEAR ON THE SUBSET SELECTION CARD.

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C
C THE FOLLOWING DIMENSIONS MUST BE GREATER THAN OR EQUAL TO THE NUMBER OF
C VARIABLES, M
C
ISN 0003      DIMENSION XBAR(70),STD(70),D(70),RY(70),ISAVE(70),V(70),
C           1,SB(70),T(70),W(70)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO THE PRODUCT OF M*M
ISN 0004      DIMENSION RX(4900)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO (M+1)*M/2
ISN 0005      DIMENSION R(2300)
C THE FOLLOWING DIMENSION MUST BE GREATER THAN OR EQUAL TO 10
ISN 0006      DIMENSION ANS(10)
ISN 0007      DIMENSION VV(70),VF(70)
ISN 0008      COMMON/BLKG/C,A1,B,GLP0M,GLPQS,INDEX
ISN 0009      COMMON/BLKF/VV,VE,ANS,TSAVE,M,K
ISN 0010      1 FORMAT (A4,A2,I5,2I2)
ISN 0011      2 FORMAT (1H1,*MULTIPLE REGRESSION*,5X,A4,A2//,6X,*SELECTION*,12,/)
ISN 0012      3 FORMAT (1H0,*VARIABLE*,5X,*MEAN*,5X,*STANDARD*,6X,*CORRELATION*,
C           1,4X,*REGRESSION*,4X,*STD. ERROR*,5X,*COMPUTED*,/,*,NL*,18X,
C           2*DEVIATION*,7X,*X VS. Y*,7X,*COEFFICIENT*,3X,*OF REG.COEF*,3X,*T
C           3VALUE*)
ISN 0013      4 FORMAT (1H ,I4,6F14.5)
ISN 0014      5 FORMAT (1H ,*DEPENDENT*)
ISN 0015      6 FORMAT (1H0/,1H ,*INTERCEPT*,10X,F16.5,/,1H ,*MULTIPLE CORRELATI
C           10N*,F15.5,/,1H ,*STD. ERROR OF ESTIMATE*,F13.5,/,)
ISN 0016      7 FORMAT (1H0,2IX,*ANALYSIS OF VARIANCE FOR THE REGRESSION*,//,5X,
C           1,*SOURCE OF VARIATION*,7X,*DEGREES*,7X,*SUM CF*,10X,*MEAN*,12X,
C           2,*F VALUE*,/,30X,*CF FREEDOM*,4X,*SQUARES*,9X,*SQUARE*)
ISN 0017      8 FORMAT (1H ,*ATTRIBUTABLE TO REGRESSION*,4X,15,F16.5,/,1H ,
C           1,*DEVIATION FROM REGRESSION*,4X,15,2F16.5)
ISN 0018      9 FORMAT (1H ,5X,*TOTAL*,19X,I5,F16.5)
ISN 0019      10 FORMAT (36I2)
ISN 0020      11 FORMAT (1H ,15X,*TABLE OF RESIDUALS*,//,1H ,*CASE NO.,*X,*Y VALUE
C           1*,5X,*ESTIMATE*,5X,*RESIDUAL*)
ISN 0021      12 FORMAT (1H ,I6,F15.5,2F14.5)
ISN 0022      13 FORMAT (1H1,*NUMBER OF SELECTIONS NOT SPECIFIED. JOB TERMINATED*)
ISN 0023      14 FORMAT (1H0,*THE MATRIX IS SINGULAR. THIS SELECTION IS SKIPPED*)
ISN 0024      15 FORMAT (10X,7E10.3)
C READ THE PROBLEM PARAMETER CARD
C
C PR,PR1 - ALPHANUMERIC NAME OF SATELLITE
C N - NUMBER OF OBSERVATIONS
C M - NUMBER OF VARIABLES
C NS - NUMBER OF SELECTIONS
C
ISN 0025      100 READ (5,1,END=300)PR,PR1,N,M,NS
ISN 0026      101=0
ISN 0027      102=0
ISN 0028      103=M-1
ISN 0029      104 DO 30 J=1,MV
ISN 0030      30 VV(J4)=0.0
ISN 0031      CALL COFF (N,M,1D,X,XBAR,STD,RX,R,D,V,T)
C TEST NUMBER OF SELECTIONS
ISN 0032      105 IF (NS) 108,109,109
ISN 0033      108 WRITE (6,13)
ISN 0034      109 GO TO 103
ISN 0035      109 DO 200 I=1,NS
ISN 0036      200 WRITE (6,2) PR,PR1,I
C READ SUBSET SELECTION CARD
C
C K - NUMBER OF INDEPENDENT VARIABLES INCLUDED
C ISAVE - A VECTOR CONTAINING THE INDEPENDENT VARIABLES INCLUDED
C
ISN 0037      READ (5,17) K,(ISAVE(J), J=1,K)
C NDEP - INDEPENDENT VARIABLE
ISN 0038      NDEP=69
ISN 0039      CALL UPER(M,5,NDEP,K,ISAVE,RX,RY)
ISN 0040      CALL MINV (RX,K,DET,V,T)
C TEST SINGULARITY OF THE MATRIX INVERTED
ISN 0041      110 IF (DET) 112,110,112
ISN 0042      110 WRITE (6,14)
ISN 0043      110 GO TO 200
ISN 0044      112 CALL MULTR (N,K,XBAR,STD,D,PR,RY,ISAVE,V,SH,T,ANS)
C PRINT MEANS, STANDARD DEVIATIONS, INTERCORRELATIONS BETWEEN X AND Y,
C REGRESSION COEFFICIENTS, STANDARD DEVIATIONS OF REGRESSION COEFFICIENTS, AND
C COMPUTED T-VALUES
ISN 0045      113 MMEK + 1
ISN 0046      113 WRITE (6,3)

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ISN 0047      DO 115 J=1,K
ISN 0048      L=ISAVE(J)
ISN 0049      C SAVE REGRESSION COEFFICIENTS AND THEIR ERRORS FOR SUBROUTINE LOVNUM
ISN 0050      VV(L)=V(J)
ISN 0051      VEL(L)=SB(J)
ISN 0052      115  WRITE (6,4) L,XBAR(L),STD(L),RY(J),V(J),SB(J),T(J)
ISN 0053      L=ISAVE(MM)
ISN 0054      #RITE (6,4) L,XBAR(L),STD(L)
ISN 0055      C PRINT INTERCEPT, MULTIPLE CORRELATION COEFFICIENT, AND STANDARD ERROR OF
C ESTIMATE
ISN 0056      #RITE (6,6) ANS(1),ANS(2),ANS(3)
ISN 0057      C PRINT ANALYSIS OF VARIANCE FOR THE REGRESSION
ISN 0058      #RITE (6,7)
ISN 0059      L=ANS(8)
ISN 0060      #RITE (6,8) K,ANS(4),ANS(6),ANS(10),L,ANS(7),ANS(9)
ISN 0061      L=N - 1
ISN 0062      SUM=ANS(4) + ANS(7)
ISN 0063      #RITE (6,9) L,SUM
ISN 0064      C CALL SUBROUTINE LOVNUM
ISN 0065      CALL LOVNUM(MT)
ISN 0066      200  CONTINUE
ISN 0067      GO TO 100
ISN 0068      300  CONTINUE
ISN 0069      RETURN
ISN 0070      END

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ISN 0032

SUBROUTINE THEORY (JPLOT,MT)

C
 C THIS SUBROUTINE COMPUTES THE PERIODS AND AMPLITUDES OF THE CONSTITUENT
 C TIDES OF THE TIP FOR THE SOLID EARTH, GIVEN THE SOLID EARTH LOVE NUMBER. THE
 C LAG ANGLE IS ASSUMED TO BE ZERO HERE. IT ALSO PLOTS THE RESULTING TIP AS A
 C SAMPLE PLOT IF DESIRED (JPLOT=1 IF YES, 0 IF NO).
 C NOTE LUNISOLAR TIDES K1 AND K2 ARE LUMPED IN WITH THE LUNAR TIDES.
 C
 C NOTATION
 C PERDM(L4,LP,LQ) - PERIOD OF LUNAR CONSTITUENT LM,LP,LQ
 C PERDS(LM,LP,LQ) - PERIOD OF SOLAR CONSTITUENT LM,LP,LQ
 C XM0UN(L4,LP,LQ) - AMPLITUDE OF LUNAR CONSTITUENT LM,LP,LQ IN ARCSECONDS
 C XSUN(LM,LP,LQ) - AMPLITUDE OF SOLAR CONSTITUENT LM,LP,LQ IN ARCSECONDS
 C
 ISN 0003 IMPLICIT REAL*8(A-H,O-Z)
 ISN 0004 DIMENSION EPSLM(2,3,3),EPSLNS(2,3,3),ARGUM(2,3,3),ARGUS(2,3,3),
 1 ARGDTM(2,3,3),ARGDTS(2,3,3)
 ISN 0005 DIMENSION B1(2),XMOON(2,3,3),XSUN(2,3,3),YKM(2,3,3),YKE(2,3,3)
 ISN 0006 DIMENION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
 ISN 0007 DIMENSION C(2,3),A1(2,3),B(2,3),GLPGM(3,3),GLPQS(3,3)
 ISN 0008 DIMENSION TIDE(2,3,3)
 ISN 0009 DIMENSION SAT(14)
 ISN 0010 DIMENSION PERDM(2,3,3),PERDS(2,3,3)
 ISN 0011 COMMON/BLKA/EPISNM,EPISLNS,ARGUM,ARGUS,ARGDTM,ARGDTS
 ISN 0012 COMMON/BLKB/B1,XX,CFNTM,CFNTS,EUM,XM0UN,XSUN,YKM,YKS,XKP
 ISN 0013 COMMON/BLKC/TE,M,XIEXP,T,XINCL,NTRACK
 ISN 0014 COMMON/BLKD/XLAG,Q,OMEGAM,DELMN,CMEGAS,DELSUN,SS,XIC,A,E,XI,XNCDT,
 1 TZERO,XM0UN,XISUN,TMS,XNDM,YNDS,F,XMEAN,XMEANS,XNCDTM,XMDOTS,
 2 OMGDCT,MEXP
 ISN 0015 COMMON/BLKG/C,A1,B,GLPQM,GLPQS,INDEX
 ISN 0016 COMMON/BLKI/SAT
 ISN 0017 DATA BLANK/4F/
 ISN 0018 DATA TM112,TM122,TM212,TM222/4H01 ,4HK1 ,4HM2 ,4HK2 /
 ISN 0019 DATA TS112,TS122,TS212,TS222/4H01 ,4HK15 ,4HS2 ,4HK35 /
 ISN 0020 PI=3.1415926535890
 C FIND THE LARGEST AMPLITUDE OF ALL THE CONSTITUENTS (IGNORING ANY CONSTITUENT
 C WITH A PERIOD LONGER THAN 2000 DAYS. THE 2000 IS AN ARBITRARY FIGURE.)
 ISN 0021 XMAX=0.0
 ISN 0022 DO 50 LM=1,2
 ISN 0023 YLM=LM
 ISN 0024 DO 50 LP=1,3
 ISN 0025 DO 50 LQ=1,3
 ISN 0026 YKMLM,LP,LQ)=XX
 ISN 0027 YKS(LM,LP,LQ)=XX
 ISN 0028 XM0UN(LM,LP,LQ)=YKM(LM,LP,LQ)*CFNTM*B1(LM)*C(LM,2)*A1(LM,LP)*
 1 GLPGM(LP,LQ)*YLM/(ARGDTM(L4,LP,LQ)*SS)
 ISN 0029 XM0UN(LM,LP,LQ)=DABS(XM0UN(LM,LP,LQ))
 ISN 0030 PERDM(LM,LP,LQ)=2.0*PI/(ARGDTM(LM,LP,LQ))
 ISN 0031 PERDS(LM,LP,LQ)=DABS(PERDM(LM,LP,LQ))
 ISN 0032 XSUN(LM,LP,LQ)=YKS(LM,LP,LQ)*CFNTS*A1(LM)*C(LM,2)*E(LM,LP)*
 1 GLPQS(LP,LQ)*YLM/(ARGDTS(LM,LP,LQ)*SS)
 ISN 0033 XSUN(LM,LP,LQ)=CABS(XSUN(LM,LP,LQ))
 C TAKE CARE OF THE LUNISOLAR CASE
 ISN 0034 IF (LP .EQ. 2 .AND. LQ .EQ. 2) XM0UN(LM,LP,LQ)=XN0UN(LM,LP,LQ) +
 1 XSUN(LM,LP,LQ)
 ISN 0035 PERDS(LM,LP,LQ)=2.0*PI/(ARGDTS(LM,LP,LQ))
 ISN 0036 PERDS(LM,LP,LQ)=DABS(PERDS(LM,LP,LQ))
 ISN 0037 PER=PERDM(LM,LP,LQ)
 ISN 0038 IF (PER-2000.0) 54,64,62
 ISN 0039 54 CONTINUE
 ISN 0040 IF (XMCN(LM,LP,LQ)-XMAX) 62,62,63
 ISN 0041 ISN 0042 63 XMAX=XM0UN(LM,LP,LQ)
 ISN 0043 62 CONTINUE
 ISN 0044 PER=PERDS(LM,LP,LQ)
 ISN 0045 IF (PER - 2000.0) 55,65,66
 ISN 0046 55 CONTINUE
 ISN 0047 IF (XSUN(LM,LP,LQ) - XMAX) 66,65,67
 ISN 0048 57 XMAX=XSUN(LM,LP,LQ)
 ISN 0049 65 CONTINUE
 ISN 0050 60 CONTINUE
 ISN 0051 3 WRITE (6,3)
 ISN 0052 3 FORMAT (1H1,///)
 ISN 0053 WRITE (6,1)
 C DO THE LUNAR TIDES
 C PRINT OUT L,M,P,Q, CONSTITUENT NAME, DISTURBING BODY, AMPLITUDE IN ARCSEC.

ORIGINAL PAGE IS
OF POOR QUALITY

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ISN 0054      C PERIOD IN DAYS, PER CENT OF LARGEST CONSTITUENT, AND ISAVE(J) VALUES
1   FORMAT (* L M P Q   TIDE  DIS.BODY   AMPLITUDE   PERIOD
1   PER CENT  ISAVE(J) (FOR USE IN SUBROUTINE REGRES)
ISN 0055      1 WRITE (5,2)
ISN 0056      2 FORMAT (32X, *(ARCSEC)*,10X,*(DAYS)*,/)
ISN 0057      DO 39 LM=1,2
ISN 0058      DO 89 LP=1,3
ISN 0059      DO 89 LQ=1,3
ISN 0060      89 TIDE(LM,LP,LQ)=BLANK
ISN 0061      TIDE(1,1,2)=TM112
ISN 0062      TIDE(1,2,2)=TM122
ISN 0063      TIDE(2,1,2)=TM212
ISN 0064      TIDE(2,2,2)=TM222
ISN 0065      LLL=2
ISN 0066      I=0
ISN 0067      DO 70 LM=1,2
ISN 0068      DO 70 LP=1,3
ISN 0069      LPP=LP - 1
ISN 0070      DO 70 LQ=1,3
ISN 0071      LQQ=LQ - 2
ISN 0072      AMP=(XMOON(LM,LP,LQ)/XMAX)*100.0
ISN 0073      I=I + 1
ISN 0074      I3=I
ISN 0075      I=I+1
ISN 0076      IF (LPP .EQ. 1 .AND. LQQ .EQ. 0) GO TO 71
ISN 0077      WRITE (5,5) LLL,LM,LPP,LQQ,TIDE(LM,LP,LQ),XMCN(LM,LP,LQ),
1   PEROM(LM,LP,LQ),AMP,13,I
ISN 0078      5   FORMAT (4I2,3X,A4,5X,*MOON*.5X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1   * AND *,12)
ISN 0079      GO TO 70
ISN 0080      71  WRITE (5,6) LLL,LM,LPP,LQQ,TIDE(LM,LP,LQ),XMCN(LM,LP,LQ),
1   PEROM(LM,LP,LQ),AMP,13,I
ISN 0081      6   FORMAT (4I2,3X,A4,3X,*MOON+EUN*.3X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1   * AND *,12)
ISN 0082      70  CONTINUE
ISN 0083      WRITE (5,4)
ISN 0084      4   FORMAT (10X,/)
ISN 0085      C DO THE SOLAR TIDES
C PRINT OUT L,M,P,Q CONSTITUENT NAME, DISTURBING BODY, AMPLITUDE IN ARCSEC.
C PERIOD IN DAYS, PER CENT OF LARGEST CONSTITUENT, AND ISAVE(J) VALUES
ISN 0086      DO 38 LM=1,2
ISN 0087      DO 38 LP=1,3
ISN 0088      DO 38 LQ=1,3
ISN 0089      88  TIDE(LM,LP,LQ)=BLANK
ISN 0090      TIDE(1,1,2)=TS112
ISN 0091      TIDE(1,2,2)=TS122
ISN 0092      TIDE(2,1,2)=TS212
ISN 0093      TIDE(2,2,2)=TS222
ISN 0094      DO 80 LM=1,2
ISN 0095      DO 80 LP=1,3
ISN 0096      LPP=LP - 1
ISN 0097      DO 80 LQ=1,3
ISN 0098      LQQ=LQ - 2
ISN 0099      AMP=(XSUN(LM,LP,LQ)/XMAX)*100.0
ISN 0100      IF (LPP .EQ. 1 .AND. LQQ .EQ. 0) GO TO 81
ISN 0102      I=I + 1
ISN 0103      I3=I
ISN 0104      I=I + 1
ISN 0105      WRITE (6,7) LLL,LM,LPP,LQQ,TIDE(LM,LP,LQ),XSUN(LM,LP,LQ),
1   PEROS(LM,LP,LQ),AMP,13,I
ISN 0106      7   FORMAT (4I2,3X,A4,5X,*SUN*.6X,D13.6,3X,F10.3,3X,F10.3,4X,I2,
1   * AND *,12)
ISN 0107      GO TO 80
ISN 0108      81  WRITE (6,8) LLL,LM,LPP,LQQ,TIDE(LM,LP,LQ)
ISN 0109      8   FORMAT (4I2,3X,A4,5X,*SUN*.10X,***,14X,***,11X,***,5X,***)
ISN 0110      80  CONTINUE
ISN 0111      WRITE (6,20) XK
ISN 0112      20  FORMAT (/////*10X,*THEORETICAL AMPLITUDES ASSUMING SOLID EARTH L0V
1E NUMBER K2 = *F7.3)
ISN 0113      WRITE (6,21) (SAT(J), J=1,14)
ISN 0114      21  FORMAT (/////*10X,13A6,A2)
C PRINT OUT A PLOT OF THE SOLID EARTH TIP (IF JPLOT=1)
ISN 0115      IF (JPLOT .EQ. 1) GO TO 83
ISN 0116      GO TO 12
ISN 0117      83  CONTINUE
ISN 0118      DO 10 L=1,MT
ISN 0119      TT=T(L)
ISN 0120      CALL ARG(TT)
ISN 0121      SUM=0.0
ISN 0122      DO 90 LM=1,2

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ISN 0124      YLM=LM
ISN 0125      DO 30 LP=1,3
ISN 0126      DO 30 LO=1,3
ISN 0127      XMOON(LM,LP,LO)=YKM(LM,LP,LO)*CFNTM*B1(LM)+C(LM,2)+A1(LM,LP)*GLPQM
ISN 0128      1(LP,LO)*YLM*ARGUM(LM,LP,LO)/(ARGCTM(LM,LP,LO)*SS)
ISN 0129      XSUNLEM,LP,L CT=YKS(LM,LP,LO)*CFNTS*B1(LM)*C(LM,2)+E(LM,LP)*GLPOS(L
ISN 0130      1P,LO)*YLM*ARGUS(LM,LP,LO)/(ARGCTS(LM,LP,LO)*SS)
ISN 0131      90  CONTINUE
ISN 0132      10  CONTINUE
ISN 0133      CALL PLOTER (MT,MEXP)
ISN 0134      12  CONTINUE
ISN 0135      RETURN
ISN 0136      END

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ISN 0002      SUBROUTINE TIME1(TSTART,TEND,DT,M)
C
C      THIS SUBROUTINE FILLS IN THE VALUES OF ARRAY T(L), BY KNOWING THE STARTING
C      TIME (TSTART), THE ENDING TIME (TEND), AND THE TIME INTERVAL BETWEEN
C      POINTS (DT).
C
C      IMPLICIT REAL*8 (A-H,O-Z)
ISN 0003      DIMENSION TEXP(200),XIEXP(200),T(700),XINCL(700),NTRACK(700)
ISN 0004      COMMON/BLKC/TEXP,XIEXP,T,XINCL,NTRACK
ISN 0005      M=(TEND-TSTART)/DT + 1.1D0
ISN 0006      12  L=1,M
ISN 0007      DO 12 L=1,M
ISN 0008      XM=L-1
ISN 0009      12  T(L)=TSTART + XM*DT
ISN 0010      RETURN
ISN 0011      END

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SATELLITE GEOS - 1 , 1966-1967 DATA

SATELLITE DATA

A (10 ⁴ *E CM)	E	INCLINATION (DEGREES)	NODE RATE (DEG/DAY)	TZERO (DAYS)	NODE (DEGREES)
8.0729	0.0726	59.3805	-2.2465	38.5000	-109.0820

MOON AND SUN DATA

OMEGA (DEGREES)	DELTA (DEGREES)	INCLINATION (DEGREES)	TMS (DAYS)	MEAN ANOMALY (DEGREES)	MEAN MOTION (DEG/CAY)	NODE RATE (DEG/DAY)
10.1770	105.9932	27.2032	35.0000	331.5588	13.1839	-0.0082
SUN	0.0	313.7153	23.4432	35.0000	31.3590	0.9856

TSTART= 37.0000 TEND= 665.0000 DT= 2.0000 (DAYS)

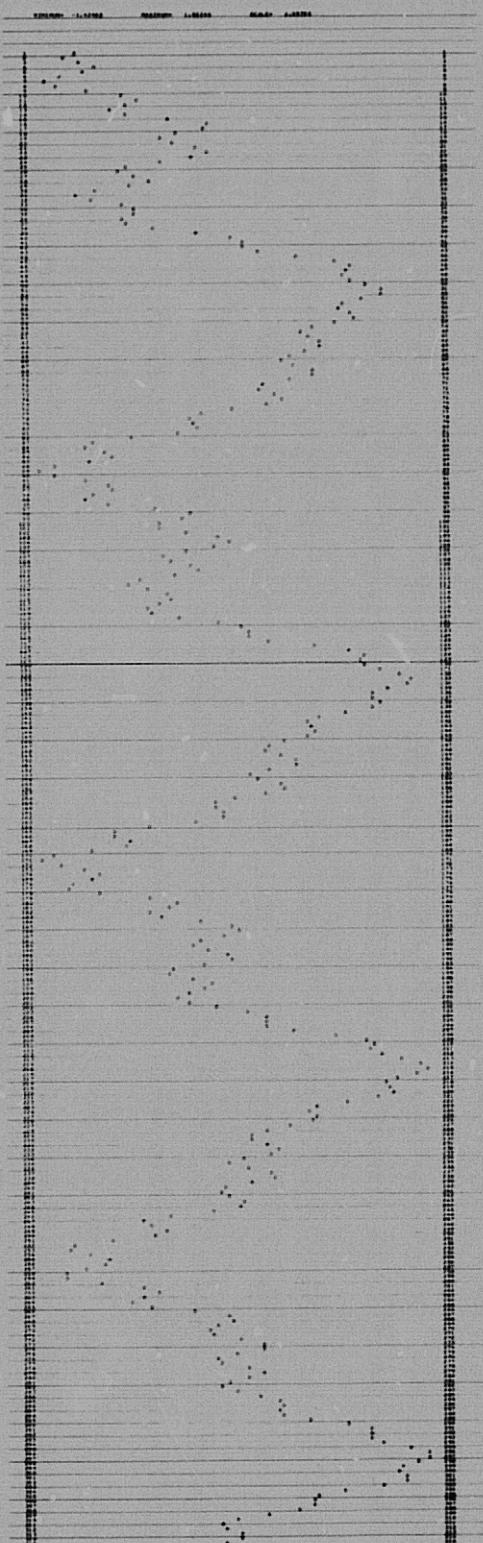
SOLID EARTH LOVE NUMBER= 0.3000 LOAD DEFORMATION COEFFICIENT= -0.3000

SOLID EARTH LAG ANGLE= 0.0 DEGREES

L-M-P-Q	TIDE	DIS-BODY	AMPLITUDE (ARCSEC)	PERIOD (DAYS)	PER CENT	ISAVE(J) (FOR USE IN SUBROUTINE REGRES)
2 1 0 -1		MOON	0.272512D-02	23.164	0.298	1 AND 2
2 1 0 0	C1	MOON	0.539345D-01	12.565	5.894	3 AND 4
2 1 0 1		MOON	0.711427D-02	8.239	3.777	5 AND 6
2 1 1 -1		MOON	0.110481D-01	33.251	1.207	7 AND 8
2 1 1 0	K1	MOON+SUN	0.915673D-00	150.830	100.000	9 AND 10
2 1 1 1		MOON	0.781613D-02	23.524	0.854	11 AND 12
2 1 1 2		MOON	0.466753D-01	7.673	0.051	13 AND 14
2 1 2 0		MOON	0.374469D-02	14.920	0.409	15 AND 16
2 1 2 1		MOON	0.224170D-03	32.537	0.024	17 AND 18
2 2 0 -1		MOON	0.831541D-02	20.243	0.909	19 AND 20
2 2 0 0	M2	MOON	0.174615D-00	11.571	19.082	21 AND 22
2 2 0 1		MOON	0.235691D-01	8.199	2.576	23 AND 24
2 2 1 -1		MOON	0.604583D-02	41.913	0.661	25 AND 26
2 2 1 0	K2	MOON+SUN	0.180663D-00	80.415	20.727	27 AND 28
2 2 1 1		MOON	0.296153D-02	20.522	0.324	29 AND 30
2 2 1 2		MOON	0.101643D-01	10.293	0.011	31 AND 32
2 2 2 0		MOON	0.343882D-03	15.445	0.092	33 AND 34
2 2 2 1		MOON	0.574525D-04	40.789	0.006	35 AND 36
1 0 -1		SUN	0.161423D-02	111.378	0.176	37 AND 38
1 0 0	P1	SUN	0.143147D-00	95.352	15.100	39 AND 40
1 0 1		SUN	0.701930D-02	69.183	0.767	41 AND 42
1 1 -1		SUN	0.113752D-01	245.502	1.298	43 AND 44
1 1 0	K1S	SUN	0.000000D+00	0.000	0.000	45 AND 46
1 1 1		SUN	0.463433D-02	111.381	0.506	47 AND 48
1 1 2		SUN	0.221337D-02	506.782	0.242	49 AND 50
1 2 -1		SUN	0.977311D-01	1307.942	15.680	51 AND 52
1 2 0	K2	SUN	0.178149D-03	285.524	0.019	53 AND 54
1 2 1		SUN	0.387753D-02	55.728	0.424	55 AND 56
2 0 0	S2	SUN	0.393573D-00	95.690	43.010	57 AND 58
2 0 1		SUN	0.199612D-01	48.322	2.181	59 AND 60
2 1 0	K2S	SUN	0.156445D-02	172.638	0.171	61 AND 62
2 1 1		SUN	0.160157D-02	65.703	0.109	63 AND 64
2 1 2		SUN	0.179401D-03	234.248	0.020	65 AND 66
2 2 0		SUN	0.186972D-02	142.756	0.204	67 AND 68
2 2 1		SUN	0.112250D-04	102.641	0.001	

THEORETICAL AMPLITUDES ASSUMING SOLID EARTH LOVE NUMBER K2 = 0.300

CEOS - 1 • 1966-1967 DATA



SATELLITE TRACKING DATA

(142 DATA POINTS, TODAY= 38.5000 DAYS)

TIME (DAYS)	INCLINATION (ARCSEC)	TIME (DAYS)	INCLINATION (ARCSEC)		
1	38.5000	-1.1304	59	317.5000	0.1680
2	51.5000	-0.4971	60	321.5000	0.4834
3	53.5000	-0.5935	61	325.5000	0.0566
4	62.5000	-0.6999	62	329.5000	0.1476
5	64.5000	-0.2256	63	333.5000	-0.0505
6	66.5000	0.0125	64	337.5000	0.3736
7	68.5000	-0.1665	65	341.5000	-0.0295
8	71.5000	-0.3124	66	345.5000	0.2167
9	86.5000	-0.7062	67	349.5000	0.1344
10	93.5000	-0.6174	68	351.5000	-0.1005
11	94.5000	-0.7184	69	359.5000	-0.2389
12	93.5000	-0.8416	70	363.5000	-0.7592
13	102.5000	-0.5733	71	367.5000	-0.9170
14	106.5000	-0.0051	72	371.5000	-0.7586
15	110.5000	-0.4471	73	373.5000	-0.6970
16	114.5000	0.1713	74	377.5000	-1.3979
17	118.5000	0.3472	75	381.5000	-0.8792
18	122.5000	0.3373	76	385.5000	-1.0307
19	126.5000	0.8694	77	389.5000	-1.0985
20	135.5000	0.6427	78	393.5250	-0.3036
21	134.5000	1.0141	79	397.5000	-0.3920
22	139.5000	0.6940	80	401.5000	-0.2335
23	143.5000	0.7383	81	405.5000	-0.1777
24	147.5000	0.7650	82	409.5000	-0.0055
25	151.5000	0.6338	83	413.5000	-0.3649
26	155.5000	0.3560	84	417.5000	-0.2518
27	157.5000	0.6396	85	421.5000	-0.2334
28	161.3750	0.3583	86	425.5000	-0.3919
29	163.5000	0.4173	87	430.5000	-0.1351
30	173.5000	0.6453	88	434.5000	-0.5187
31	175.5000	0.4152	89	438.5000	-0.2887
32	187.5000	0.3485	90	442.5000	0.1284
33	184.5000	0.2226	91	446.5000	0.0345
34	188.5000	-0.1093	92	450.5000	0.7752
35	192.5000	-0.1424	93	454.5000	1.1467
36	196.5000	-0.3616	94	458.5000	0.8060
37	200.5000	-0.7914	95	462.5000	1.2743
38	204.5000	-0.8355	96	466.5000	1.1251
39	207.5000	-0.8143	97	470.5000	0.9267
40	211.5000	-0.4939	98	474.5000	0.8581
41	214.5000	-1.1035	99	478.5000	0.7030
42	218.5000	-0.7275	100	482.5000	0.2595
43	221.5000	-0.7375	101	486.5000	0.3372
44	225.5000	-0.6962	102	490.5000	-0.1988
45	230.5000	-0.3615	103	494.5000	-0.2286
46	234.5000	-0.2757	104	498.5000	0.1401
47	270.5000	-0.5275	105	507.5000	0.0271
48	271.5000	-0.6399	106	521.5000	-0.0057
49	277.5000	-0.6509	107	525.5000	-0.3877
50	281.5000	-0.0321	108	529.5000	-0.5373
51	286.5000	0.6249	109	531.5000	-0.6423
52	289.5000	0.8206	110	537.5000	-0.7491
53	293.5000	1.0013	111	541.5000	-1.1932
54	297.5000	0.8364	112	545.5000	-0.8495
55	301.5000	1.2144	113	549.5000	-0.6622
56	305.5000	0.9345	114	553.5000	-0.9727
57	310.5000	0.6565	115	557.5000	-0.2525
58	317.5000	0.9481	116	561.5000	-0.6371

1.7	565.5000	-0.1555	130	615.5000	1.1740
118	569.5000	-0.0840	131	619.5000	1.0720
119	573.5000	0.0910	132	625.5000	1.1437
120	577.5000	0.2459	133	629.5000	1.2924
121	581.5000	0.0964	134	632.5000	0.9806
122	585.5250	0.0729	135	636.5000	1.2935
123	587.5000	-0.2413	136	640.5000	1.0124
124	593.5000	0.2322	137	644.5000	0.3505
125	597.5000	-0.3299	138	649.5000	0.3425
126	601.5000	0.1938	139	652.5000	-0.0373
127	605.5000	0.1958	140	656.5000	-0.2360
128	609.5000	0.3115	141	660.2500	-0.1557
129	613.6250	0.3361	142	664.5000	-0.1384

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SELECTION 1

VARIABLE NO.	MEAN	STANDARD DEVIATION	CORRELATION X VS. Y	REGRESSION COEFFICIENT	STD. ERROR OF REG. COEF.	COMPUTED T VALUE
5	0.11462	1.37594	0.47335	0.34098	0.00905	37.66267
10	-0.02424	1.48806	-0.06838	-0.01434	0.00369	-1.47252
27	0.02810	0.33258	0.19415	0.03944	0.05923	6.91445
28	-0.01233	0.33263	0.17832	0.03298	0.06033	0.04947
30	-0.03475	0.654410	0.00175	0.19384	0.05640	3.43657
40	-0.03306	0.355337	-0.10086	0.21203	0.05715	2.21044
55	-0.06401	0.92311	0.48564	0.35203	0.01326	19.59209
56	-0.02547	0.93516	-0.02670	-0.03784	0.01530	-2.47516
DEPENDENT 69	0.00114	0.65653				

INTERCEPT -0.02420

MULTIPLE CORRELATION 0.95554

STD. ERROR OF ESTIMATE 0.16796

ANALYSIS OF VARIANCE FOR THE REGRESSION

SOURCE OF VARIATION	DEGREES OF FREEDOM	SUM OF SQUARES	MEAN SQUARES	F. VALUE
ATTRIBUTABLE TO REGRESSION	8	36.8327	7.10478	251.83546
DEVIATION FROM REGRESSION	133	3.75220	0.02821	
TOTAL	141	30.59467		

*****FREQUENCY DEPENDENT LOVE NUMBERS*****
 (ASSUMING 2ND DEGREE TIDES ONLY)

*****OCEAN TIDE PARAMETERS*****
(ASSUMING 2ND DEGREE TIDES
ONLY AND SOLID EARTH LOVE
NUMBER K2=0.300 AND SOLID
EARTH TIDAL LAG=0.0 DEG)

TIDAL INCLINATION

TIME
(JAN 10 0 HRS UT = 1)

INCLINATION
(ARCSEC)

卷之三

0.370000	-0.844470	00	66	0.171000	02	0.412260	00
0.390000	-0.327220	00	69	0.173000	03	0.413360	00
0.410000	-0.237120	00	70	0.175000	03	0.417270	00
0.430000	-0.132230	01	71	0.177000	03	0.383960	00
0.450000	-0.132200	01	72	0.179000	03	0.351948D	00
0.470000	-0.121540	01	73	0.181000	03	0.313402D	00
0.490000	-0.097130	00	74	0.183000	03	0.252559D	00
0.500000	-0.061641D	00	75	0.185000	04	0.173100D	00
0.520000	-0.021763D	00	76	0.187000	05	0.123345D	-01
0.540000	-0.074490D	00	77	0.189000	06	0.2374D	-01
0.560000	-0.044293D	00	78	0.191000	03	0.1413300	00
0.580000	-0.031676D	03	80	0.195000	03	0.266340	00
0.600000	-0.041159D	00	81	0.197000	03	0.395240	00
0.620000	-0.032248D	00	82	0.199000	03	0.52372D	00
0.640000	-0.028412D	00	83	0.201000	03	0.64731D	00
0.660000	-0.017053D	00	84	0.203000	03	0.76157D	00
0.680000	-0.011531D	00	85	0.205000	03	0.82320D	00
0.700000	-0.080518D	-01	86	0.207000	03	0.94575D	20
0.720000	-0.057559D	-01	87	0.209000	03	0.10389D	01
0.740000	-0.076587D	-01	88	0.211000	03	0.10423D	01
0.770000	-0.10662D	00	89	0.213000	03	0.10556D	01
0.790000	-0.15558D	00	90	0.215000	03	0.10582D	01
0.810000	-0.22039D	00	91	0.217000	03	0.10727D	01
0.830000	-0.29712D	00	92	0.219000	03	0.107401D	00
0.850000	-0.31118D	00	93	0.221000	03	0.10204D	00
0.870000	-0.46753D	00	94	0.223000	03	0.11466D	00
0.900000	-0.55096D	00	95	0.225000	03	0.71590D	00
0.910000	-0.62625D	00	96	0.227000	03	0.10161D	00
0.930000	-0.63856D	00	97	0.229000	03	0.39366D	00
0.950000	-0.73351D	00	98	0.231000	03	0.39966D	00
0.970000	-0.75756D	00	99	0.233000	03	0.32418D	00
0.990000	-0.75734D	00	100	0.235000	03	0.22055D	00
0.100000	-0.77321D	00	101	0.237000	03	0.15251D	00
0.103000	-0.83231D	00	102	0.239000	02	0.10304D	00
0.105000	-0.60579D	00	103	0.241000	02	0.73567D	-01
0.107000	-0.50772D	00	104	0.243000	02	0.2816D	00
0.109000	-0.34897D	00	105	0.245000	03	0.76326D	-01
0.111000	-0.25154D	00	106	0.247000	03	0.10655D	00
0.113000	-0.12255D	00	107	0.249000	03	0.15292D	00
0.115000	-0.53996D	-01	108	0.251000	03	0.21198D	00
0.117000	-0.41236D	00	109	0.253000	03	0.27958D	00
0.119000	-0.35875D	00	110	0.255000	03	0.35102D	00
0.121000	-0.51671D	00	111	0.257000	03	0.42133D	00
0.123000	-0.55270D	00	112	0.259000	03	0.48349D	00
0.125000	-0.77053D	00	113	0.261000	03	0.5387D	00
0.127000	-0.56929D	00	114	0.263000	03	0.5766D	00
0.129000	-0.24602D	00	115	0.265000	02	0.59548D	00
0.131000	-0.22923D	00	116	0.267000	02	0.59249D	00
0.134000	-0.10286D	01	117	0.269000	03	0.56576D	00
0.135000	-0.10355D	01	118	0.271000	03	0.51456D	00
0.137000	-0.10211D	00	119	0.273000	03	0.43226D	00
0.139000	-0.098814D	00	120	0.275000	03	0.34132D	00
0.141000	-0.094538D	00	121	0.277000	03	0.22331D	00
0.143000	-0.088002D	00	122	0.279000	03	0.83774D	-01
0.145000	-0.071237D	00	123	0.281000	03	0.58119D	-01
0.147000	-0.074157D	00	124	0.283000	03	0.21237D	00
0.149000	-0.067091D	00	125	0.285000	03	0.36879D	00
0.151000	-0.060409D	00	126	0.287000	03	0.52201D	00
0.153000	-0.054410D	00	127	0.289000	03	0.66681D	00
0.155000	-0.04732D	00	128	0.291000	03	0.72831D	00
0.157000	-0.045244D	00	129	0.293000	03	0.10222D	00
0.159000	-0.042363D	00	130	0.295000	03	0.10050C	01
0.161000	-0.040328D	00	131	0.297000	03	0.10742D	01
0.163000	-0.037555D	00	132	0.299000	03	0.11181D	01
0.165000	-0.034863D	00	133	0.301000	03	0.11292D	01
0.167000	-0.030225D	00	134	0.303000	03	0.11987D	01

135	0.325000 03	0.124720 01	207	0.453000 03	0.802070 00
136	0.327000 03	0.478090 00	210	0.455000 03	0.222730 00
137	0.329000 03	0.395260 00	211	0.457000 03	0.192510 01
138	0.331000 03	0.303040 00	212	0.459000 03	0.110560 01
139	0.333000 03	0.795900 00	213	0.461000 03	0.116140 01
140	0.335000 03	0.604280 00	214	0.463000 03	0.119080 01
141	0.337000 03	0.514280 00	215	0.465000 03	0.119310 01
142	0.339000 03	0.427570 00	216	0.467000 03	0.116890 01
143	0.341000 03	0.351120 00	217	0.469000 03	0.111960 01
144	0.343000 03	0.237100 00	218	0.471000 03	0.104600 01
145	0.345000 03	0.236800 00	219	0.473000 03	0.957340 00
146	0.347000 03	0.209560 00	220	0.475000 03	0.851780 00
147	0.349000 03	0.177800 00	221	0.477000 03	0.738940 00
148	0.351000 03	0.157070 00	222	0.479000 03	0.614660 00
149	0.353000 03	0.156120 00	223	0.481000 03	0.492810 00
150	0.355000 03	0.172090 00	224	0.483000 03	0.375060 00
151	0.357000 03	0.131660 00	225	0.485000 03	0.265620 00
152	0.359000 03	0.171260 00	226	0.487000 03	0.168090 00
153	0.361000 03	0.197280 00	227	0.490000 03	0.352470-01
154	0.363000 03	0.196260 00	228	0.491000 03	0.189730-01
155	0.365000 03	0.185160 00	229	0.493000 03	-0.298480-01
156	0.367000 03	0.161460 00	230	0.495000 03	-0.613420-01
157	0.369000 03	0.123390 00	231	0.497000 03	-0.766120-01
158	0.371000 03	0.599700-01	232	0.499000 03	-0.776570-01
159	0.373000 03	0.116260-02	233	0.510000 03	-0.672480-01
160	0.375000 03	-0.721670-01	234	0.503000 03	-0.487600-01
161	0.377000 03	-0.178250 00	235	0.505000 03	-0.259780-01
162	0.379000 03	-0.284500 00	236	0.507000 03	-0.288060-02
163	0.381000 03	-0.397620 00	237	0.509000 03	0.165830-01
164	0.383000 03	-0.313780 00	238	0.511000 03	0.287140-01
165	0.385000 03	-0.628790 00	239	0.513000 03	0.302700-01
166	0.387000 03	-0.718390 00	240	0.515000 03	0.166480-01
167	0.389000 03	-0.638110 00	241	0.517000 03	-0.797220-02
168	0.371000 03	-0.442100 00	242	0.519000 03	-0.503200-01
169	0.373000 03	-0.993150 00	243	0.521000 03	-0.108980 00
170	0.375000 03	-0.134210-01	244	0.523000 03	-0.182370 00
171	0.377000 03	-0.106930 01	245	0.525000 03	-0.258820 00
172	0.379000 03	-0.107350 01	246	0.527000 03	-0.365600 00
173	0.381000 03	-0.105480 01	247	0.529000 03	-0.469340 00
174	0.383000 03	-0.101410 01	248	0.531000 03	-0.576120 00
175	0.385000 03	-0.953560 00	249	0.533000 03	-0.681710 00
176	0.387000 03	-0.375860 00	250	0.535000 03	-0.781780 00
177	0.389000 03	-0.784620 00	251	0.537000 03	-0.872120 00
178	0.391000 03	-0.684010 00	252	0.539000 03	-0.948860 00
179	0.393000 03	-0.378530 00	253	0.541000 03	-0.100860 01
180	0.395000 03	-0.472860 00	254	0.543000 03	-0.104890 01
181	0.397000 03	-0.715620 00	255	0.545000 03	-0.105770 01
182	0.399000 03	-0.278910 00	256	0.547000 03	-0.105430 01
183	0.401000 03	-0.198630 00	257	0.549000 03	-0.103990 01
184	0.403000 03	-0.133740 00	258	0.551000 03	-0.992480 00
185	0.405000 03	-0.463750-01	259	0.553000 03	-0.927160 00
186	0.407000 03	-0.577130-01	260	0.555000 03	-0.835810 00
187	0.409000 03	-0.478820-01	261	0.557000 03	-0.751960 00
188	0.411000 03	-0.559630-01	262	0.559000 03	-0.549670 00
189	0.413000 03	-0.903900 01	263	0.561000 03	-0.543290 00
190	0.415000 03	-0.117290 00	264	0.553000 03	-0.437250 00
191	0.417000 03	-0.154120 00	265	0.565000 03	-0.335910 00
192	0.419000 03	-0.216370 00	266	0.567000 03	-0.242890 00
193	0.421000 03	-0.269490 00	267	0.569000 03	-0.161840 00
194	0.423000 03	-0.318820 00	268	0.571000 03	-0.052690-01
195	0.425000 03	-0.359770 00	269	0.573000 03	-0.449260-01
196	0.427000 03	-0.383100 00	270	0.575000 03	-0.116100-01
197	0.429000 03	-0.400150 00	271	0.577000 03	-0.486970-02
198	0.431000 03	-0.392970 00	272	0.579000 03	0.567760-02
199	0.433000 03	-0.364580 00	273	0.581000 03	-0.710970-02
200	0.435000 03	-0.313970 00	274	0.583000 03	-0.306180-01
201	0.437000 03	-0.241260 00	275	0.585000 03	-0.613270-01
202	0.439000 03	-0.147650 00	276	0.587000 03	-0.252640-01
203	0.441000 03	-0.354170-01	277	0.589000 03	-0.128210 00
204	0.443000 03	-0.922150-01	278	0.591000 03	-0.155940 00
205	0.445000 03	-0.231200 00	279	0.593000 03	-0.174420 00
206	0.447000 03	-0.276850 00	280	0.595000 03	-0.130090 00
207	0.449000 03	-0.324060 00	281	0.597000 03	-0.170000 00
208	0.451000 03	-0.675740 00	282	0.599000 03	-0.142010 00

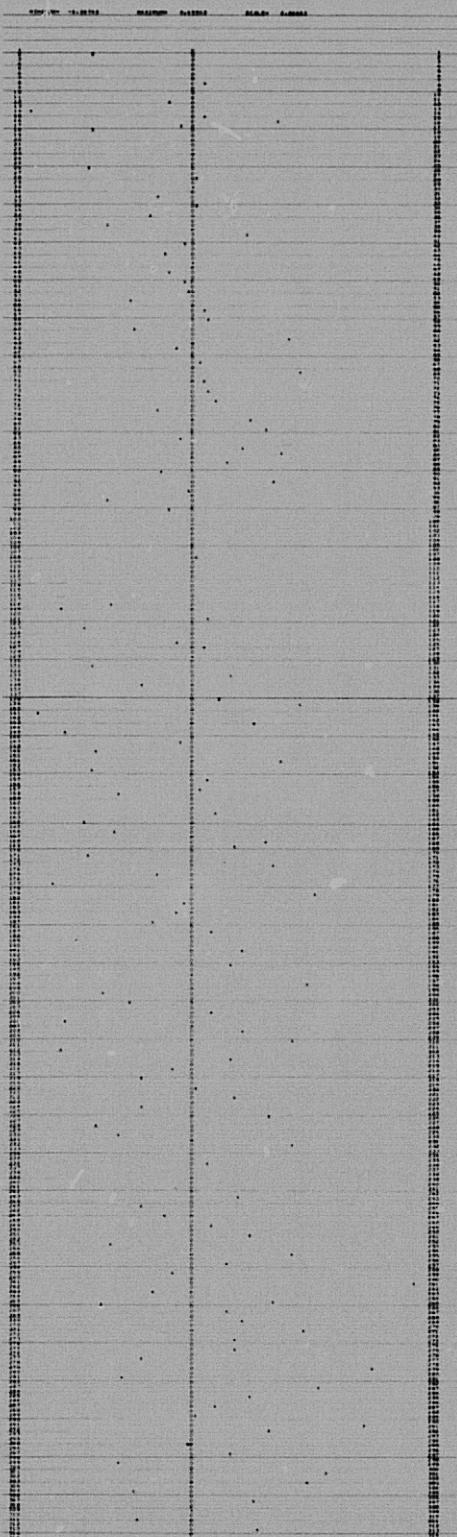
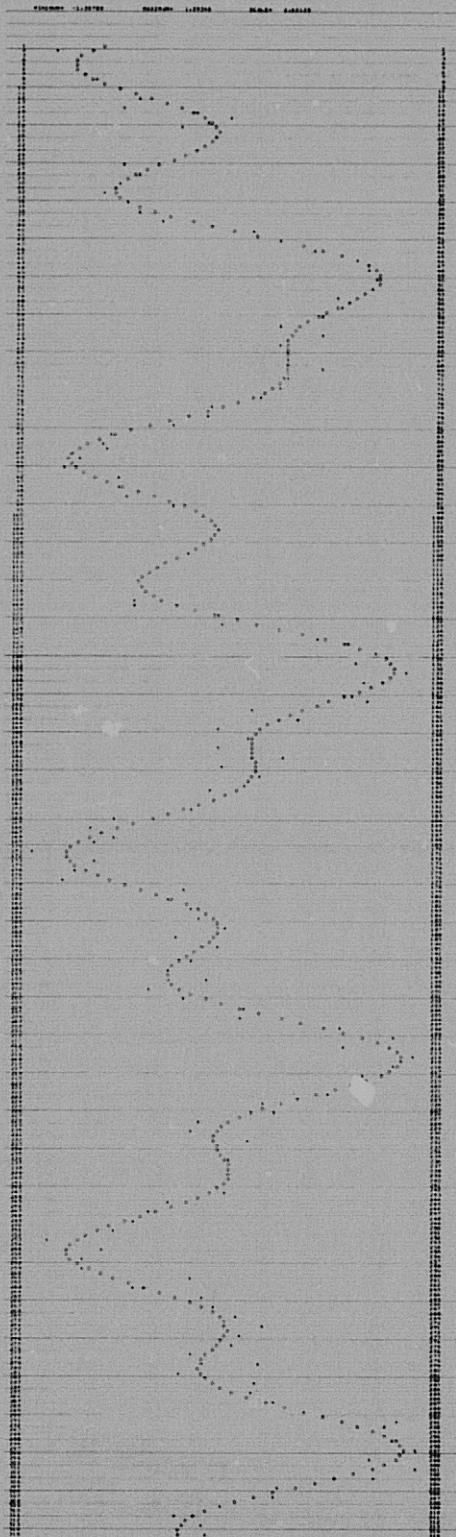
283	0.601000 03	-0.749110 -01	300	0.635000 01	0.103490 01
284	0.602000 03	-0.735140 -01	301	0.637000 03	0.094270 00
285	0.605000 03	0.593080 -01	302	0.639000 03	0.983820 00
286	0.607000 03	0.157680 00	303	0.641000 03	0.758320 00
287	0.609000 03	0.272750 00	304	0.643000 03	0.522370 00
288	0.611000 03	0.397840 00	305	0.645000 03	0.481370 00
289	0.613000 03	0.528510 00	306	0.647000 03	0.334660 00
290	0.615000 03	0.660240 00	307	0.649000 03	0.203170 00
291	0.617000 03	0.737690 00	308	0.651000 03	0.752870 -01
292	0.619000 03	0.905300 00	309	0.653000 03	0.369300 -01
293	0.621000 03	0.101000 01	310	0.655000 03	0.133200 00
294	0.623000 03	0.109580 01	311	0.657000 03	0.210170 00
295	0.625000 03	0.115950 01	312	0.659000 03	0.266510 00
296	0.627000 03	0.119820 01	313	0.661000 03	0.301980 00
297	0.629000 03	0.121030 01	314	0.663000 03	0.317380 00
298	0.631000 03	0.119500 01	315	0.665000 03	0.314540 00
299	0.633000 03	0.115270 01			

RESIDUALS

TIME (JAN 1, 0 HRS UT = 1)	RESIDUAL (ARCSEC)	TIME (JAN 1, 0 HRS UT = 1)	RESIDUAL (ARCSEC)	TIME (JAN 1, 0 HRS UT = 1)	RESIDUAL (ARCSEC)
1 0.385000 02	-0.250850 00	53 0.351500 C3	0.154650 00	101 0.342300 -01	0.734230 -01
2 0.515000 02	0.117330 -02	54 0.355800 C3	0.215430 00	102 0.152570 00	-0.152570 00
3 0.585000 02	-0.300580 -01	55 0.363500 C3	0.110340 00	103 0.144530 00	0.110340 00
4 0.625000 02	-0.343450 00	56 0.371500 C3	0.174400 00	104 0.174400 00	0.174400 00
5 0.645000 02	0.394330 -01	57 0.377500 C3	0.235410 00	105 0.235410 00	-0.235410 00
6 0.665000 02	0.199370 00	58 0.373500 C3	0.151370 -01	106 0.151370 -01	-0.151370 -01
7 0.685000 02	-0.193240 -01	59 0.377500 C3	0.234310 00	107 0.234310 00	0.241720 00
8 0.705000 02	-0.225220 00	60 0.381500 C3	0.525000 -01	108 0.525000 -01	-0.445360 -01
9 0.685000 02	-0.260290 00	61 0.385500 C3	0.100260 00	109 0.100260 00	0.282220 -01
10 0.695000 02	-0.932530 -02	62 0.389500 C3	0.258670 00	110 0.258670 00	-0.258670 00
11 0.645000 02	-0.147030 -01	63 0.393500 C3	3.125000 00	111 0.736610 -01	0.736610 -01
12 0.585000 02	-0.313480 -01	64 0.397500 C3	0.466630 -02	112 0.466630 -02	0.201560 00
13 0.122500 C3	0.243930 -01	65 0.401500 C3	0.183950 00	113 0.183950 00	-0.157700 00
14 0.105500 C3	-0.715630 -01	66 0.405500 C3	0.693040 -01	114 0.693040 -01	0.255560 00
15 0.110500 C3	-0.160050 00	67 0.409500 C3	0.142370 00	115 0.142370 00	0.245540 00
16 0.114500 C3	0.156870 00	68 0.413500 C3	0.278590 00	116 0.278590 00	0.832940 -01
17 0.118500 C3	0.158070 -01	69 0.417500 C3	5.227600 00	117 5.227600 00	-0.123390 00
18 0.122500 C3	-0.315480 -01	70 0.421500 C3	0.138150 00	118 0.138150 00	-0.212500 -01
19 0.126500 C3	0.220920 -01	71 0.425500 C3	0.577600 -01	119 0.577600 -01	-0.144360 00
20 0.130500 C3	-0.454010 -01	72 0.429500 C3	0.145240 00	120 0.145240 00	0.732760 00
21 0.134500 C3	-0.217670 -01	73 0.433500 C3	0.173590 00	121 0.173590 00	-0.218620 00
22 0.138500 C3	0.258520 -02	74 0.437500 C3	0.246450 -01	122 0.246450 -01	0.116310 00
23 0.143500 C3	-0.125370 00	75 0.441500 C3	0.116310 00	123 0.116310 00	-0.255610 -01
24 0.147500 C3	-0.412330 -01	76 0.445500 C3	0.413410 -01	124 0.413410 -01	-0.413410 -01
25 0.151500 C3	0.454250 -01	77 0.449500 C3	0.449500 -01	125 0.449500 -01	-0.449500 -01
26 0.155500 C3	-0.125180 00	78 0.453500 C3	0.445450 00	126 0.445450 00	0.278590 00
27 0.159500 C3	0.221560 00	79 0.457500 C3	0.832940 -01	127 0.832940 -01	0.525000 00
28 0.163380 C3	-0.376270 -01	80 0.461500 C3	5.227600 00	128 5.227600 00	-0.229220 -01
29 0.168500 C3	0.121910 -01	81 0.465500 C3	0.138150 00	129 0.138150 00	-0.212500 -01
30 0.172500 C3	0.235190 00	82 0.469500 C3	0.577600 -01	130 0.577600 -01	-0.144360 00
31 0.176500 C3	0.197820 -01	83 0.473500 C3	0.144360 00	131 0.144360 00	0.732760 00
32 0.180500 C3	0.216220 -01	84 0.477500 C3	0.116310 00	132 0.116310 00	-0.255610 -01
33 0.184500 C3	0.276520 -01	85 0.481500 C3	0.116310 00	133 0.116310 00	-0.144360 00
34 0.188500 C3	-0.111328 00	86 0.485500 C3	0.449500 -01	134 0.449500 -01	-0.449500 -01
35 0.192500 C3	0.217120 -01	87 0.489500 C3	0.144360 00	135 0.144360 00	0.138150 00
36 0.196500 C3	0.130280 00	88 0.493500 C3	0.577600 -01	136 0.577600 -01	-0.212500 -01
37 0.200500 C3	-0.572500 -01	89 0.497500 C3	0.116310 00	137 0.116310 00	-0.255610 -01
38 0.204500 C3	0.911720 -01	90 0.501500 C3	0.246450 -01	138 0.246450 -01	0.116310 00
39 0.207500 C3	0.204620 00	91 0.505500 C3	0.116310 00	139 0.116310 00	-0.255610 -01
40 0.211500 C3	-0.723440 -01	92 0.509500 C3	0.116310 00	140 0.116310 00	-0.144360 00
41 0.214500 C3	-0.667430 -01	93 0.513500 C3	0.449500 -01	141 0.449500 -01	-0.449500 -01
42 0.218500 C3	0.194000 00	94 0.517500 C3	0.144360 00	142 0.144360 00	0.138150 00
43 0.222500 C3	-0.137950 -01	95 0.521500 C3	0.577600 -01	143 0.577600 -01	-0.212500 -01
44 0.226500 C3	-0.165930 00	96 0.525500 C3	0.116310 00	144 0.116310 00	-0.255610 -01
45 0.230500 C3	-0.346680 -01	97 0.529500 C3	0.246450 -01	145 0.246450 -01	0.116310 00
46 0.235500 C3	-0.145710 -01	98 0.533500 C3	0.116310 00	146 0.116310 00	-0.255610 -01
47 0.239500 C3	-0.167290 00	99 0.537500 C3	0.246450 -01	147 0.246450 -01	0.116310 00
48 0.243500 C3	-0.326310 00	100 0.541500 C3	0.116310 00	148 0.116310 00	-0.255610 -01
49 0.247500 C3	-0.735180 -02	101 0.545500 C3	0.449500 -01	149 0.449500 -01	-0.449500 -01
50 0.251500 C3	-0.283510 00	102 0.549500 C3	0.144360 00	150 0.144360 00	0.138150 00
51 0.256500 C3	-0.717790 -02	103 0.553500 C3	0.577600 -01	151 0.577600 -01	-0.168120 00
52 0.260500 C3	-0.795270 -02	104 0.557500 C3	0.116310 00	152 0.116310 00	-0.212500 -01
53 0.263500 C3	-0.222845 01	105 0.561500 C3	0.246450 -01	153 0.246450 -01	0.116310 00
54 0.267500 C3	-0.423862 00	106 0.565500 C3	0.116310 00	154 0.116310 00	-0.255610 -01
55 0.271500 C3	0.906980 -01	107 0.569500 C3	0.449500 -01	155 0.449500 -01	-0.449500 -01
56 0.275500 C3	-0.669650 -01	108 0.573500 C3	0.144360 00	156 0.144360 00	0.138150 00
57 0.2810500 C3	0.301560 -01	109 0.577500 C3	0.577600 -01	157 0.577600 -01	-0.168120 00
58 0.2813500 C3	0.466720 00	110 0.581500 C3	0.116310 00	158 0.116310 00	-0.212500 -01
59 0.2817500 C3	-0.323820 00	111 0.585500 C3	0.246450 -01	159 0.246450 -01	0.116310 00
60 0.2821500 C3	0.144530 00	112 0.589500 C3	0.116310 00	160 0.116310 00	-0.255610 -01
61 0.2825500 C3	-0.281990 00	113 0.593500 C3	0.449500 -01	161 0.449500 -01	-0.449500 -01
62 0.2829500 C3	-0.264700 -01	114 0.597500 C3	0.144360 00	162 0.144360 00	0.138150 00
63 0.2833500 C3	-0.217550 00	115 0.601500 C3	0.577600 -01	163 0.577600 -01	-0.168120 00
64 0.2837500 C3	0.189430 00	116 0.605500 C3	0.116310 00	164 0.116310 00	-0.212500 -01
65 0.2841500 C3	-0.327360 00	117 0.609500 C3	0.246450 -01	165 0.246450 -01	0.116310 00
66 0.2845500 C3	0.362390 -01	118 0.613500 C3	0.116310 00	166 0.116310 00	-0.255610 -01
67 0.2849500 C3	0.225960 -01	119 0.617500 C3	0.449500 -01	167 0.449500 -01	-0.449500 -01

135	1.632500 C3	0.274720 00	137	0.652500 C3	-0.272370-01
136	0.642500 C3	0.221510 00	140	0.655500 03	-0.143150 00
137	0.644500 C3	-0.165070 00	141	0.660250 03	0.135770 00
138	0.645500 C3	0.103950 00	142	0.654500 C3	0.173430 00

SIGMA = SQRT((SUM OF SQUARES)/(MEXP-1)) = 0.16314



MULTIPLE REGRESSION GEOS 1
SELECTION 2

variable	mean	standard deviation	correlation	regression coefficient	std. error of reg. coeff.	computed t value
NO.			X VS. Y			
9	0.11402	1.57594	0.83835	0.33968	0.06699	46.57646
10	-0.02424	1.48505	-0.06838	-0.01588	0.0746	-2.12973
21	0.00560	0.61087	0.20756	0.25014	0.02680	9.33432
27	0.02810	0.33259	0.19415	0.38370	0.03463	11.15683
30	-0.03475	0.34410	0.00175	0.18491	0.07363	5.50297
55	-0.00601	0.42311	0.48504	0.29684	0.01200	24.73010
56	-0.02547	0.43616	-0.02570	-0.03398	0.01184	-2.87070
DEPENDENT	0.00114	0.65553				

INTERCEPT -0.02673

MULTIPLE CORRELATION 0.98105

STD. ERROR OF ESTIMATE 0.13028

ANALYSIS OF VARIANCE FOR THE REGRESSION

SOURCE OF VARIATION	DEGREES OF FREEDOM	SUM OF SQUARES	MEAN SQUARES	F VALUE
ATTRIBUTABLE TO REGRESSION	7	53.31595	3.33025	430.79956
DEVIATION FROM REGRESSION	134	2.27452	0.01697	
TOTAL	141	54.59047		

*****FREQUENCY DEPENDENT LOVE NUMBERS*****
(ASSUMING 2ND DEGREE TIDES ONLY)

*****OCEAN TIDE PARAMETERS*****
(ASSUMING 2ND DEGREE TIDES
ONLY AND SOLID EARTH LOVE
NUMBER K2=0.300 AND SOLID
EARTH TIDAL LAG=0.0 DEG)

L	M	P	O	TIDE	DIS	BODY	LOVE NUMBER	STD. ERROR	LAG ANGLE (DEGREES)	STD. ERROR (DEGREES)	C (CM)	STD. ERROR (CM)	PHASE (DEGREES)	STD. ERROR (DEGREES)
2	1	0	0	P1		MOON								
2	1	0	0			MOON								
2	1	0	1			MOON								
2	1	1	-1			MOON								
2	1	1	0	K1		MOON+SUN	0.24068	0.00495	2.67745	1.25557	7.92093	2.65155	10.7300	4.5983
2	1	1	1			MOON								
2	1	2	-1			MOON								
2	1	2	0			MOON								
2	1	2	1			MOON								
2	2	0	-1			MOON								
2	2	0	0	M2		MOON	0.25014	0.02580	0.0	0.0	5.03532	2.73349	270.0000	0.0
2	2	0	1			MOON								
2	2	1	-1			MOON								
2	2	1	0	K2		MOON+SUN	0.28926	0.02593	0.0	0.0	0.17294	0.41731	270.0000	0.0
2	2	1	1			MOON								
2	2	2	-1			MOON								
2	2	2	0			MOON								
2	2	2	1			MOON								
2	1	0	-1			SUN								
2	1	0	0	P1		SUN	0.18491	0.03360	0.0	0.0	4.60221	1.34373	180.0000	0.0
2	1	0	1			SUN								
2	1	1	-1			SUN								
2	1	1	0	K15		SUN								
2	1	1	1			SUN								
2	2	1	-1			SUN								
2	2	1	0	K15		SUN								
2	2	1	1			SUN								
2	2	2	-1			SUN								
2	2	2	0	S2		SUN	0.29878	0.01200	6.52989	2.27016	1.64422	0.57037	354.6259	20.1514
2	2	2	1			SUN								
2	2	2	1			SUN								
2	2	2	0			SUN								
2	2	2	1			SUN								

TIDAL INCLINATION

TIME (JAN 1, 0 HRS UT = 0)	INCLINATION (ARCSEC)	TIME (JAN 1, 0 HRS UT = 1)	INCLINATION (ARCSEC)
0.370000 02	-0.332850 00	58	0.171000 03
0.390000 02	-0.104790 01	59	0.017300 03
0.410000 02	-0.995360 00	60	0.175000 03
0.430000 02	-0.891870 00	61	0.177000 03
0.450000 02	-0.883450 00	62	0.179000 03
0.470000 02	-0.991170 00	63	0.191000 03
0.490000 02	-0.103920 01	64	0.133000 03
0.510000 02	-0.103840 01	65	0.185000 03
0.530000 02	-0.335250 00	66	0.197000 03
0.550000 02	-0.617830 00	67	0.149000 03
0.570000 02	-0.525110 00	68	0.019100 03
0.590000 02	-0.557910 00	69	0.019300 03
0.610000 02	-0.575940 00	70	0.195000 03
0.630000 02	-0.460950 00	71	0.197000 03
0.650000 02	-0.235240 00	72	0.199000 03
0.670000 02	-0.505380-01	73	0.201000 03
0.690000 02	-0.283510-01	74	0.203000 03
0.710000 02	-0.138170 00	75	0.019500 03
0.730000 02	-0.228400 00	76	0.019700 03
0.750000 02	-0.190850 00	77	0.211000 03
0.770000 02	-0.723550-01	78	0.213000 03
0.790000 02	-0.252300-01	79	0.215000 03
0.810000 02	-0.145100 00	80	0.217000 03
0.830000 02	-0.367360 00	81	0.219000 03
0.850000 02	-0.531320 00	82	0.221000 03
0.870000 02	-0.544650 00	83	0.223000 03
0.890000 02	-0.475560 00	84	0.225000 03
0.910000 02	-0.475000 00	85	0.227000 03
0.930000 02	-0.616750 00	86	0.229000 03
0.950000 02	-0.303270 00	87	0.231000 03
0.970000 02	-0.890550 00	88	0.233000 03
0.990000 02	-0.797840 00	89	0.235000 03
0.010000 03	-0.625140 00	90	0.237000 03
0.030000 03	-0.326590 00	91	0.239000 03
0.050000 03	-0.553270 00	92	0.241000 03
0.070000 03	-0.395440 00	93	0.243000 03
0.090000 03	-0.516090 00	94	0.245000 03
0.110000 03	-0.269980 00	95	0.247000 03
0.130000 03	-0.176920-01	96	0.249000 03
0.150000 03	-0.194400 00	97	0.251000 03
0.170000 03	-0.231790 00	98	0.253000 03
0.190000 03	-0.250370 00	99	0.255000 03
0.210000 03	-0.347580 00	100	0.257000 03
0.230000 03	-0.648270 00	101	0.259000 03
0.250000 03	-0.894980 00	102	0.261000 03
0.270000 03	-0.984510 00	103	0.263000 03
0.290000 03	-0.931020 00	104	0.265000 03
0.310000 03	-0.861520 00	105	0.267000 03
0.330000 03	-0.908280 00	106	0.269000 03
0.350000 03	-0.105380 01	107	0.271000 03
0.370000 03	-0.115380 01	108	0.273000 03
0.390000 03	-0.109070 01	109	0.275000 03
0.410000 03	-0.399620 00	110	0.277000 03
0.430000 03	-0.734660 00	111	0.279000 03
0.450000 03	-0.710530 00	112	0.281000 03
0.470000 03	-0.785760 00	113	0.283000 03
0.490000 03	-0.810360 00	114	0.285000 03
0.510000 03	-0.687350 00	115	0.287000 03
0.530000 03	-0.478210 00	116	0.289000 03
0.550000 03	-0.341220 00	117	0.291000 03
0.570000 03	-0.367310 00	118	0.293000 03
0.590000 03	-0.485950 00	119	0.295000 03
0.610000 03	-0.540000 00	120	0.297000 03
0.630000 03	-0.450660 00	121	0.299000 03
0.650000 03	-0.295400 00	122	0.301000 03
0.670000 03	-0.240410 00	123	0.303000 03
0.690000 03	-0.325090 00	124	0.305000 03

135	0.315000 03	0.310900 00	0.453000 03	0.934060 00
136	0.309000 03	0.315400 00	0.455000 03	0.959850 00
137	0.311000 03	0.383580 00	0.457000 03	0.916140 00
138	0.313000 03	0.346750 00	0.459000 03	0.947790 00
139	0.315000 03	0.563130 00	0.461000 03	0.110560 01
140	0.317000 03	0.413580 00	0.463000 03	0.128040 01
141	0.317000 03	0.235240 00	0.465000 03	0.131710 01
142	0.319000 03	0.314360 00	0.467000 03	0.118210 01
143	0.321000 03	0.393030 00	0.469000 03	0.994730 00
144	0.323000 03	0.370770 00	0.471000 03	0.904680 00
145	0.325000 03	0.218150 00	0.473000 03	0.936740 00
146	0.327000 03	0.558100-01	0.475000 03	0.958220 00
147	0.329000 03	0.771100-01	0.477000 03	0.851900 00
148	0.331000 03	0.148410 00	0.479000 03	0.614850 00
149	0.333000 03	0.235600 00	0.481000 03	0.365210 00
150	0.335000 03	0.296540 00	0.483000 03	0.255750 00
151	0.337000 03	0.174900 00	0.485000 03	0.281420 00
152	0.339000 03	0.519740-01	0.487000 03	0.305750 00
153	0.341000 03	0.630250-01	0.489000 03	0.203910 00
154	0.343000 03	0.187990 00	0.491000 03	-0.219800-02
155	0.345000 03	0.284300 00	0.493000 03	-0.165090 00
156	0.347000 03	0.222460 00	0.495000 03	-0.165830 00
157	0.349000 03	0.323180-01	0.497000 03	-0.391320-01
158	0.351000 03	0.147980 00	0.499000 03	0.621300-01
159	0.353000 03	0.132830 00	0.501000 03	0.257780-01
160	0.355000 03	0.141970 00	0.503000 03	-0.104360 00
161	0.357000 03	0.2145140 00	0.505000 03	-0.177800 00
162	0.359000 03	0.305100 00	0.507000 03	-0.932640-01
163	0.361000 03	0.565420 00	0.509000 03	0.672460-01
164	0.363000 03	0.759990 00	0.511000 03	0.151920 00
165	0.365000 03	0.616260 00	0.513000 03	0.935720-01
166	0.367000 03	0.765650 00	0.515000 03	-0.576500-01
167	0.369000 03	0.770860 00	0.517000 03	-0.166610 00
168	0.371000 03	0.912420 00	0.519000 03	-0.128330 00
169	0.373000 03	0.111060-01	0.521000 03	-0.366550-01
170	0.375000 03	0.120550 01	0.523000 03	-0.480880-01
171	0.377000 03	0.112710 01	0.525000 03	-0.224280 00
172	0.379000 03	0.951240 00	0.527000 03	-0.466540 00
173	0.381000 03	0.665850 00	0.529000 03	-0.615700 00
174	0.383000 03	0.902120 00	0.531000 03	-0.620110 00
175	0.385000 03	0.372930 00	0.533000 03	-0.579280 00
176	0.387000 03	0.927750 00	0.535000 03	-0.641950 00
177	0.389000 03	0.724410 00	0.537000 03	-0.841530 00
178	0.391000 03	0.477480 00	0.539000 03	-0.105780 01
179	0.393000 03	0.342230 00	0.541000 03	-0.113950 01
180	0.395000 03	0.355930 00	0.543000 03	-0.106010 01
181	0.397000 03	0.493180 00	0.545000 03	-0.943180 00
182	0.399000 03	0.341410 00	0.547000 03	-0.910460 00
183	0.401000 03	0.154500 00	0.549000 03	-0.103220 01
184	0.403000 03	0.272710-01	0.551000 03	-0.111640 01
185	0.405000 03	0.6220920-01	0.553000 03	-0.104850 01
186	0.407000 03	0.554870-01	0.555000 03	-0.835240 00
187	0.409000 03	0.188990 00	0.557000 03	-0.619890 00
188	0.411000 03	0.292570 00	0.559000 03	-0.535440 00
189	0.413000 03	0.102430 00	0.561000 03	-0.568560 00
190	0.415000 03	0.268720-01	0.563000 03	-0.577910 00
191	0.417000 03	0.951070-01	0.565000 03	-0.447120 00
192	0.419000 03	0.289290 00	0.567000 03	-0.211370 00
193	0.421000 03	0.448360 00	0.569000 03	-0.242490-01
194	0.423000 03	0.448440 00	0.571000 03	0.390230-03
195	0.425000 03	0.453550 00	0.573000 03	-0.74460-01
196	0.427000 03	0.316830 00	0.575000 03	-0.155900 00
197	0.429000 03	0.245960 00	0.577000 03	-0.828150-01
198	0.431000 03	0.285000 00	0.579000 03	-0.680000-01
199	0.433000 03	0.405240 00	0.581000 03	-0.142610 00
200	0.435000 03	0.448360 00	0.583000 03	-0.537880-01
201	0.437000 03	0.318070 00	0.585000 03	-0.124510 00
202	0.439000 03	0.778880-01	0.587000 03	-0.231190 00
203	0.441000 03	0.113600 00	0.589000 03	-0.184730 00
204	0.443000 03	0.167300 00	0.591000 03	-0.527450-01
205	0.445000 03	0.154120 00	0.593000 03	-0.182820-01
206	0.447000 03	0.226480 00	0.595000 03	-0.113770 00
207	0.449000 03	0.433470 00	0.597000 03	-0.252180 00
208	0.451000 03	0.743140 00	0.599000 03	-0.276120 00

283	0.601000 03	-0.131200 00	300	0.635000 03	0.362330 30
284	0.603000 03	0.779510-01	301	0.637000 03	0.101670 01
285	0.605000 03	0.197970 00	302	0.639000 03	0.01710 01
286	0.607000 03	0.187190 00	303	0.641000 03	0.84440 00
287	0.609000 03	0.157640 00	304	0.643000 03	0.573980 30
288	0.611000 03	0.254490 00	305	0.645000 03	0.319860 00
289	0.613000 03	0.499840 00	306	0.647000 03	0.254910 00
290	0.615000 03	0.765250 00	307	0.649000 03	0.67770 30
291	0.617000 03	0.902370 00	308	0.651000 03	0.330100 00
292	0.619000 03	0.892800 00	309	0.653000 03	0.530200-01
293	0.621000 03	0.854530 00	310	0.655000 03	-0.191870 30
294	0.623000 03	0.950560 00	311	0.657000 03	-0.345390 00
295	0.625000 03	0.114590 01	312	0.659000 03	-0.325810 00
296	0.627000 03	0.130910 01	313	0.661000 03	-0.213410 30
297	0.629000 03	0.130770 01	314	0.663000 03	-0.165760 30
298	0.631000 03	0.115640 01	315	0.665000 03	-0.292760 00
299	0.633000 03	0.100000 01			

RESIDUALS

TIME
(JAN 1, 0 HRS UT = 1)RESIDUAL
(ARCSEC)

1	0.385000 02	-0.123040 00	64	0.359500 C3	-0.691630 -01
2	0.515000 02	0.101080 00	70	0.351500 C3	-0.140320 00
3	0.535000 02	-0.483000 -01	71	0.367500 03	-0.109920 00
4	0.625000 C2	-0.195680 00	72	0.371500 C3	0.352290 -01
5	0.645000 02	0.690440 -01	73	0.377500 C3	0.657490 -01
6	0.593000 02	0.266040 -01	74	0.377500 02	-0.135680 00
7	0.685000 C2	-0.128690 00	75	0.381500 C3	0.65100 -01
8	0.725000 02	-0.206300 00	76	0.385500 03	-0.208940 00
9	0.665000 02	-0.152000 00	77	0.389500 03	0.114460 00
10	0.935000 02	-0.155010 00	78	0.397500 03	-0.209250 -01
11	0.945000 C2	0.239980 -01	80	0.401500 C3	0.597310 -01
12	0.985000 02	-0.697620 -02	81	0.405500 03	-0.210720 00
13	0.102500 C3	-0.113450 00	82	0.409500 C3	0.485350 -01
14	0.105500 C3	-0.199450 -01	83	0.413500 C3	-0.162510 00
15	0.110500 03	-0.195030 00	84	0.417500 C3	-0.229380 -01
16	0.114500 C3	0.411740 -02	85	0.422500 C3	0.187030 00
17	0.118500 C3	0.103620 00	86	0.426500 C3	-0.218650 -01
18	0.122500 03	0.103480 -01	87	0.430500 C3	0.128820 00
19	0.126500 C3	-0.113610 00	88	0.434500 C3	-0.561290 -01
20	0.130500 03	0.716180 -01	89	0.438500 C3	-0.142900 00
21	0.134500 C3	-0.101720 -02	90	0.442500 C3	-0.371150 -01
22	0.135500 C3	-0.699900 -01	91	0.446500 C3	-0.109310 00
23	0.134500 C3	0.242460 -01	92	0.450500 C3	0.101050 00
24	0.137500 C3	-0.377030 -01	93	0.454500 C3	0.174520 00
25	0.131500 C3	-0.365540 -02	94	0.458500 C3	-0.111750 00
26	0.155500 C3	-0.248460 -01	95	0.462500 C3	0.234410 -01
27	0.159500 C3	0.128480 00	96	0.466500 C3	-0.102240 00
28	0.153380 C3	-0.640330 -01	97	0.470500 C3	0.159860 -01
29	0.156500 C3	0.116780 00	98	0.474500 C3	-0.111320 00
30	0.172500 C3	0.107290 00	99	0.478500 C3	0.137550 -01
31	0.176500 C3	0.107930 00	100	0.482500 C3	-0.797920 -02
32	0.180500 C3	0.103170 00	101	0.486500 C3	0.286650 -01
33	0.134500 C3	-0.106560 00	102	0.490500 C3	-2.230790 00
34	0.188500 C3	-0.157080 -01	103	0.494500 C3	-0.457520 -01
35	0.192500 C3	0.133960 00	104	0.498500 C3	0.924950 -01
36	0.196500 C3	-0.160390 -01	105	0.502500 C3	0.872300 -01
37	0.200500 C3	0.427050 -01	106	0.506500 C3	0.150500 -01
38	0.204500 C3	0.959790 -01	107	0.521500 C3	-0.102580 00
39	0.207500 C3	0.461820 -01	108	0.525500 C3	0.923880 -01
40	0.211500 C3	0.131200 00	109	0.529500 C3	-0.517840 -01
41	0.214500 C3	0.949135 -01	110	0.533500 C3	0.151710 00
42	0.218500 C3	0.391200 -01	111	0.537500 C3	-0.612320 -01
43	0.222500 C3	0.371140 -01	112	0.541500 C3	0.773400 -01
44	0.226500 C3	-0.484820 -01	113	0.545500 C3	0.992870 -01
45	0.230500 C3	-0.162520 00	114	0.553500 C3	0.321440 -01
46	0.250500 C3	0.561120 -01	115	0.557500 C3	0.331470 00
47	0.270500 C3	-0.595480 -01	116	0.561500 C3	-0.576540 -01
48	0.273500 C3	-0.244750 00	117	0.565500 C3	0.237520 00
49	0.277500 C3	-0.157880 00	118	0.569500 C3	-0.824170 -01
50	0.281500 C3	-0.215530 00	119	0.573500 C3	0.180290 00
51	0.286500 C3	-0.732990 -02	120	0.577500 C3	0.296780 00
52	0.284500 C3	-0.145170 00	121	0.581500 C3	-0.487940 -01
53	0.293500 C3	0.758600 -01	122	0.585500 C3	0.205210 00
54	0.271500 C3	-0.182050 00	123	0.589500 C3	0.859490 -01
55	0.301500 C3	-0.409360 -01	124	0.593500 C3	0.262540 00
56	0.305500 C3	0.185700 -01	125	0.597500 C3	-0.551080 -01
57	0.310500 C3	-0.214200 -01	126	0.601500 C3	0.269170 00
58	0.313500 C3	0.137250 00	127	0.605500 C3	-0.195450 -01
59	0.317500 C3	-0.198400 00	128	0.609500 C3	0.155460 00
60	0.321500 C3	0.146940 00	129	0.613500 C3	-0.527600 -01
61	0.325500 C3	-0.397720 00	130	0.616500 C3	0.290100 00
62	0.329500 C3	0.114970 00	131	0.619500 C3	0.191990 00
63	0.333500 C3	-0.238430 00	132	0.623500 C3	-0.928280 -01
64	0.337500 C3	0.985450 -01	133	0.624500 C3	-0.333370 -01
65	0.341500 C3	-0.711240 -01	134	0.628500 C3	-0.601590 -01
66	0.345500 C3	-0.451860 -02	135	0.632500 C3	0.291720 00
67	0.349500 C3	-0.475740 -01	136	0.636500 C3	0.101710 00
68	0.353500 C3	-0.77751100 -01			

137 0.644500 C3
138 0.648500 C3
139 0.652500 C3

-0.36023D-01
0.79508D-01
-0.14542D-00

140 1.656500 C3
141 0.660250 C3
142 0.664500 C3

-3.13215D-01
0.10385D-00
0.82549D-01

SIGMA = SQRT((SUM OF SQUARES)/(MEXP-1)) = 0.12702

Table 1

Orbital Data for the BE-C, GEOS-I, and
GEOS-II Satellites

Satellite	Semimajor Axis (10^8 cm)	Inclination (degrees)	Eccentricity	Nodal Rate (degrees/day)
BE-C	7.5022	41.1667	0.025	-4.2535
GEOS-I	8.0729	59.3805	0.073	-2.2465
GEOS-II	7.7052	105.7896	0.033	1.3997

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Table 2

Tidal Parameters Derived from the Multiple Linear Regression Analyses of the Tidal Perturbations
 in the Orbital Inclinations of the BE-C, GEOS-I, and GEOS-II Satellites
 (The errors indicated are the formal statistical errors.)

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Satellite	Tide	ℓ_{mpq}	Period (days)	Amplitude (arc sec)	$c_{2\text{mp0}}$	$s_{2\text{mp0}}$	$d_{2\text{mp0}}$	$\delta_{2\text{mp0}}$ (deg)	C_{2m}^+ (cm)	ϵ_{2m}^+ (deg)
BE-C	O_1	2100	11.8	0.09	0.276 ± 0.077	-0.018 ± 0.088	0.28 ± 0.08	-3.6 ± 18.1	3.0 ± 8.1	144 ± 163
	K_1	2110	84.8	0.80	0.254 ± 0.010	0.025 ± 0.007	0.26 ± 0.01	5.7 ± 1.6	6.9 ± 1.2	29 ± 8
	M_2	2200	10.3	0.11	0.204 ± 0.053	0.030 ± 0.054	0.21 ± 0.05	8.4 ± 15.1	10.3 ± 5.4	287 ± 31
	K_2	2210	42.4	0.12	0.322 ± 0.065	0.128 ± 0.072	0.35 ± 0.06	21.7 ± 11.6	2.1 ± 1.2	10 ± 28
	P_1	2100	57.8	0.13	0.205 ± 0.036	-0.016 ± 0.041	0.21 ± 0.04	-4.5 ± 11.4	3.8 ± 1.5	170 ± 24
	S_2	2200	34.4	0.20	0.253 ± 0.030	0.025 ± 0.030	0.25 ± 0.03	5.6 ± 6.8	2.5 ± 1.4	298 ± 33
GEOS-I	O_1	2100	12.6	—	—	—	—	—	—	—
	K_1	2110	160.8	0.73	0.241 ± 0.005	0.011 ± 0.005	0.24 ± 0.01	2.7 ± 1.3	7.9 ± 0.7	11 ± 5
	M_2	2200	11.7	0.15	0.251 ± 0.027	0.017 ± 0.027	0.25 ± 0.03	3.9 ± 6.1	5.3 ± 2.8	289 ± 29
	K_2	2210	80.4	0.18	0.284 ± 0.034	0.000 ± 0.035	0.28 ± 0.03	0.0 ± 7.1	0.3 ± 0.6	270 ± 122
	P_1	2100	85.4	0.09	0.181 ± 0.044	0.010 ± 0.045	0.18 ± 0.04	3.3 ± 14.2	4.8 ± 1.8	185 ± 22
	S_2	2200	55.7	0.39	0.297 ± 0.012	0.034 ± 0.012	0.30 ± 0.01	6.6 ± 2.3	1.7 ± 0.6	355 ± 20
GEOS-II	O_1	2100	14.4	—	—	—	—	—	—	—
	K_1	2110	255.4	0.81	0.257 ± 0.021	-0.046 ± 0.013	0.26 ± 0.02	-10.2 ± 2.7	8.4 ± 2.2	313 ± 16
	M_2	2200	15.3	0.25	0.242 ± 0.025	0.050 ± 0.025	0.25 ± 0.02	11.7 ± 5.7	7.8 ± 2.5	311 ± 18
	K_2	2210	127.7	0.44	0.306 ± 0.023	0.012 ± 0.029	0.31 ± 0.02	2.2 ± 5.3	0.2 ± 0.5	28 ± 105
	P_1	2100	629.8	0.28	0.050 ± 0.022	-0.107 ± 0.037	0.12 ± 0.03	-65.0 ± 12.3	10.9 ± 1.0	157 ± 7
	S_2	2200	434.7	4.58	0.340 ± 0.007	-0.015 ± 0.004	0.34 ± 0.01	-2.5 ± 0.6	2.1 ± 0.3	111 ± 6

Table 3

Secular Changes in the Moon's Orbit and the Earth's Orientation
and Spin, and the Dissipation of Energy for Selected Tides
(The entries are a weighted average over all three satellites
The errors indicated are the formal statistical errors)

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$\dot{X}_{\ell_{mpq}}$	$[X]_{\ell_{mpq}}$ (Moon)				$[X]_{\ell_{mpq}}$ (Sun)			
	2100	2110	2200	2210	2100	2110	2200	2210
\dot{n}_M (arc sec/(100 yr) 2)	3 ± 13	0	-29 ± 15	0	—	—	—	—
\dot{a}_M (cm/yr)	-0.4 ± 1.9	0	4.3 ± 2.2	0	—	—	—	—
\dot{e}_M (/10 ⁹ yr)	0.0 ± 0.001	0	-0.002 ± 0.001	0	—	—	—	—
\dot{j} (deg/10 ⁹ yr)	-0.3 ± 1.5	-0.2 ± 0.1	-0.7 ± 0.3	-0.0 ± 0.1	—	—	—	—
\dot{i}_s (deg/10 ⁹ yr)	-1.9 ± 9.2	-0.7 ± 0.3	3.2 ± 1.6	-0.1 ± 0.2	-1.0 ± 0.5	-0.2 ± 0.1	-0.2 ± 0.1	-0.0 ± 0.1
$\dot{\theta}$ (10 ⁻²² rad/sec 2)	0.3 ± 1.4	-0.1 ± 0.1	-6.3 ± 3.2	-0.0 ± 0.1	0.1 ± 0.1	-0.0 ± 0.1	$+0.4 \pm 0.2$	-0.0 ± 0.1
\dot{E} (10 ¹⁹ erg/sec)	0.1 ± 0.7	-0.1 ± 0.1	-3.6 ± 1.8	-0.0 ± 0.1	0.1 ± 0.1	-0.0 ± 0.1	$+0.2 \pm 0.1$	-0.0 ± 0.1

Table 4

Secular Changes in the Moon's Orbit and the Earth's Orientation
and Spin, and the Dissipation of Energy for Selected Tides
(The entries are a weighted average over the BE-C and GEOS-I satellites
The errors indicated are the formal statistical errors)

\dot{X}	ℓ_{mpq}	[X] ℓ_{mpq} (Moon)				[X] ℓ_{mpq} (Sun)			
		2100	2110	2200	2210	2100	2110	2200	2210
\dot{n}_M (arc sec/(100 yr) ²)		3 ± 13	0	-17 ± 20	0	—	—	—	—
\dot{a}_M (cm/yr)		-0.4 ± 1.9	0	2.4 ± 3.0	0	—	—	—	—
\dot{e}_M ($/10^9$ yr)		0.0 ± 0.001	0	-0.001 ± 0.001	0	—	—	—	—
\dot{j} (deg/ 10^9 yr)		-0.3 ± 1.5	-0.3 ± 0.1	-0.4 ± 0.5	-0.0 ± 0.1	—	—	—	—
\dot{i}_s (deg/ 10^9 yr)		-1.9 ± 9.2	-1.3 ± 0.3	1.8 ± 2.3	-0.2 ± 0.2	-0.1 ± 0.7	-0.3 ± 0.1	0.7 ± 0.2	-0.0 ± 0.1
$\dot{\theta}$ (10^{-22} rad/sec ²)		0.3 ± 1.4	-0.2 ± 0.1	-3.6 ± 4.4	-0.0 ± 0.1	0.0 ± 0.1	-0.0 ± 0.1	-1.3 ± 0.4	-0.0 ± 0.1
\dot{E} (10^{19} erg/sec)		0.1 ± 0.7	-0.1 ± 0.1	-2.0 ± 2.5	-0.0 ± 0.1	0.0 ± 0.1	-0.0 ± 0.1	-0.7 ± 0.3	-0.0 ± 0.1

Table 5

$P_{\ell_{\text{mpq}}}$ for $\ell = 2$, $q = 0$ for the Quantities Shown in the Left-Hand Column

\dot{x}	ℓ_{mpq}	$P_{\ell_{\text{mpq}}} \text{ (Moon)}$						$P_{\ell_{\text{mpq}}} \text{ (Sun)}$					
		2100	2110	2120	2200	2210	2220	2100	2110	2120	2200	2210	2220
\dot{n}_M (arc sec/(100 yr) ²)	-144.6	0	+0.3	-847.1	0	+0.0	-	-	-	-	-	-	-
\dot{a}_M (cm/yr)	+ 21.4	0	-0.0	+125.1	0	-0.0	-	-	-	-	-	-	-
\dot{e}_M (/10 ⁹ yr)	- 0.0076	0	+0.0	- 0.0447	0	+0.0	-	-	-	-	-	-	-
\dot{j} (deg/10 ⁹ yr)	+ 16.7	-18.2	-0.1	- 19.4	-1.9	-0.0	-	-	-	-	-	-	-
\dot{i}_s (deg/10 ⁹ yr)	+105.3	-81.0	-0.6	+ 94.0	-8.4	-0.0	+22.5	-17.5	-0.1	+19.9	-1.6	-0.0	-
$\dot{\theta}$ (10 ⁻²² rad/sec ²)	- 15.6	-14.2	-0.0	-182.8	-1.5	0.0	- 3.3	- 3.1	-0.0	-38.7	-0.3	-0.0	-
\dot{E} (10 ¹⁹ erg/sec)	- 8.5	- 8.3	-0.0	-103.6	-0.9	-0.0	- 2.0	- 1.8	-0.0	-22.8	-0.2	-0.0	-

C.2

92

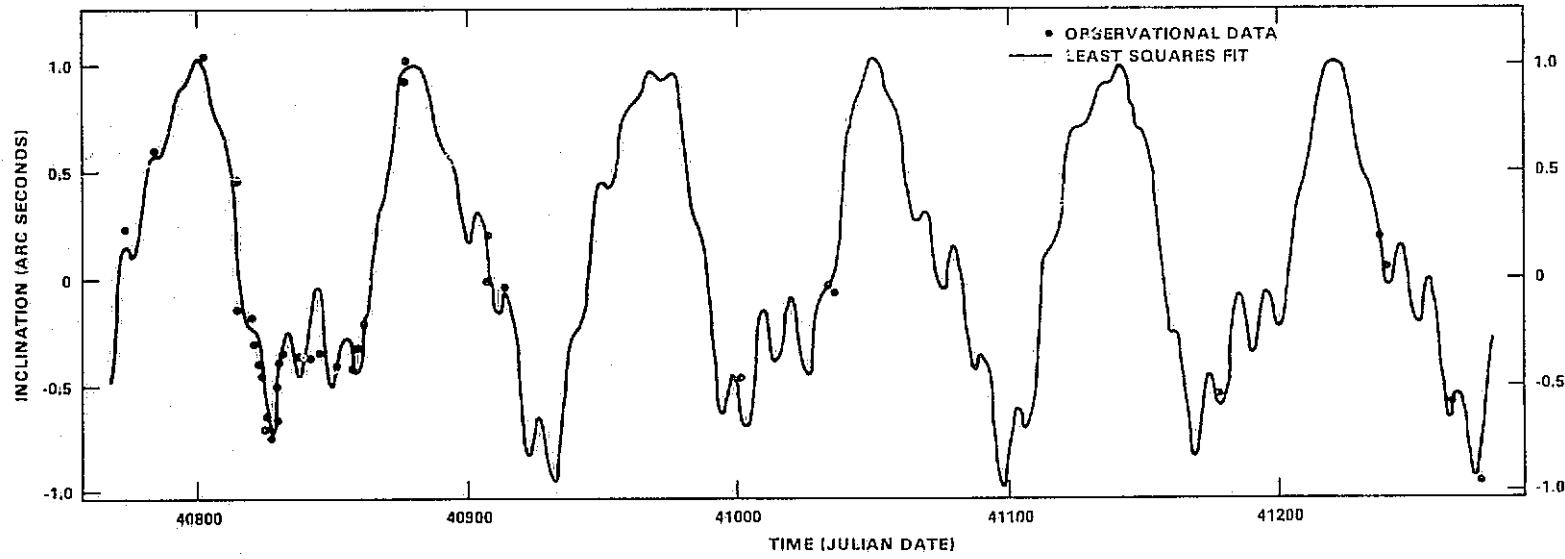


Figure 1. Inclination Data and Regression Curve for BE-C

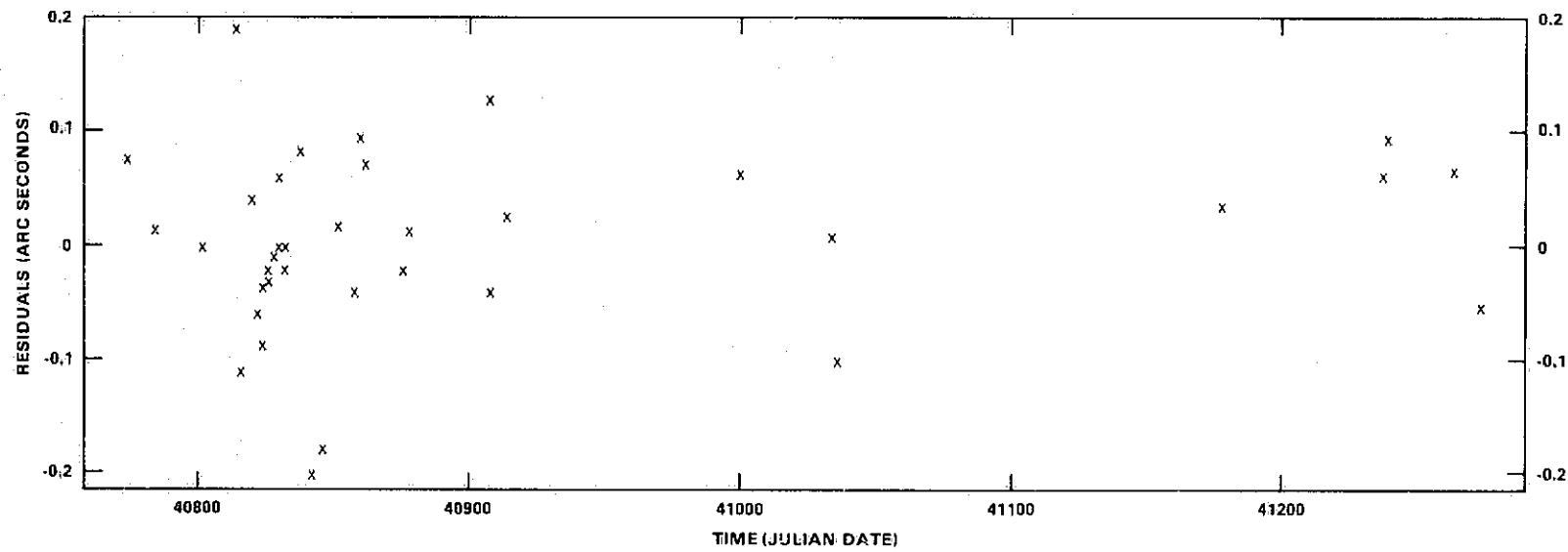


Figure 2. Residuals for Regression Curve Shown in Figure 1.
 Standard Error of Estimate: 0.0626

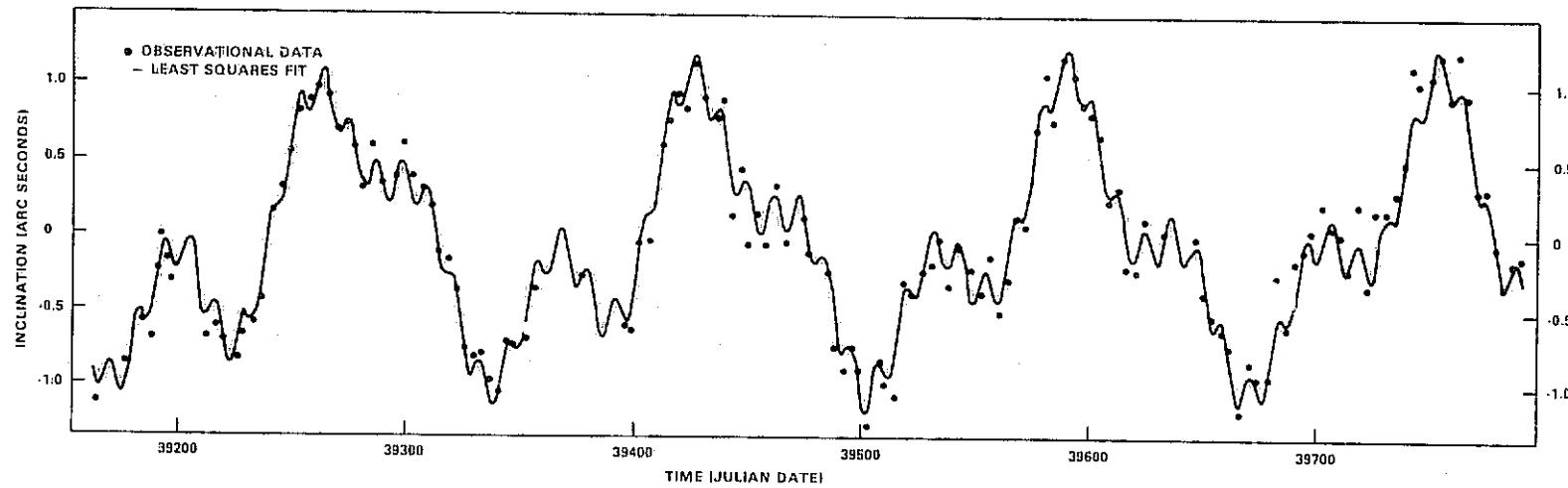


Figure 3. Inclination Data and Regression Curve for GEOS-I

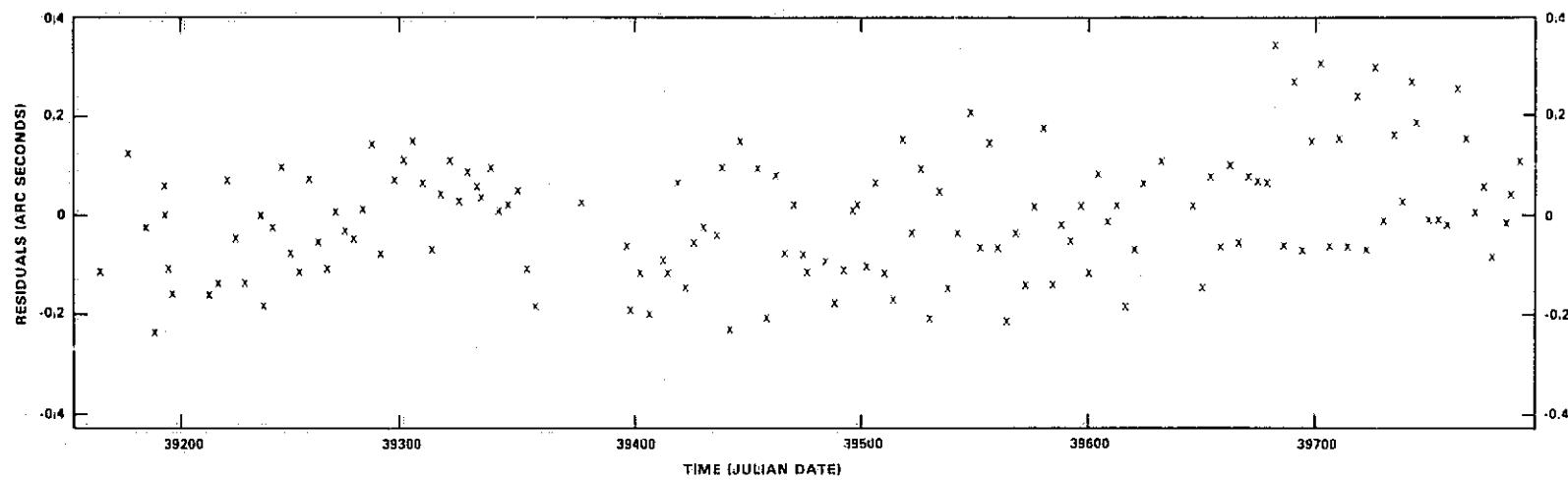


Figure 4. Residuals for Regression Curve Shown in Figure 3.
Standard Error of Estimate: 0.132

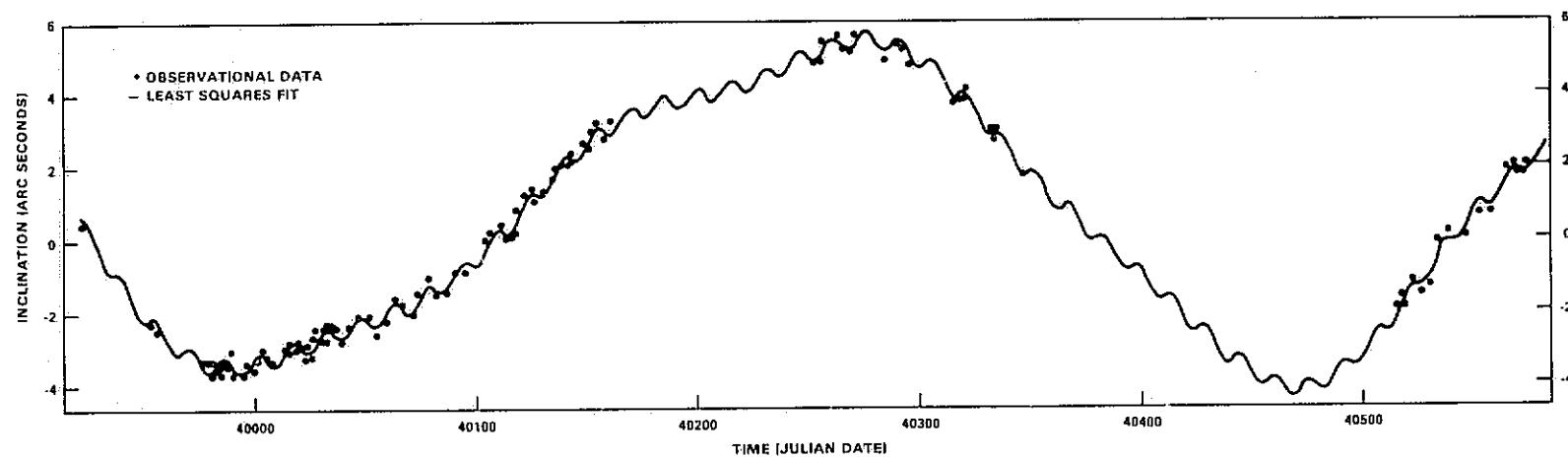


Figure 5. Inclination Data and Regression Curve for GEOS-II

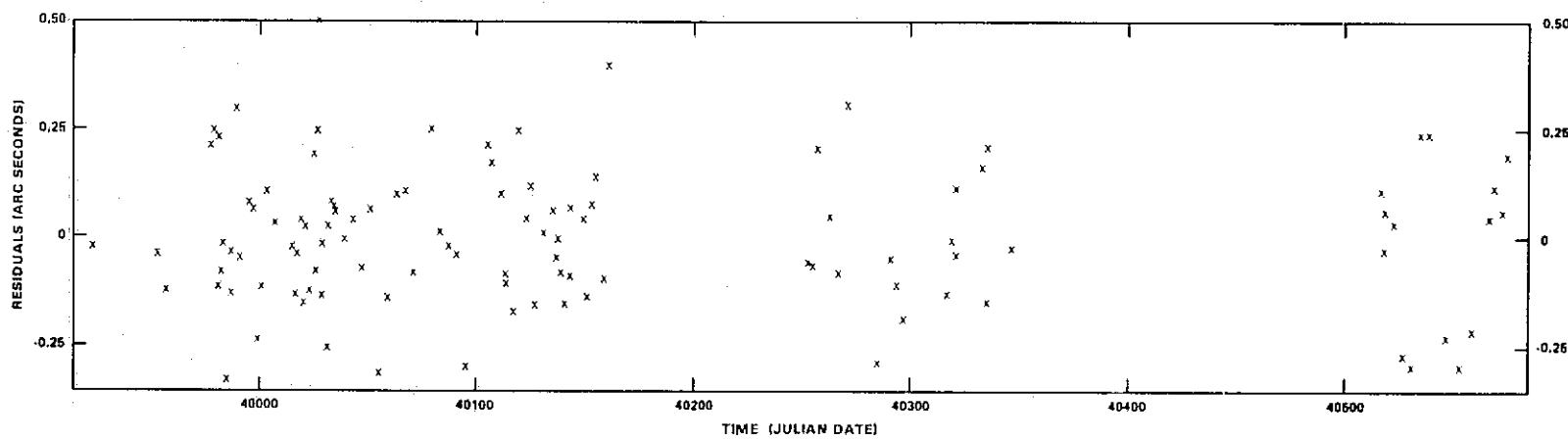


Figure 6. Residuals for Regression Curve Shown in Figure 5.
Standard Error of Estimate: 0.175

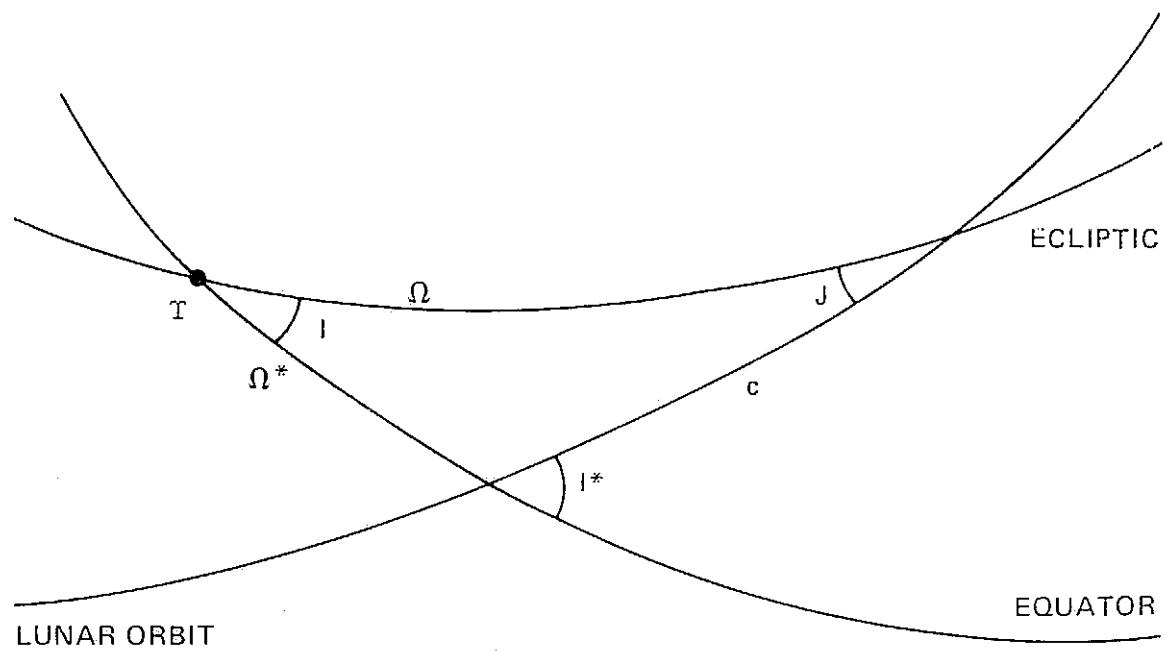


Figure 7. Spherical Triangle Used for Computing the Moon's Position With Respect to the Earth's Equator